Model checking: Introductory examples

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Formal verification: Goals



Example 1: Mutual exclusion protocol

An engineering task

- Let us consider a concurrent (multi-process) system
- At most one process is allowed to access a shared resource at a time (mutual exclusion is required)
 - Example: Use of communication channel
 - Access to resource: "Critical sections" in the programs; at most one process is allowed to be in critical section
 - The platform (OS, framework) does not give support: no semaphore, no monitor, etc.
 - Only shared variables can be used (atomic reading/writing)
- How to do it?
 - Classical solutions (Peterson, Lamport, Fischer etc.)
 - Custom algorithm

Algorithm for mutual exclusion

- 2 processes, 3 shared variables (H. Hyman, 1966)
 - o **blocked0**: process 1 (P0) wants to enter
 - o **blocked1**: process 2 (P1) wants to enter
 - **turn**: which process is allowed to enter (0 for P0, 1 for P1)



Is the algorithm correct?

The model in UPPAAL (version 1)

Declarations:

bool blocked0; bool blocked1; int[0,1] turn=0; system P0, P1;

Automaton PO:

Used modeling artefacts:

- Global variables
- Variables with restricted domain



The model in UPPAAL (version 2)

Declarations:

bool blocked[2]; int[0,1] turn; P0 = P(0); P1 = P(1); system P0,P1;

Template P with parameter const int pid:



Used modeling artefacts:

- Global variables
- Variables with restricted domain
- Variables of array type
- Modeling common behavior with templates
- Template instantiation with parameters

```
while (true) { P0
    blocked0 = true;
    while (turn!=0) {
        while (blocked1==true) {
            skip;
        }
        turn=0;
    }
    // Critical section
    blocked0 = false;
    // Do other things
}
```

Properties to verify in the example

- Mutual exclusion:
 - At most one process is allowed to be in the critical section
- The expected behavior is possible:
 - For P0 it is possible to enter the critical section
 - For P1 it is possible to enter the critical section
- Starvation freedom:
 - PO shall eventually enter the critical section
 - P1 shall eventually enter the critical section
- Deadlock freedom:

It is not possible that processes are just waiting

How to do model checking in UPPAAL?

- Atomic propositions:
 - Values of variables can be referred: e.g., a!=1
 - Using integer arithmetic and bit operations
 - Control locations can be referred: e.g., Train.cross
 - For parameterized processes: forall, exists quantifiers
 - **Deadlock** (no action): Specific deadlock proposition
- Boolean operators:

o and, or, imply, not, ? : (this latter is the "if-then-else")

- Temporal operators: Restricted CTL
 - Notation: [] instead of G, and <> instead of F
 - This way we have CTL operators: A[], A<>, E[], E<>
 - [] is also interpreted on finite paths (till the last state)
 - Temporal operators cannot be nested
 - But there is a special operator: p-->q means A[] (p imply A<> q)

Configuring model checking in UPPAAL

- Set of properties can be provided
 Model checking can be initiated one-by-one
- Diagnostic trace (counter-example or witness) can be generated
 - Some, shortest, or fastest
 - It is loaded into the simulator (for debugging)
- Search order in the state space:
 - Depth-first, random depth-first
 - Breadth-first
- State space representation:
 - Compact data structure
 - Under- / over-approximation
 - Hash table size can be specified

UPPAAL: Formalizing requirements

Mutual exclusion:

At most one process is allowed to be in the critical section

A[] not (P0.cs and P1.cs)

Labels for critical sections: PO.cs and P1.cs

- The expected behavior is possible:
 - For P0 it is possible to enter the critical section: E<>(P0.cs)
 - For P1 it is possible to enter the critical section: E<>(P1.cs)
- Starvation freedom:

PO shall eventually enter the critical section: A<>(PO.cs) P1 shall eventually enter the critical section: A<>(P1.cs)

Deadlock freedom:

It is not possible that processes are just waiting: A[] not deadlock

UPPAAL: Results of model checking

- Mutual exclusion is not ensured
 - Counterexample: specific interleaving between the processes (can be replayed in simulator)
- No deadlock
- The expected behavior is possible
- Starvation freedom cannot be checked without extending the model with timing
 - Trivial counterexample: Time elapses indefinitely in the initial location
 - Valid timed behavior in the model
 - Enforcing progress: urgent location, or location invariants
 - Starvation freedom?
 - The system is not starvation free (cyclic counterexample exists)

Fixing the algorithm: Mutual exclusion ensured

Hyman's algorithm

 For process P0 (P1 analogously):

Hyman:

```
while (true) {
    blocked0 = true;
    while (turn!=0) {
        while (blocked1==true) {
            skip;
        }
        turn=0;
    }
    // Critical section
    blocked0 = false;
    // Do other things
}
```

Peterson's algorithm

 For process P0 (P1 analogously):

Peterson:

```
while (true) {
    blocked0 = true;
    turn=1;
    while (blocked1==true &&
        turn!=0) {
            skip;
    }
    // Critical section
```

blocked0 = false;
// Do other things

}



The problem

Game: Rolling a dice

- n players, 1 referee
- Each player rolls a dice once
- Then tells the result to the referee
- The referee
 - Collects all results
 - Finds the largest result(s)
 - Announces the winner(s)
- Players count the number of their winning rounds
- The winner of the game is who won 10 rounds

What do we have to solve:

- Generate random value
- Communication
 - Value passing
 - Broadcast communication
 - Handling channel arrays
 - Ordering of update sections
- Data structures
- Functions
- Concurrency and timing
- Model checking

Basic idea for the solution: Sketch of the models



Possibilities for modelling transitions in UPPAAL



Solution: System and the player



system Player, Referee;

```
const int players = 3;
const int wins = 10;
```

```
typedef int[0,players-1] id_t;
typedef int[0,6] dice_t;
```

struct {
 id_t who;
 dice_t what;
} roll;

id_t winner;

chan say;

broadcast chan announce;





- In each execution, there is a player who is the winner of the game
 - $\circ~$ The count of the highest rolls reaches the value of wins

A<> exists (i : id_t) (Player(i).count == wins)

- Referee decides if all players made their rolls
 - This happens at least once:

E<> Referee.Decision && forall (i : id_t) (Referee.rolls[i] > 0)

• This happens eventually on all paths:

A<> Referee.Decision && forall (i : id_t) (Referee.rolls[i] > 0)

- The system has no deadlock
 - There is no such state, which has no enabled transition to another state
 A[] not deadlock

Overview

A<> exists (i : id_t) (Player(i).count == wins)			
A<> Referee.Decision && forall (i : id_t) Referee.rolls[i] > 0			
E<> Referee.Decision && forall (i : id_t) Referee.rolls[i] > 0			
A[] not deadlock Remove			
Comments			
Query			
A<> exists (i : id_t) (Player(i).count == wins)			
Comment			
Status			
A[] not deadlock			
Established direct connection to local server.			
(Academic) UPPAAL version 4.0.13 (rev. 4577), September 2010 server.			
The verification was aborted due to an error. Most likely, this is caused by an out-of-range assignment or out-of-range array lookup.			
E<> Referee.Decision && forall (i : id_t) Referee.rolls[i] > 0			
Property is satisfied.			
A<> Referee.Decision && forall (i : id_t) Referee.rolls[i] > 0			
Property is not satisfied.			
A<> exists (i : id_t) (Player(i).count == wins)			
Property is not satisfied.			

Overview

		and the second second second second
A<> exists (i : id_t) (Player(i).count =	== wins)	Check
A<> Referee.Decision && forall (i : id_t	;) Referee.rolls[i] > 0	Check
E<> Referee.Decision && forall (i : id_t	c) Referee.rolls[i] > 0	Insert
A[] not deadlock	•	Remove
		Comments
Query		
A<> exists (i : id_t) (Player(i).count == wins)	Oeadlock-freeness: at	oorted
Comment	 Win counters may c 	overflow in
	the current model	
	 (We will not correct 	t it now)
Status		
A[] not deadlock	7	
Established direct connection to local server.		
(Academic) UPPAAL version 4.0.13 (rev. 4577), Septembe	r 2010 server.	
The verification was aborted due to an error. Most likely, t	his is caused by an out-of-range assignment or out-of-ran	nge array lookup.
E<> Referee.Decision && forall (i : id_t) Referee.rolls[i] >	0	

Property is satisfied.

A<> Referee.Decision && forall (i : id_t) Referee.rolls[i] > 0

Property is not satisfied.

A<> exists (i : id_t) (Player(i).count == wins)

Property is not satisfied.

111

Overview

<pre>A<> exists (i : id_t) (Player(i).count == A<> Referee.Decision && forall (i : id_t) E<> Referee.Decision && forall (i : id_t) A[] not deadlock</pre>	<pre>wins) Referee.rolls[i] > 0 Referee.rolls[i] > 0 Referee.rolls[i] > 0 Check Insert Remove Comments</pre>
A<> exists (i : id_t) (Player(i).count == wins) Comment	It is possible to reach a state where every player has sent their result and the referee has noted them.
Status A[] not deadlock Established direct connection to local server. (Academic) UPPAAL version 4.0.13 (rev. 4527), September 2 The verification was aborted due to an error. Most likely, this E<> Referee.Decision && forall (i : id_t) Referee.rolls[i] > 0 Property is satisfied. A<> Referee.Decision && forall (i : id_t) Referee.rolls[i] > 0 Property is not satisfied. A<> exists (i : id_t) (Player(i).count == wins) Property is not satisfied.	2010 server. s is caused by an out-of-range assignment or out-of-range array lookup.

Overview A<> exists (i : id_t) (Player(i).count == wins) Check A<> Referee.Decision && forall (i : id t) Referee.rolls[i] > 0 Insert E<> Referee.Decision && forall (i : id t) Referee.rolls[i] > 0 Remove A[] not deadlock Comments Ouery A<> exists (i : id_t) (Player(i).count == wins) But there is a path where no such state is reachable! Comment Trivial counterexample: Timing Other counterexample: Wrong use of concurrency Status All not deadlock Established direct connection to local server. (Academic) UPPAAL version 4.0.13 (rev. 4577), September 2010 -- server. The verification was aborted due to an error. Most likely, this is caused by an out-of-range assignment or out-of-range array lookup. E<> Referee.Decision && forall (i : id_t) Referee.rolls[i] > 0 Property is satisfied. A<> Referee.Decision && foral (i : id_t) Referee.rolls[i] > 0 Property is not satisfied. 🖉 A<> exists (i : id_t) (Player(i).count == wins) Property is not satisfied.

Avoiding trivial counterexample by state invariants

- If we examine all possible paths (e.g. A<>) then UPPAAL also checks the possibility of not leaving a state (if it is a valid behavior)
- Solution: State (location) invariant
 - Add a clock variable
 - Initialize when entering the state
 - Not leaving a state is valid until the state invariant holds (here in the example: for at most 1 time units)



Wrong concurrency – why?



MŰEGYETEM 1782

Avoiding wrong concurrency (dice_roll_1.1)



- Problem: Concurrent activities of the players on shared variable
 Registering the results: writing to the roll shared variable
 - Communication with the referee: using roll with the say! transition
- Potential solution:
 - Implementing atomic "update and send" operations by introducing a "committed" state (it must be left instantly)

Special constructs that can be used (dice_roll_2.0)

- Monitoring an array of channels
 - The receiving process checks all channels "at once" using a Select construct
 - Synchronization is performed on the channel that is ready
 - Channel id can be used in the Update section
 - Model checker will examine all potential synchronizations



```
Using iterators in functions
void reset_rolls() {
for (i : id_t) rolls[i] = 0;
}
```

```
void find_winner() {
  for (i : id_t) {
    if (rolls[i] > best) {
        best = rolls[i];
        winner = i;
     }
    }
    best = 0;
}
```

"Compact" model

- Using arrays of channels
- Applying operator
 "? :"
- Collecting results in a single state
- Using iterators
- Reset state can be omitted



Other modeling advices and practices

- Order of evaluating arc expressions:
 Select » Guard » Sync » Update
 - On a synchronized arc, Update of the sender is evaluated before the Update of the receiver (but not before the evaluation of the Guard of the receiver)
 - Cannot test (in a guard) a global variable that was set by synchronized arc
- Using functions: Debugging is difficult
 - Statement by statement simulation is not possible
- When verifying properties such as A<> q, clock variables must be used to avoid the trivial counterexample (not leaving a state)
 - Note: A<> is also included in "leads to": p --> q means A[] (p imply A<> q)
 - Do not forget to reset clock variables when necessary
- The model checker of UPPAAL cannot check deadlocks when using channel or automata level priorities (these should be avoided)