# **Hierarchical Petri nets**

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## Hierarchical modeling

- Hierarchy: Model elements are placed on different levels of hierarchy
  - Clarity: System > subsystem > component
  - Reusable elements
- Model refinement (top-down style)
  - Systematically giving more details to elements
    - Subsystems are expanded during design
  - Removing "uncertainties"
    - Transparent (glass-)box from black box
- Model building (bottom-up style)
  - Building from subnets: as a higher level element
  - Goal is to reduce local complexity  $\rightarrow$  clarity

## **Example:** Refining activities

- Modeling: Systematic refinement of transitions
  - Giving more details to the activity
- Substituting partial Petri net models
  - Starting and ending with a transition
  - Original input and output arcs are connected to these
- Advices
  - A non-detailed activity can be used later for refinements
  - Detailed modeling increases complexity

#### Example: Transition refinement



**Hierarchical Petri nets** 

- "Main net" on top of hierarchy
- "Subnets" as building blocks
  - Transition to be refined
  - Place to be refined
- "Interaction points" between subnets: Transitions or places
  - Interface transition
  - Interface place

Systematic refinement of transitions

- Refine transition with subnet
  - Higher level net: Transition to be refined as substitute transition ("coarse transition")
  - Places of the higher level net can be connected (arcs)
  - Connected places appear in the subnet (for building subnet)



### Systematic refinement of places

- Refine place with subnet
  - Higher level net: Place to refine as substitute place ("coarse place")
  - Transitions of the higher level net can be connected (arcs)
  - Connected transitions appear in the subnet (for building subnet)

# Supporting hierarchy

#### • DNAnet tool

- Building from subnets (bottom-up)
  - Interaction points: places or transitions
  - Arcs between subnets can be connected to interaction points
- Not a systematic refinement, only subnet reuse
- PetriDotNet tool
  - Coarse transition: subnet from transition
- Snoopy tool
  - Coarse transition: subnet from transition
  - Coarse place: subnet from place
  - Increasing clarity: global places / transitions

### **DNAnet ABP example: Processes**

#### • Adding subnets:

- Systematic model refinement is not supported
- Reuse of elements is supported
- Process subnets
  - Interaction points are transitions here

Sender subnet



#### **Receiver** subnet



## **DNAnet ABP example: Channels and connections**

- Channel subnets
  - Interaction points are places here



- Connecting subnets
  - Arcs between subnets: defining source and target interaction points



#### PetriDotNet: Connect subnets

- Refineable element: Coarse transition
  - Input and output places can be added
  - These appear in the subnet ("as a reference")



#### PetriDotNet ABP example: Sender process subnet



# Summary

- Hierarchical modeling
  - Model refinement
  - Model building
- Systematic model refinement
  - Coarse transitions
  - Coarse places
- Model building: reusing subnets
  - Interaction points: transitions or places