

Software Model Checking with Abstraction-Based Methods

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INTRODUCTION

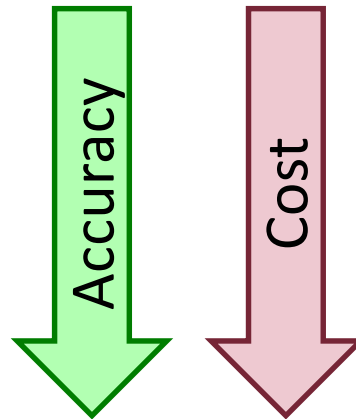
Introduction

■ Motivation

- Checking the **source code directly**
- Should work by “pushing a button”
 - No deep background knowledge should be required

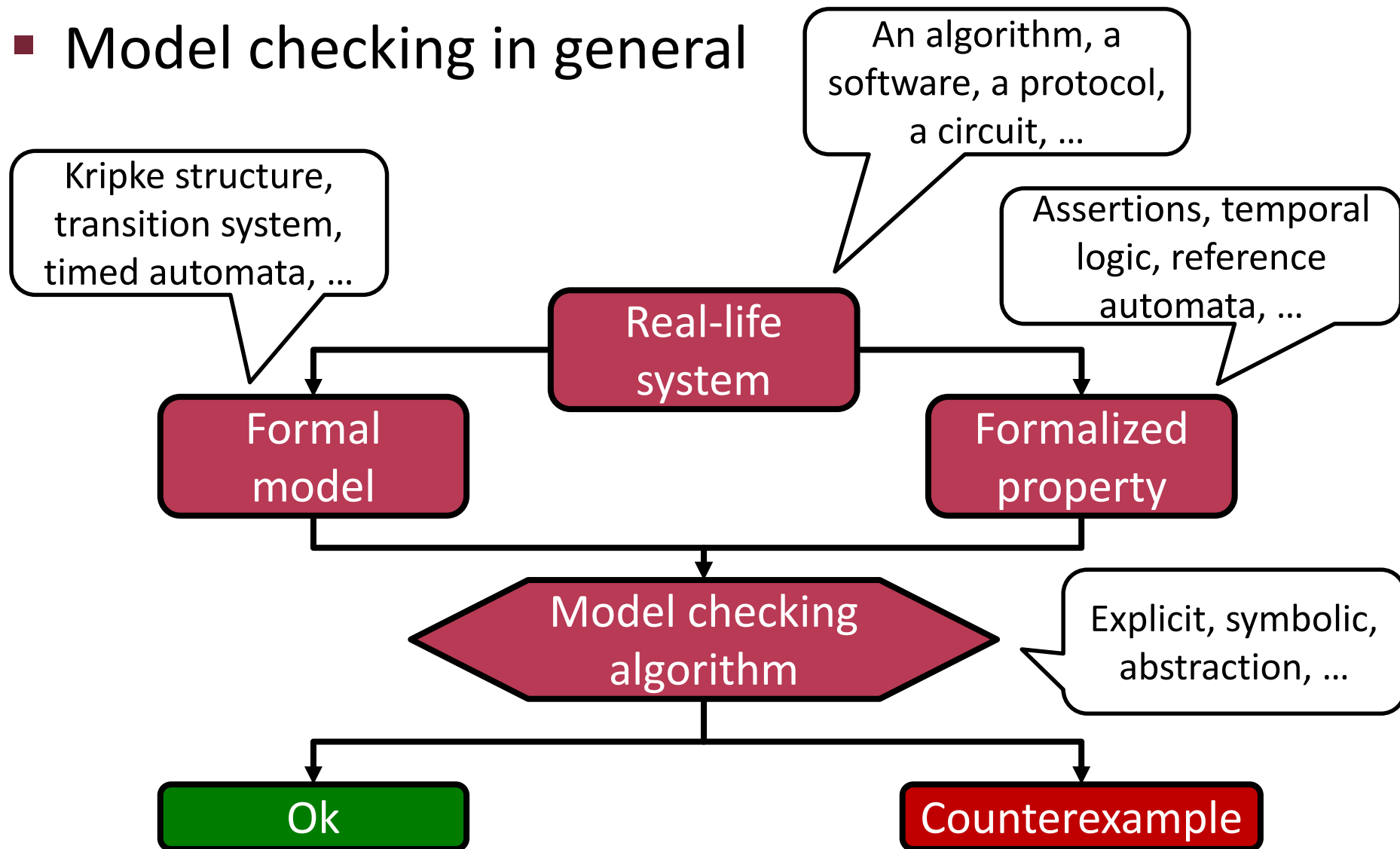
■ Typical software verification techniques

- Static analysis
 - Error patterns
 - Abstract interpretation
- **Model checking**



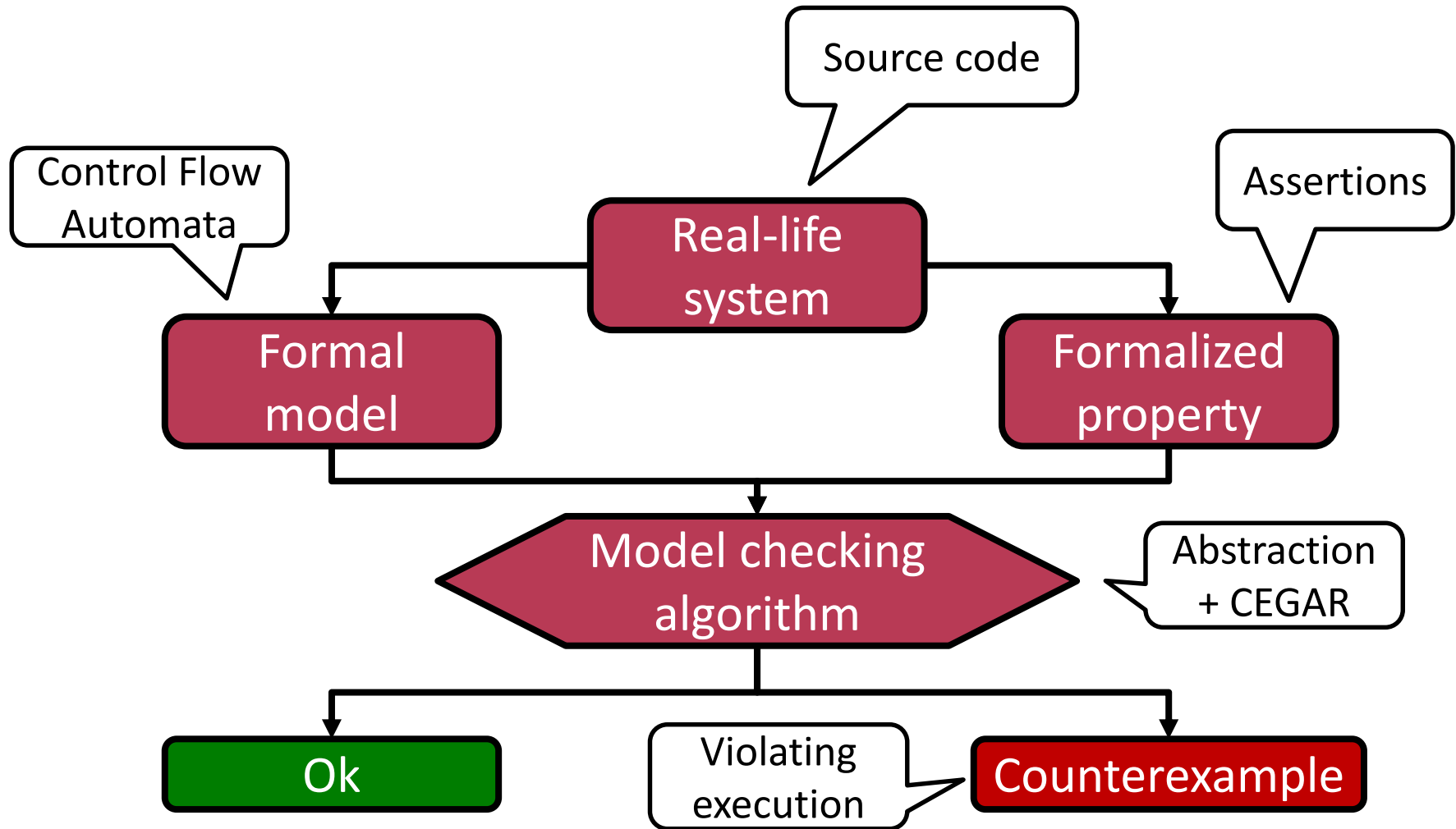
Introduction – Model Checking

■ Model checking in general



Introduction – Model Checking

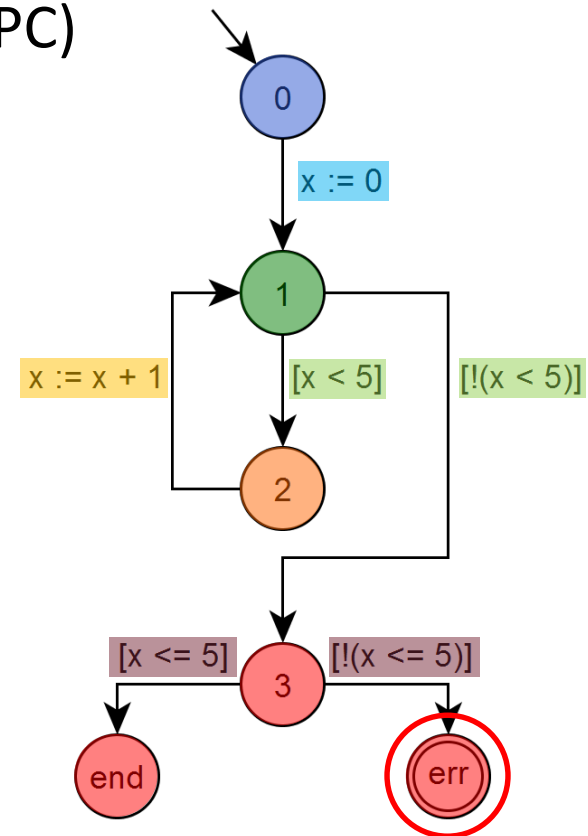
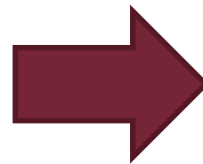
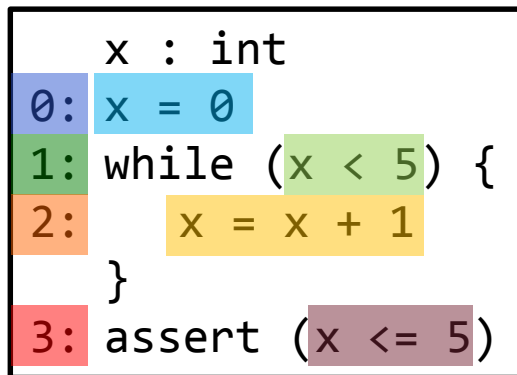
- This lecture: focus on **software** and **abstraction**



Introduction – Model and Property

Control-Flow Automata (CFA)

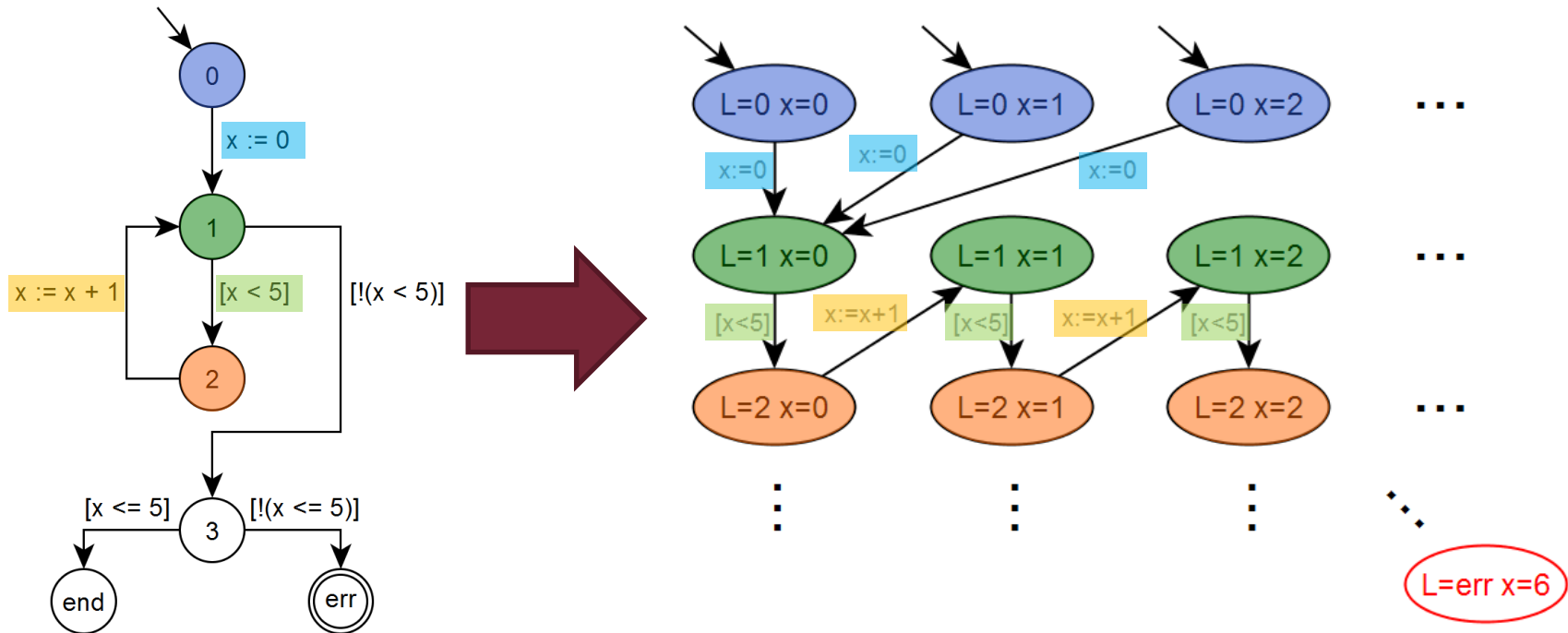
- $L = (l_0, l_1, \dots)$: set of control **locations** (PC)
- G : set of **edges** with **operations** over a set of **variables**
 - E.g., guard, assignment ...



- Typical property: “**error**” location (l_E) should not be reachable

Introduction – States and Transitions

- **State**: location + valuation of variables (L, x_1, x_2, \dots, x_n)
- **Transition**: operations
- **Problem**: **state space explosion** caused by data variables
 - E.g., 10 locations and 2 integers: $10 \cdot 2^{32} \cdot 2^{32}$ possible states
- **Goal**: **reduce** the state space representation **by abstraction**



Introduction – Mathematical Logic

■ Propositional logic (PL)

- Boolean variables and operators
- SAT problem: is the formula satisfiable
 - Example: bounded model checking
- Expressive power sometimes not enough

$$\neg p \wedge (p \vee q)$$

■ First order logic (FOL)

- Functions, predicates, quantifiers
- Not decidable in general

$$\forall x, y \exists z: p(f(x, y), g(z))$$

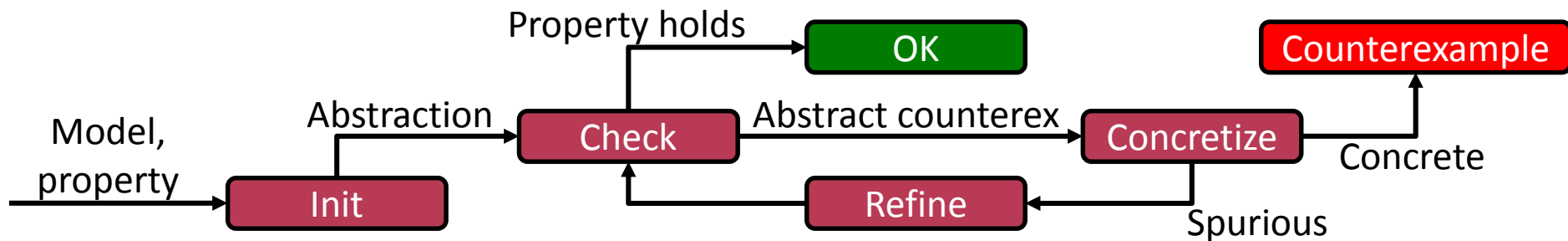
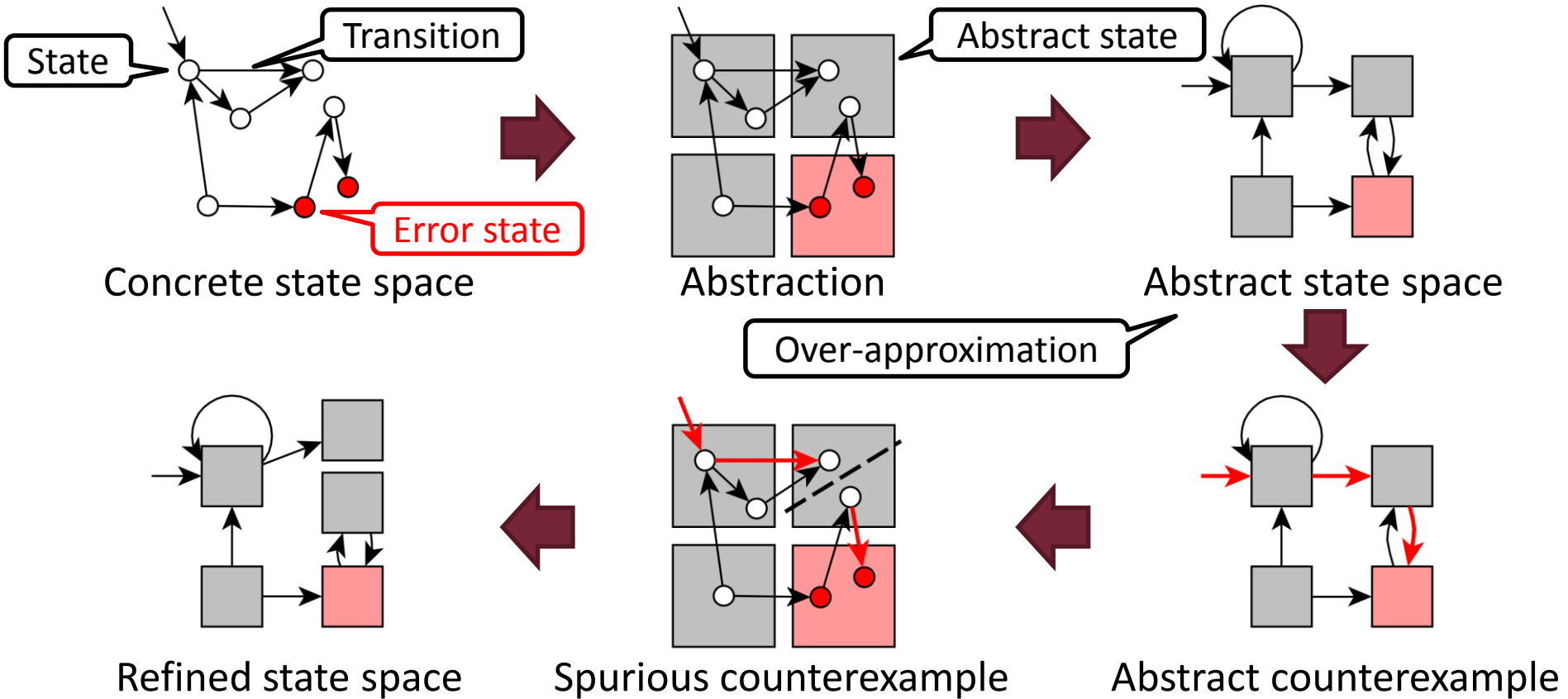
■ Satisfiability Modulo Theories (SMT)

- FOL formulas
- Interpreted symbols, decidable fragments
 - E.g., integer arithmetic

$$(x \leq y + 1) \wedge (y \geq 3)$$

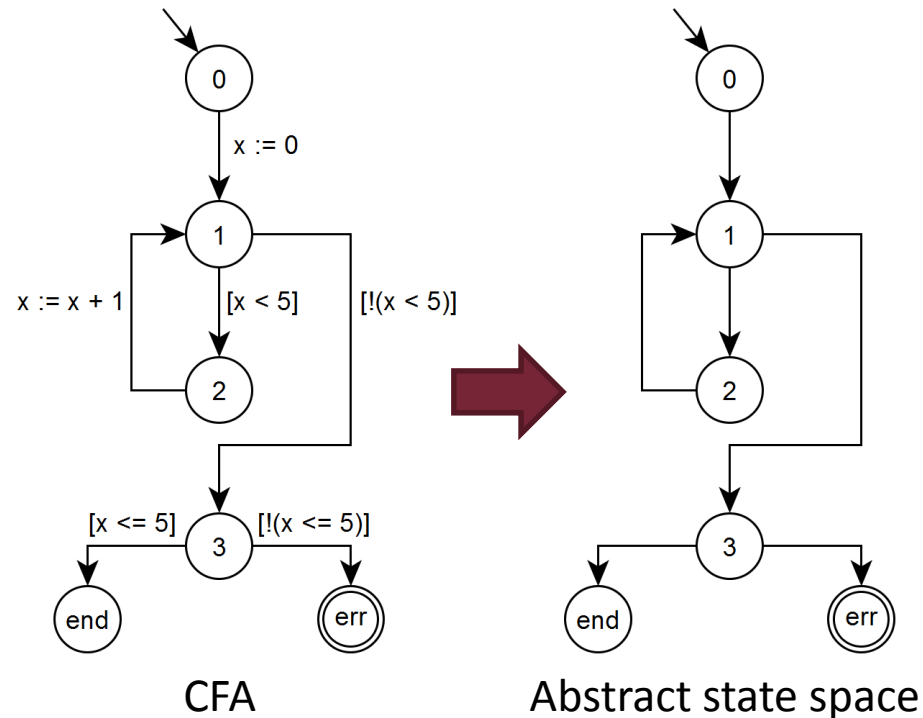
COUNTEREXAMPLE-GUIDED ABSTRACTION REFINEMENT (CEGAR)

CEGAR – Introduction



Abstraction – Introduction

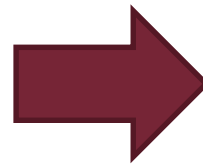
- **Abstraction**
 - General mathematical concept
 - Goal: hide details
 - Result: easier problem
- **Example**
 - Location abstraction
 - $(l, x_1, x_2, \dots, x_n) \rightarrow (l)$
 - Usually not enough alone
 - Error location trivially reachable
 - Extension with **predicate abstraction**



Predicate Abstraction

- Predicate abstraction
 - Keep track of **predicates instead of concrete values** for variables
 - Abstract state: concrete states corresponding to the same location, satisfying the **same predicates**
- Performing abstraction
 - Enumerate and join concrete states
 - State space explosion ☹️
 - 3x3 concrete states in the example → 5 abstract states

Variables:
 $x, y; D_x = D_y = \{0,1,2\}$
Predicates:
 $(x = y), (x < y), (y = 2)$



$y \backslash x$	0	1	2
0	$(x = y)$		
1	$(x < y)$	$(x = y)$	
2	$(x < y)$ $(y = 2)$	$(x < y)$ $(y = 2)$	$(x = y)$ $(y = 2)$

Predicate Abstraction

- Performing abstraction (differently)
 - Enumerate **abstract states only**: which one is feasible?
 - Predicate set $P \rightarrow |L| \cdot 2^{|P|}$ possible abstract states

- Example

- 3 predicates \rightarrow 8 possible abstract states (for each location)
- Some of them are not feasible
 - Use SMT solver to filter
 - E.g. $(x = y) \wedge (x < y) \wedge \neg(y = 2)$ cannot hold at the same time

	$x = y$	$x < y$	$y = 2$
1	X	X	X
2	X	X	✓
3	X	✓	X
4	X	✓	✓
5	✓	X	X
6	✓	X	✓
7	✓	✓	X
8	✓	✓	✓

Predicate Abstraction

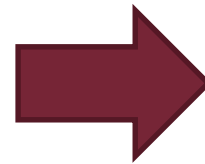
■ Abstract states with Boolean variables

- Concrete Abstract
- $(l, x_1, \dots, x_n) \rightarrow (l, b_1, \dots, b_m)$
- b_i : Boolean variable: i th predicate holds or not
- Notation: $p(b_i) = \begin{cases} p_i & \text{if } b_i \text{ is true} \\ \neg p_i & \text{otherwise} \end{cases}$

■ Example

Variables:
 $x, y; D_x = D_y = \{0,1,2\}$

Predicates:
 $(x = y), (x < y), (y = 2)$



$l \ x \ y$
↓ ↓ ↓
 $(0,0,0) \rightarrow (0, T, F, F)$
 $(6,1,2) \rightarrow (6, F, T, T)$
 ↑ ↑ ↑ ↑
 $l \ (x = y) \ (x < y) \ (y = 2)$

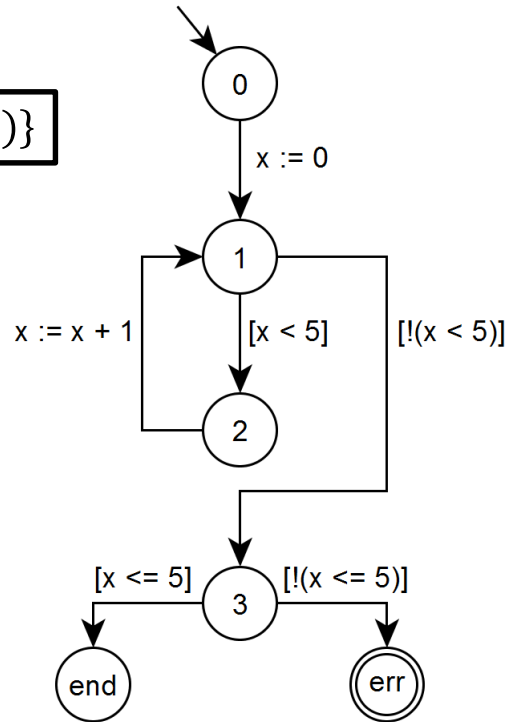
Predicate Abstraction

- Abstract initial states, error states
 - Abstract **initial** state: (l, b_1, \dots, b_m) , where $l = l_0$
 - Abstract **error** state: (l, b_1, \dots, b_m) , where $l = l_E$
- Abstract transitions
 - Abstract **transition**: at **least one concrete** transition exists between contained concrete states (**existential** property of the abstraction)
 - Calculate with SMT solver (without enumerating concrete states)
 - For (l, b_1, \dots, b_m) and (l', b'_1, \dots, b'_m) :
 - $\exists op: (l, op, l') \in G$, i.e. there is an edge with operation op between locations in the CFA, and
 - $p(b_1) \wedge \dots \wedge p(b_m) \wedge op \wedge p(b'_1) \wedge \dots \wedge p(b'_m)$ is satisfiable

Predicate Abstraction

- Example

$$P = \{(x \leq 5)\}$$



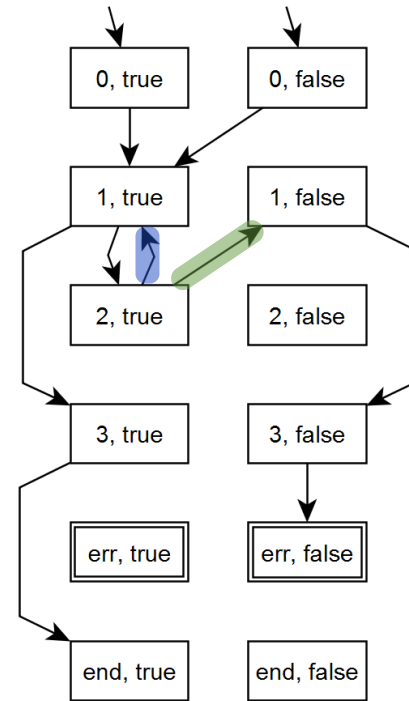
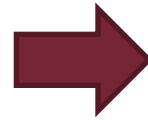
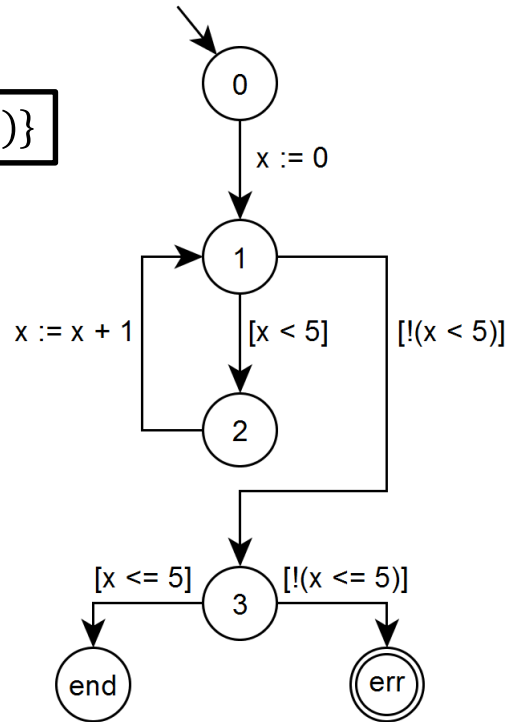
0, true	0, false
1, true	1, false
2, true	2, false
3, true	3, false
err, true	err, false
end, true	end, false

- 6 locations, 1 predicate \rightarrow 12 abstract states

Predicate Abstraction

Example

$$P = \{(x \leq 5)\}$$



Transition examples

○ $(2, \text{true}) \rightarrow (1, \text{true})$

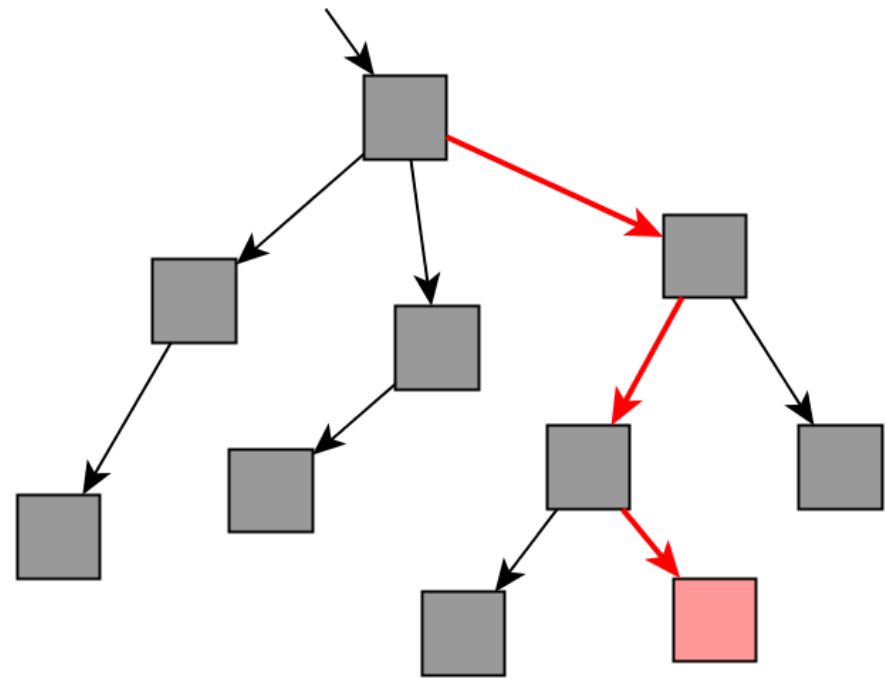
- $(2, x := x + 1, 1) \in G$ and $(x \leq 5) \wedge (x' = x + 1) \wedge (x' \leq 5)$ is satisfiable: $x = 0, x' = 1$

○ $(2, \text{true}) \rightarrow (1, \text{false})$

- $(2, x := x + 1, 1) \in G$ and $(x \leq 5) \wedge (x' = x + 1) \wedge \neg(x' \leq 5)$ is satisfiable: $x = 5, x' = 6$

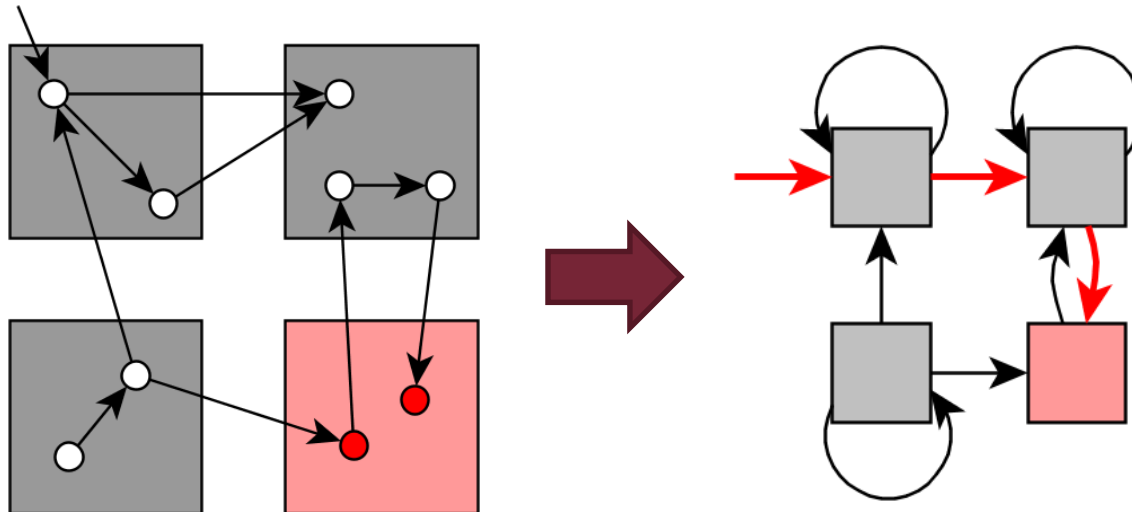
Model Checking

- **Traverse** abstract state space
 - With some **search strategy**, e.g., DFS, BFS
 - Search for error state
- **Optimizations**
 - **On-the-fly**
 - Calculate abstract states during the search
 - **Incremental**
 - Do not explore unchanged parts after refinement



Model Checking

- **Properties** of existential abstraction
 - **Over-approximates** the original model
 - There is a corresponding abstract path for each concrete path
 - If **no** abstract path exists to error state: concrete **does not exist** either
 - If abstract path **exists** to error state: concrete path **may exist**
 - Therefore, **abstract counterexamples** must be checked
 - Does it have a corresponding concrete path?

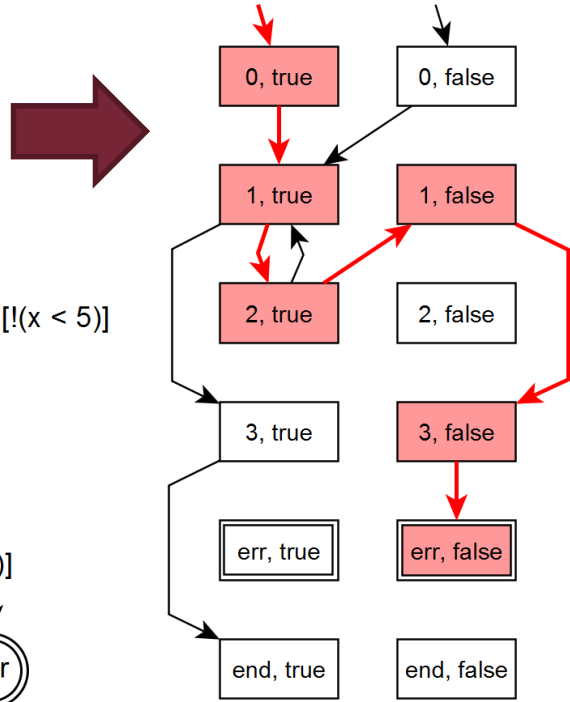
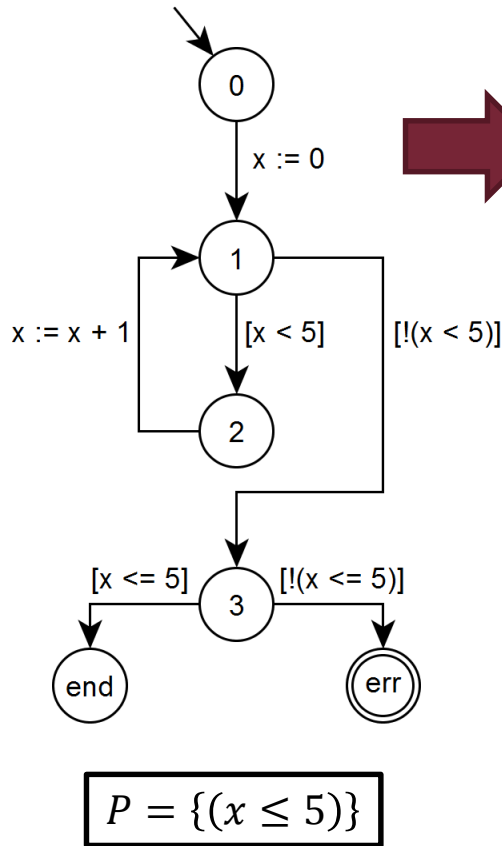


Abstract Counterexample

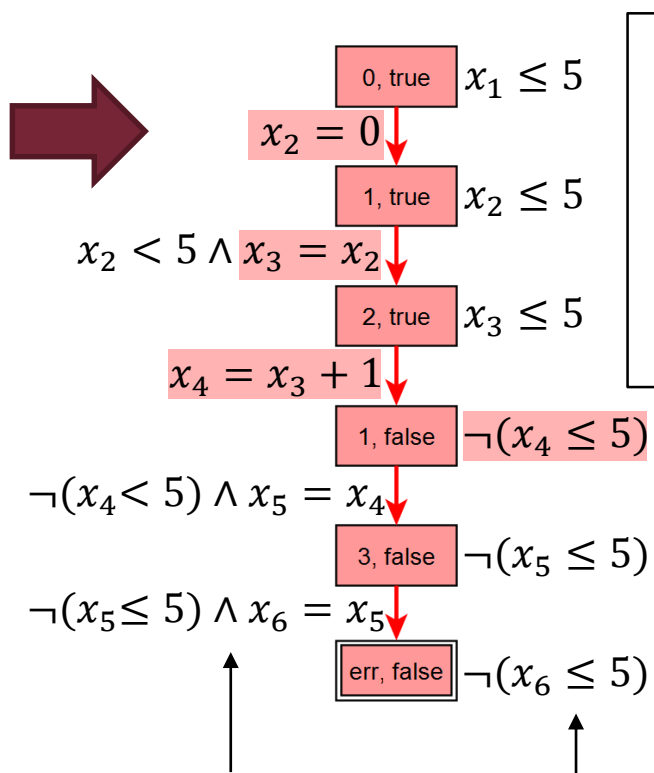
- Form of abstract counterexample
 - Sequence of **locations and predicates**
 - $(l_1, b_{1,1}, \dots, b_{1,m}), (l_2, b_{2,1}, \dots, b_{2,m}), \dots, (l_n, b_{n,1}, \dots, b_{n,m})$
- Finding a **concrete path** \rightarrow traverse a part of the concrete state space
 - Guided by abstract counterexample (what should be explored)
 - SMT solver can be used
 - Similarly to bounded model checking (BMC)
 - Generalize the method presented at existential abstraction for n steps
- Concrete path **exists** \rightarrow concrete model is **faulty**
- Concrete path **does not exist** \rightarrow **spurious** counterexample

Abstract Counterexample

Example



Abstract counterexample (6 states)



Operations on transitions

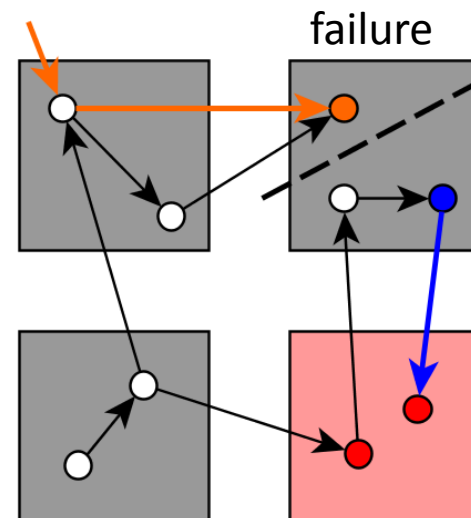
Predicates of states

$(x_1 = 3)$
 $(x_2 = 0)$
 $(x_3 = 0)$
 $(x_4 = ?)$

Not satisfiable

Spurious Counterexample

- “Failure” state: A concrete path exists until a state and after, but these are *separate* in the concrete model
- Group concrete states mapped to “failure” state
 - D = “Dead-end”: reachable
 - B = “Bad”: transition to next state
 - IR = “Irrelevant”: others
- Reason for spurious counterexample
 - Set of predicates does not distinguish D and B



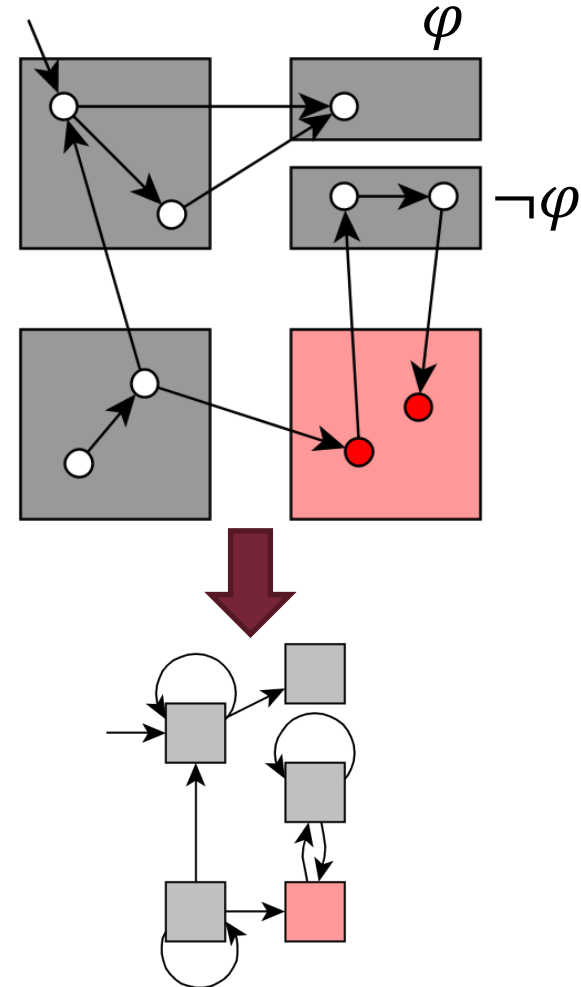
Abstraction Refinement

■ Eliminating the spurious counterexample

- More predicates (finer abstraction)
- Separate **D** and **B**
 - Without enumerating concrete states
 - Describe **D** and **B** with formulas
 - SMT solver can generate a formula φ that separates (holds for D but not for B)
 - This method is called *interpolation*
- The set $P \cup \{\varphi\}$ will **eliminate** this spurious counterexample
 - Moreover it is enough to split only the failure state (*lazy abstraction*)

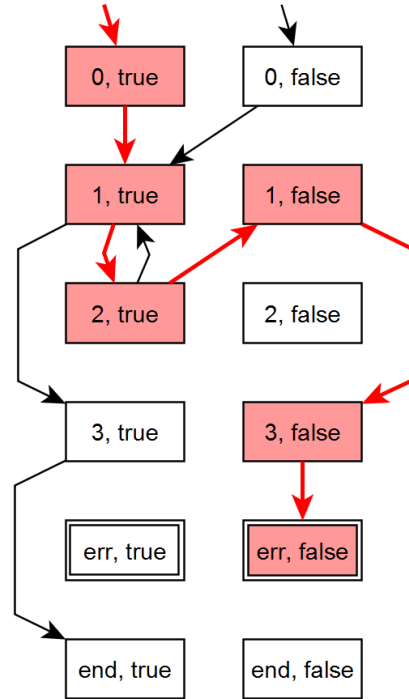
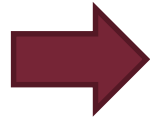
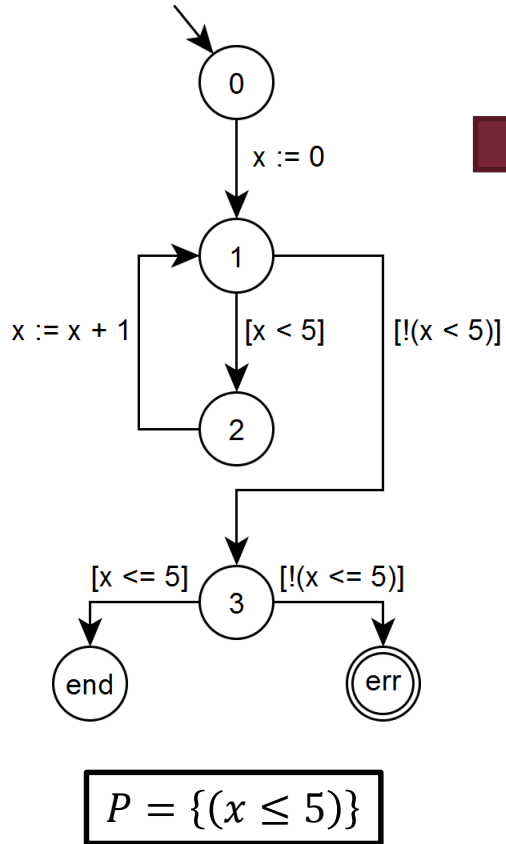
■ Additional spurious counterexamples

- More predicates

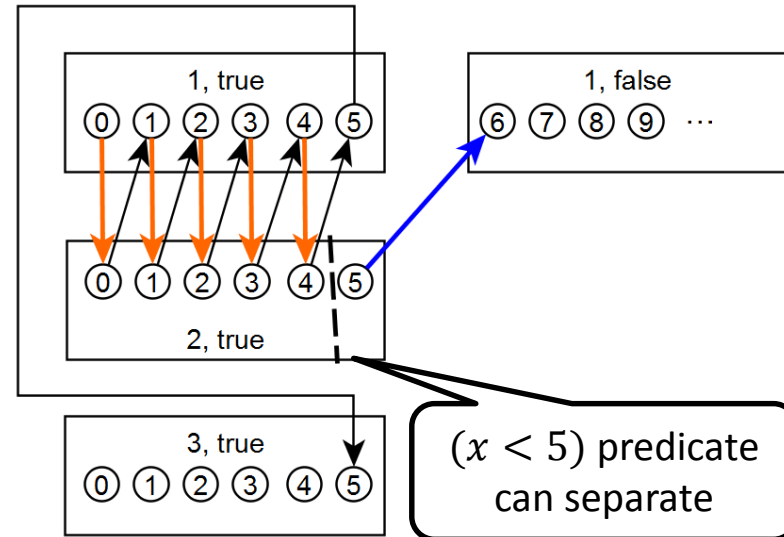


Abstraction Refinement

Example

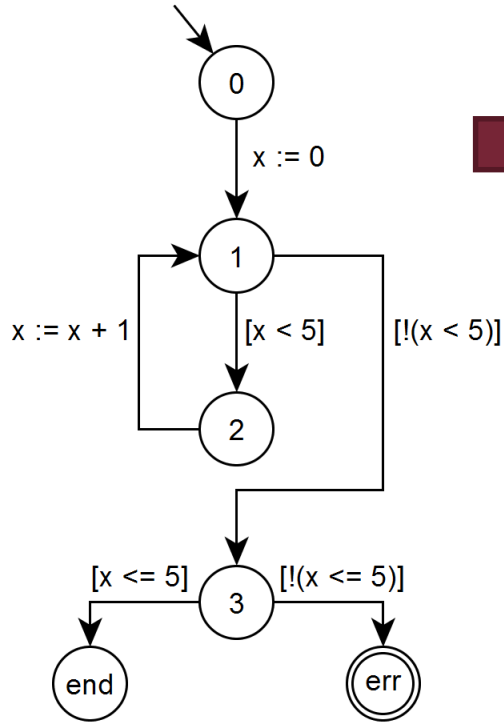


$(x_1 = 3)$
 $(x_2 = 0)$
 $(x_3 = 0)$
 $(x_4 = ?)$

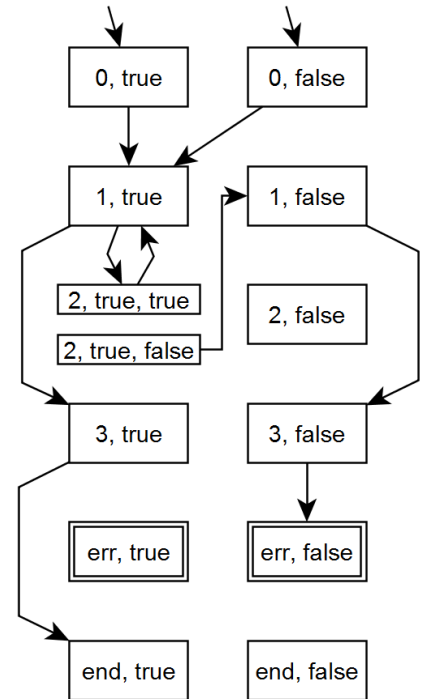
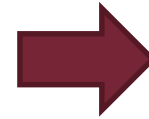
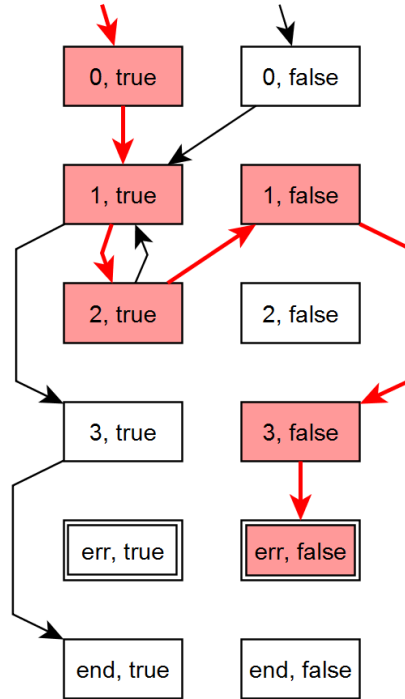
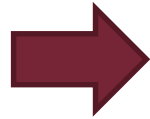


Abstraction Refinement

Example

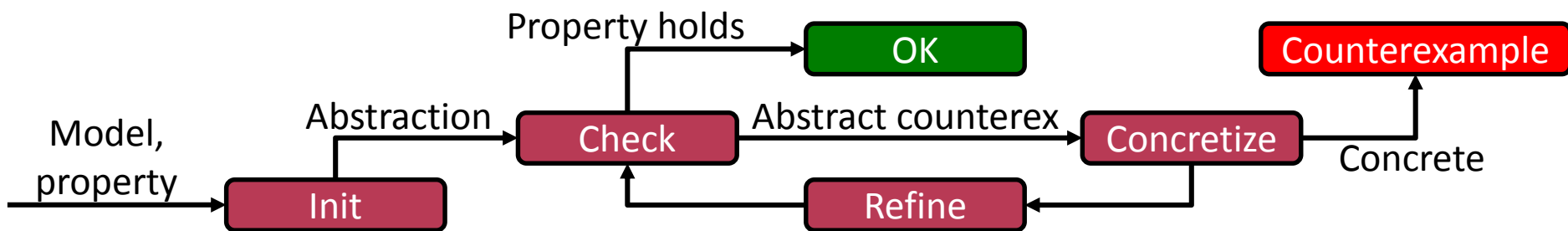
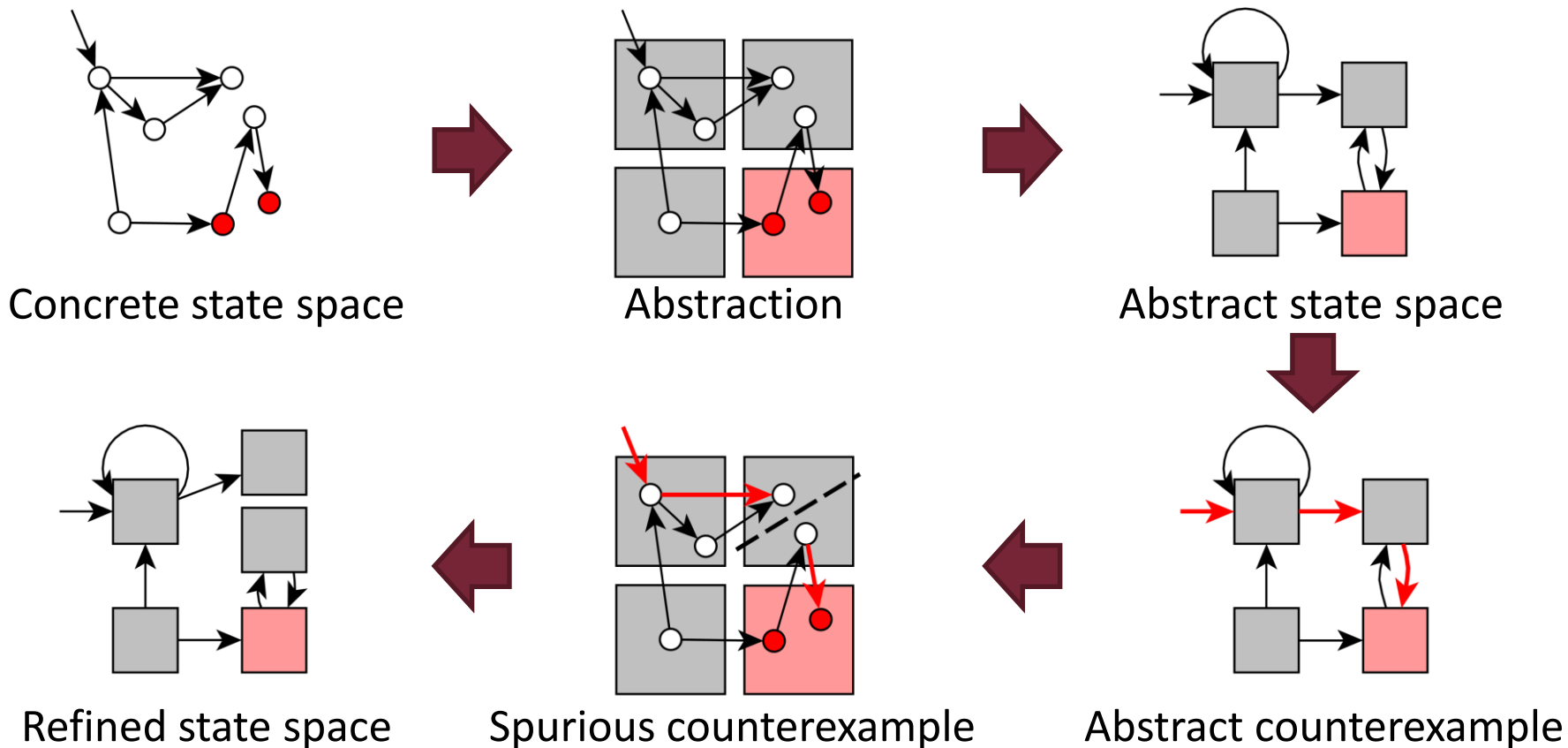


$$P = \{(x \leq 5)\}$$



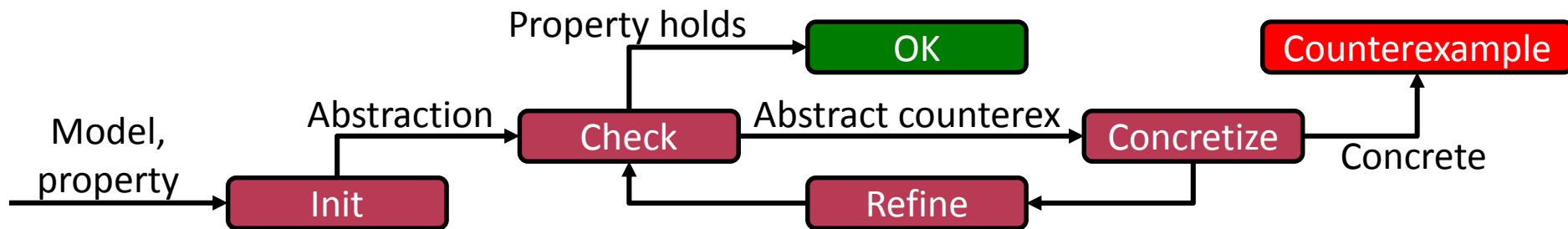
$$P = \{(x \leq 5), (x < 5)\}$$

CEGAR – Summary



The algorithm

- Counterexample-Guided Abstraction Refinement (CEGAR)
 - Automatic method
 - Each step is automatic
 - Deep knowledge of formal methods is not required
 - How about the **initial** set of **predicates**?
 - It can be an empty set (the algorithm will split states)
 - It can come from conditional statements in the software
 - Other heuristics



TOOLS

Tools

■ SLAM2

- Part of Static Driver Verifier Research Platform (SDVRP)
- Structure
 - Driver **C code**: analyzed component
 - Platform model: describe environment
 - Analysis: adherence to API usage rules
- Algorithms
 - Create Boolean program with **predicate abstraction**
 - Symbolic model checking: BEBOP tool
 - **CEGAR loop**
- research.microsoft.com/en-us/projects/slam/

Tools

■ BLAST

- Berkeley Lazy Abstraction Software Verification Tool
- Input: **C program** + requirement (BLAST Query Language)
- **Predicate abstraction**
 - Building abstract reachability tree (ART)
- Refinement: new predicate with interpolation
 - **Lazy abstraction**: apply new predicate locally
- Limitations: multiplication, bit operations, overflow
- mtc.epfl.ch/software-tools/blast/index-epfl.php

Tools

■ CPAchecker

- The Configurable Software-Verification Platform
- Input: **C program** + specification
 - Assertion, error label, deadlock, null dereference, ...
- Highly **configurable**
 - Different kinds of abstractions (not only predicate)
 - Can consider multiple prefixes of a counterexample
 - Chooses from different refinements (refinement strategy)
- cpachecker.sosy-lab.org/

Tools

■ Theta

- Generic, modular, configurable model checking framework
- Developed at BME-MIT
- **Generic**: various kinds of formal models
 - Transition systems, control flow automata, timed automata
- **Modular**: reusable and combinable modules
- **Configurable**: different algorithms and strategies
- github.com/FTSRG/theta

Tools

- **Competition** on Software Verification 2017 (SV-COMP)
 - sv-comp.sosy-lab.org/2017/
 - **32 tools, 8908 input tasks** (program + requirement)
 - Categories
 - Arrays (ArraysReach, ArraysMemSafety)
 - Bit Vectors (BitVectorsReach, Overflows)
 - Heap Data Structures (HeapReach, HeapMemSafety)
 - Floats
 - Integers and Control Flow (ControlFlow, Simple, ECA, Loops, Recursive, ProductLines, Sequentialized)
 - Termination
 - Concurrency
 - Software Systems (DeviceDriversLinux64, BusyBox)

SUMMARY

Summary

- Software model checking
 - Verification by “pushing a button”
 - Problem to be solved: state space explosion
 - Solution: **abstraction**
 - Location + predicates
 - Properties of existential abstraction
 - **CEGAR**: automatically obtain proper abstraction
 1. Initial abstraction
 2. Model checking
 3. Examining the counterexample
 4. Refining the abstraction
 - **Tools**