

Graph Abstraction & Model Generation Techniques

Oszkár Semeráth, Rebeka Farkas



Budapest University of Technology and Economics
Department of Measurement and Information Systems
ftsrg Research Group



Main topics of the course

Graph Abstraction Techniques

- Partial Modeling (MAVO)
- Shaping (Neighbourhood, TVLA)

Model generation

- Motivation & Use-Cases
- Requirements & Objectives: the CoREDiSc criteria
- Related approaches
 - Graph Solver
 - Solver-Based Approaches
 - Design-Space Exploration

Summary & Learning Outcomes

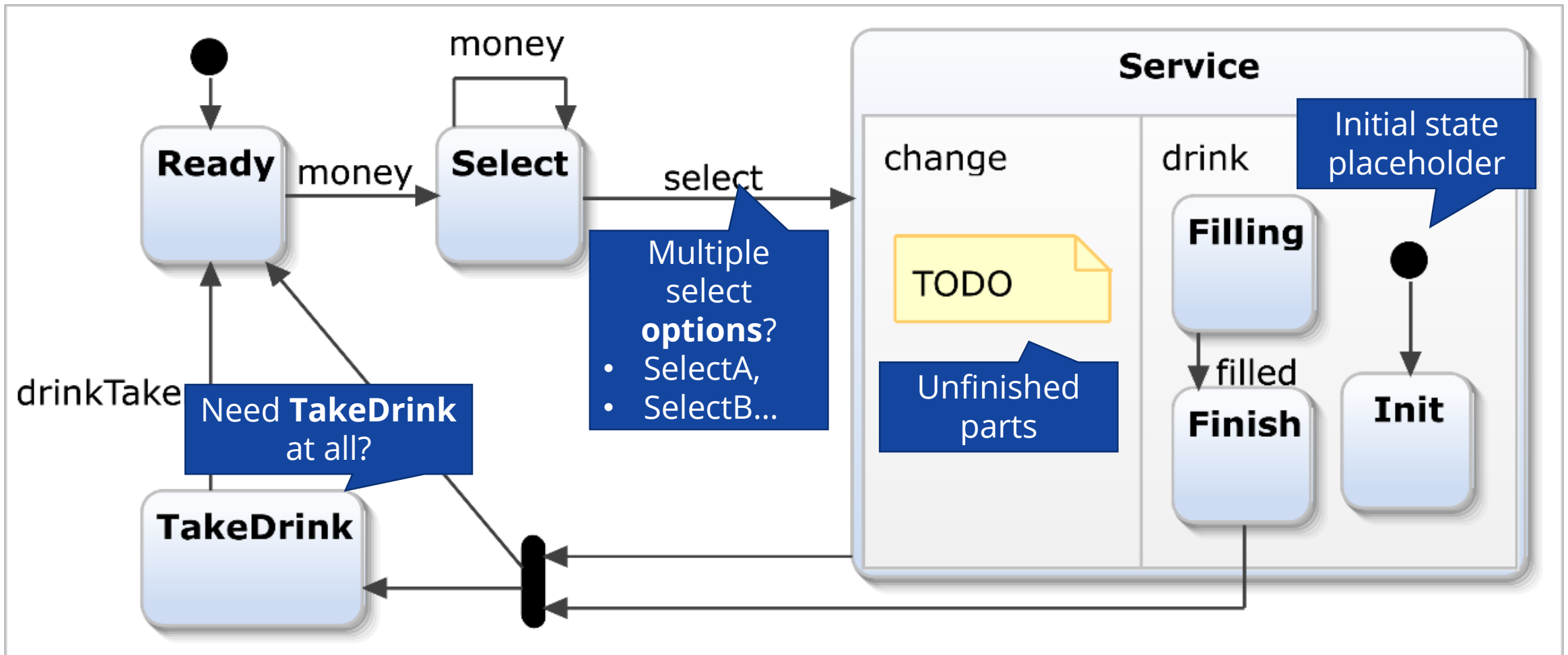
Graph Abstraction Techniques

Graph Abstraction

- **Previously:** concrete graph-based models
- **Motivation:** capture a range of potential models
 - Uniform handling of a range of graphs
 - Verification of graph-based systems
- Terminology:
 - *abstraction*: $graph \rightarrow abstractgraph$
 - Refinement between abstract graphs: $A_1 \sqsubseteq A_2$
 - Concretization of an abstract graph A is G if $abstraction(G) \sqsubseteq A$
- **Goal:** illustrate useful graph abstraction techniques

Partial Modeling

Example: Unfinished models



Motivation

- Early phase of development → high uncertainty in the models
- Editor forces the developer to work with complete models

Missing ⇔ Undecided / Uncertain / Unknown

Model refinement ⇔ Model rewriting

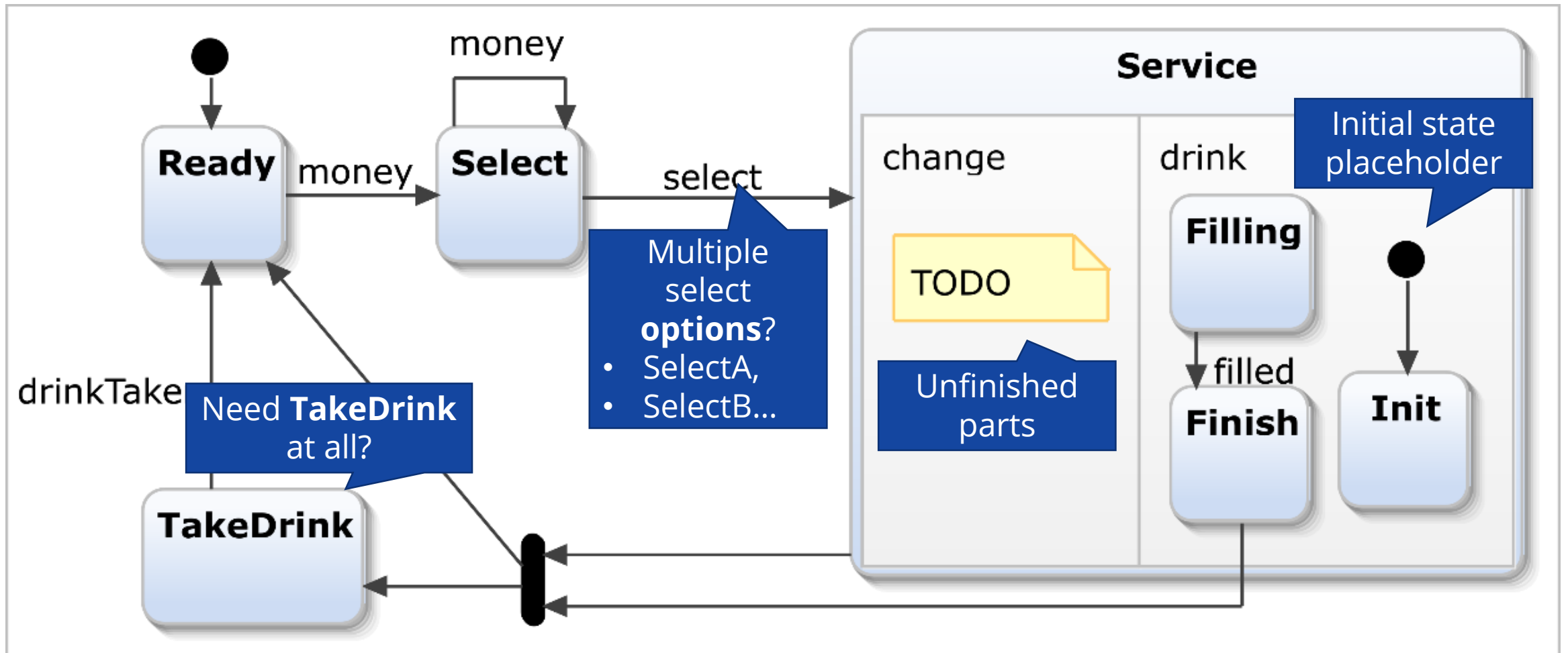
- **Issues:**
 - Forces the developer to make premature decisions
 - No way to list / document design alternatives
 - Editor mixes: invalid ⇔ unfinished
- **Clarify the semantics of missing elements**

Partial Modeling

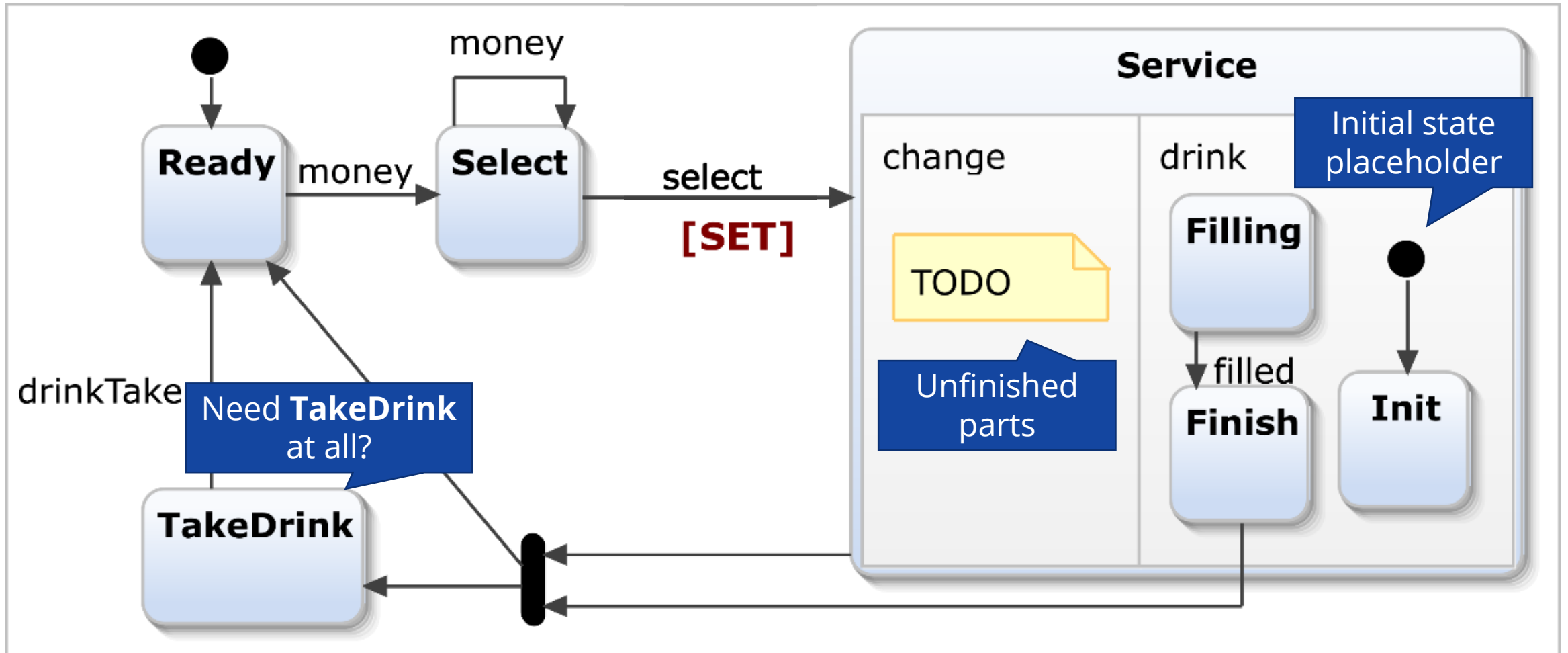
- Generic technique to explicitly represent uncertainty in models
 - Generic: works for every metamodel
 - Explicitly represent: uncertainty = model element
 - In Models: The uncertainty is attached to the models
- **MAVO**: practical way to annotate model with uncertainty
 - **M**ay: elements can be omitted
 - **A**bstract (Set): representing sets of elements
 - **V**ar: elements that can be merged
 - **O**pen: new elements can be added
- Automation: generate alternatives, check all alternatives

Michalis Famelis, Rick Salay, and Marsha Chechik. Partial models: towards modeling and reasoning with uncertainty. In: Proceedings of the 34th International Conference on Software Engineering, pp. 573–583. IEEE Press, 2012.

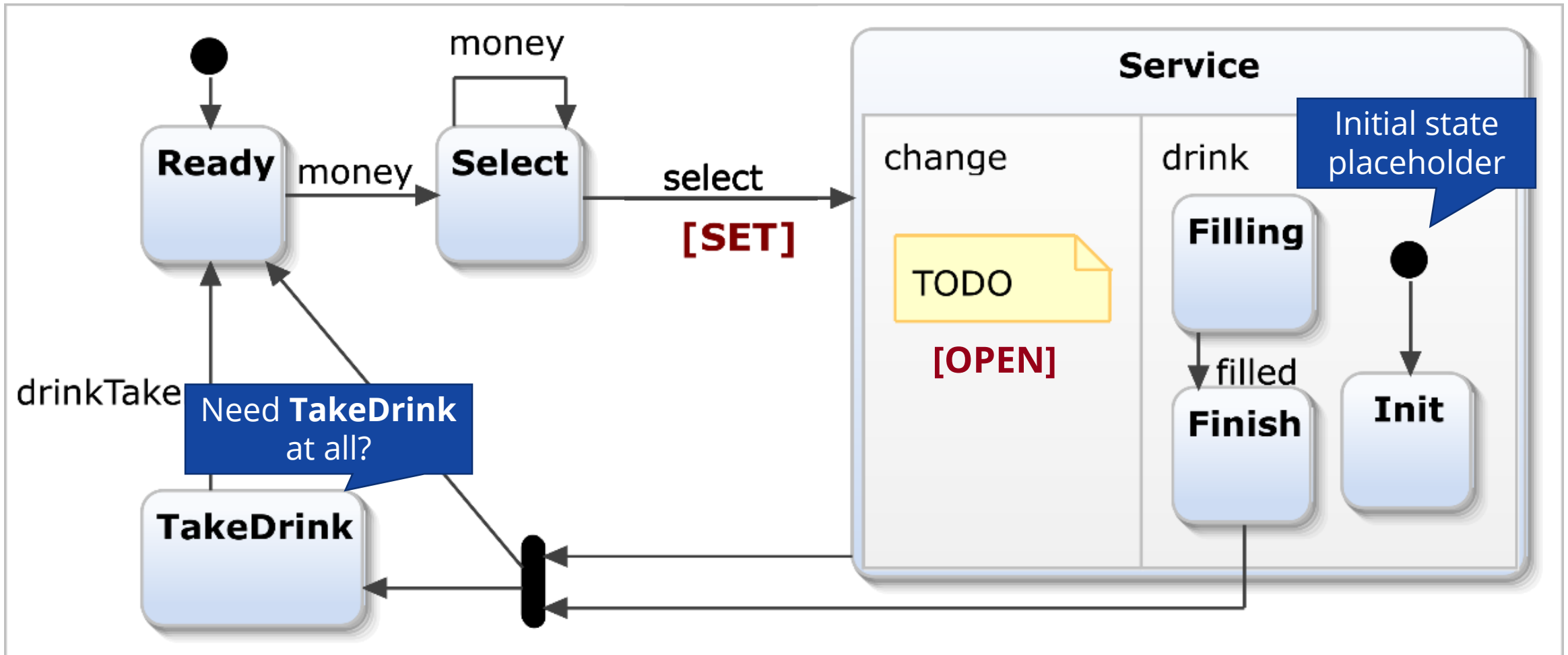
Example: Unfinished models with MAVO



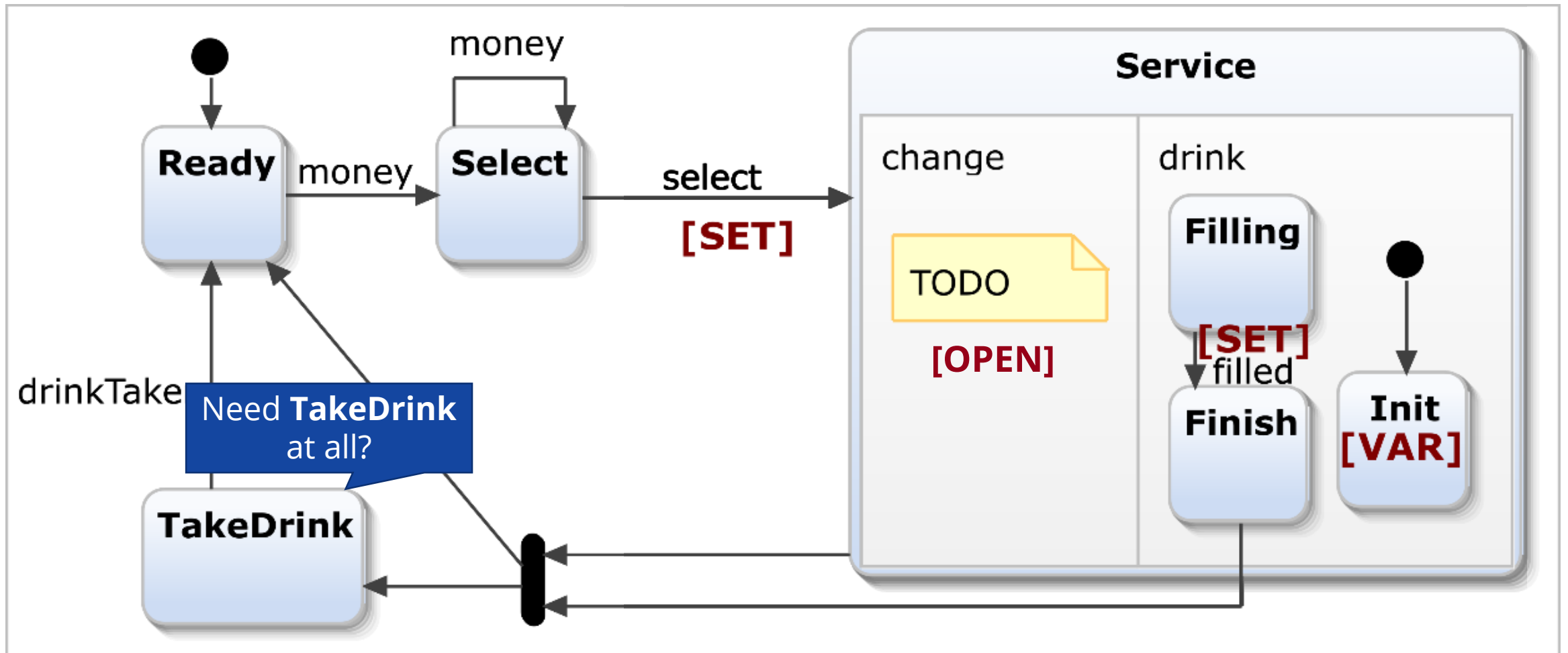
Example: Unfinished models with MAVO



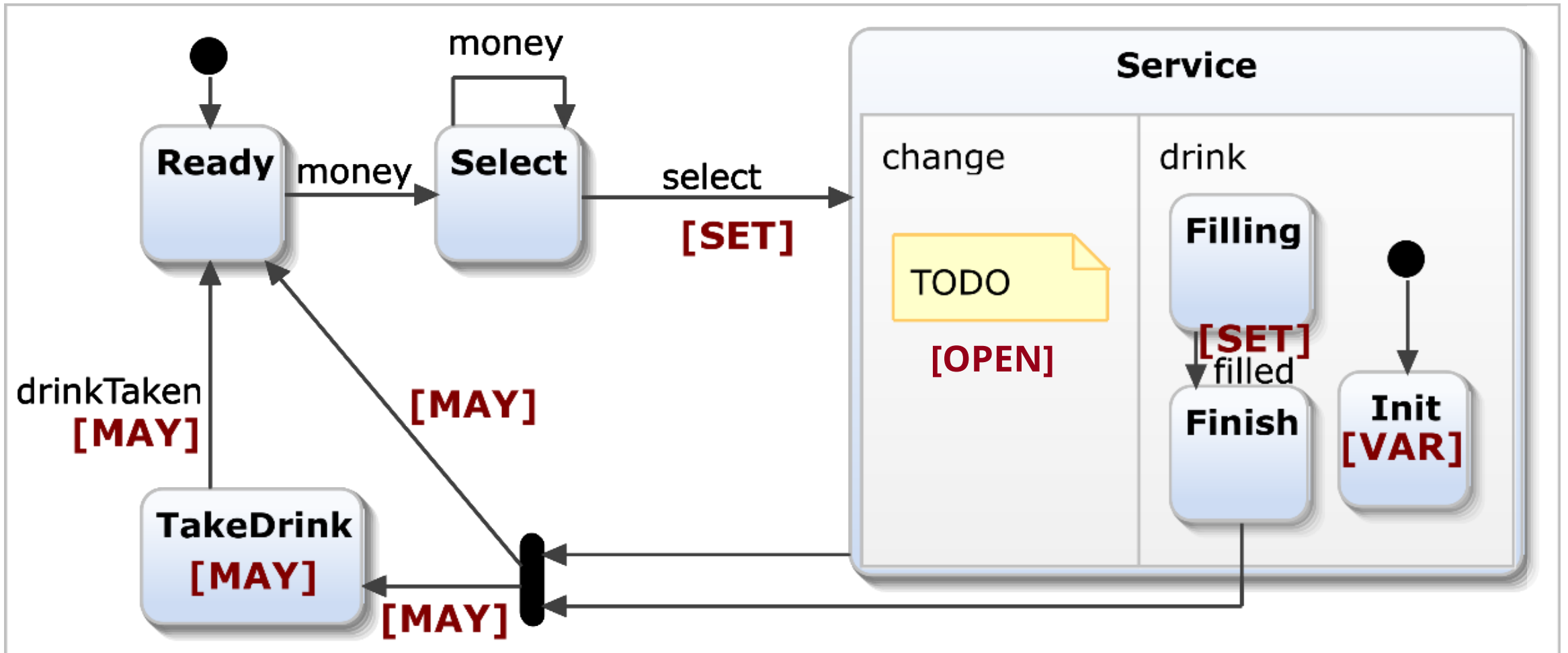
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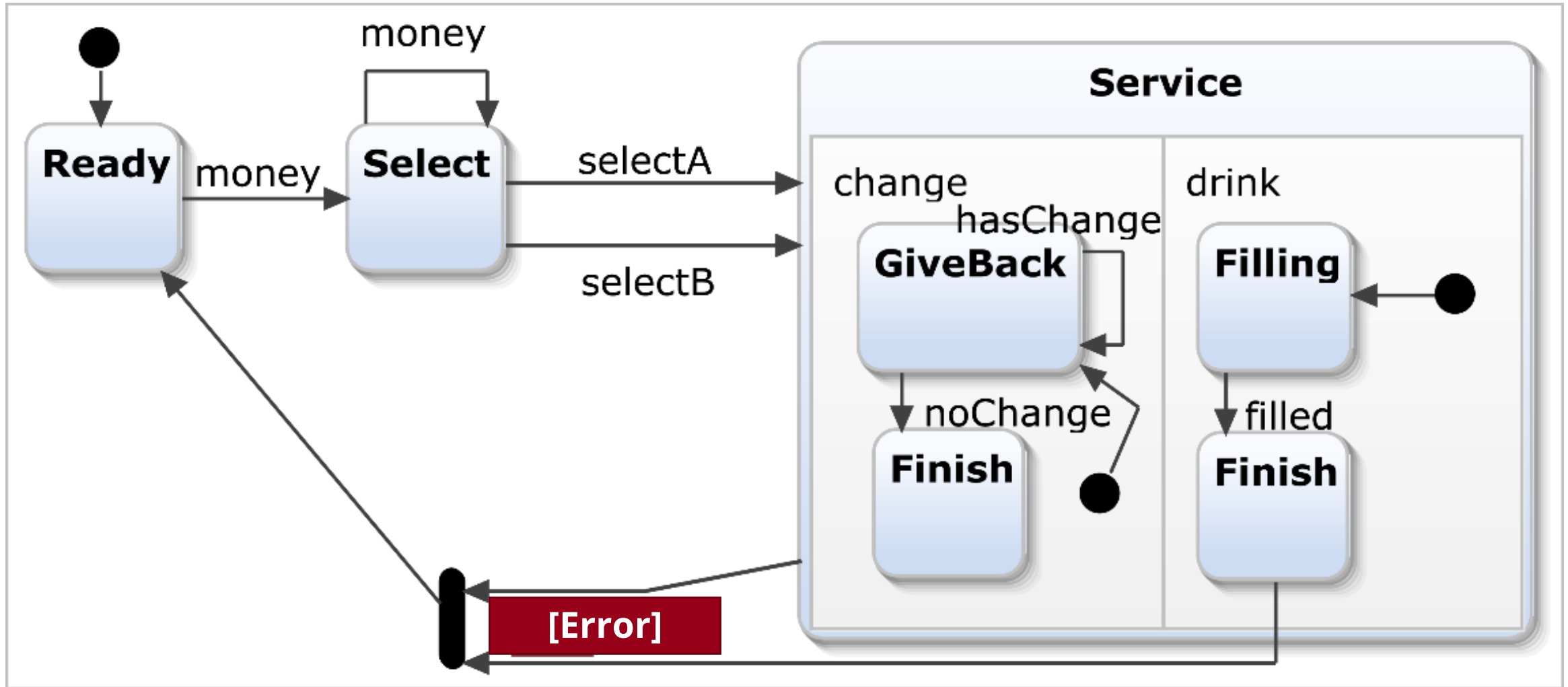
Example: Unfinished models with MAVO



Example: Unfinished models with MAVO



Example: Example concretization



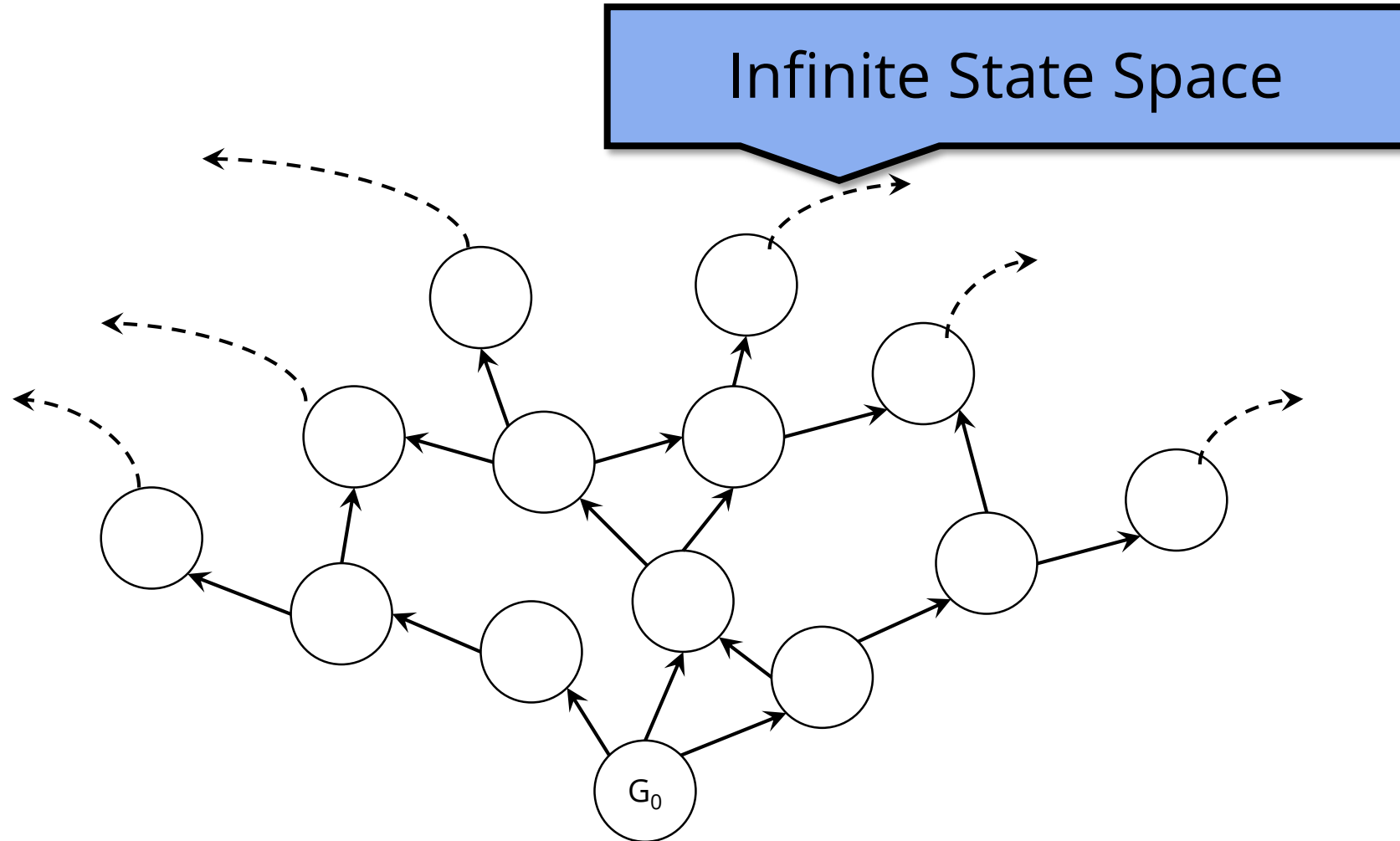
Partial Modeling Summary

- Partial modeling captures the uncertainty of models
- 1 partial model = set of complete model
- MAVO: framework for uncertainty annotation + tooling

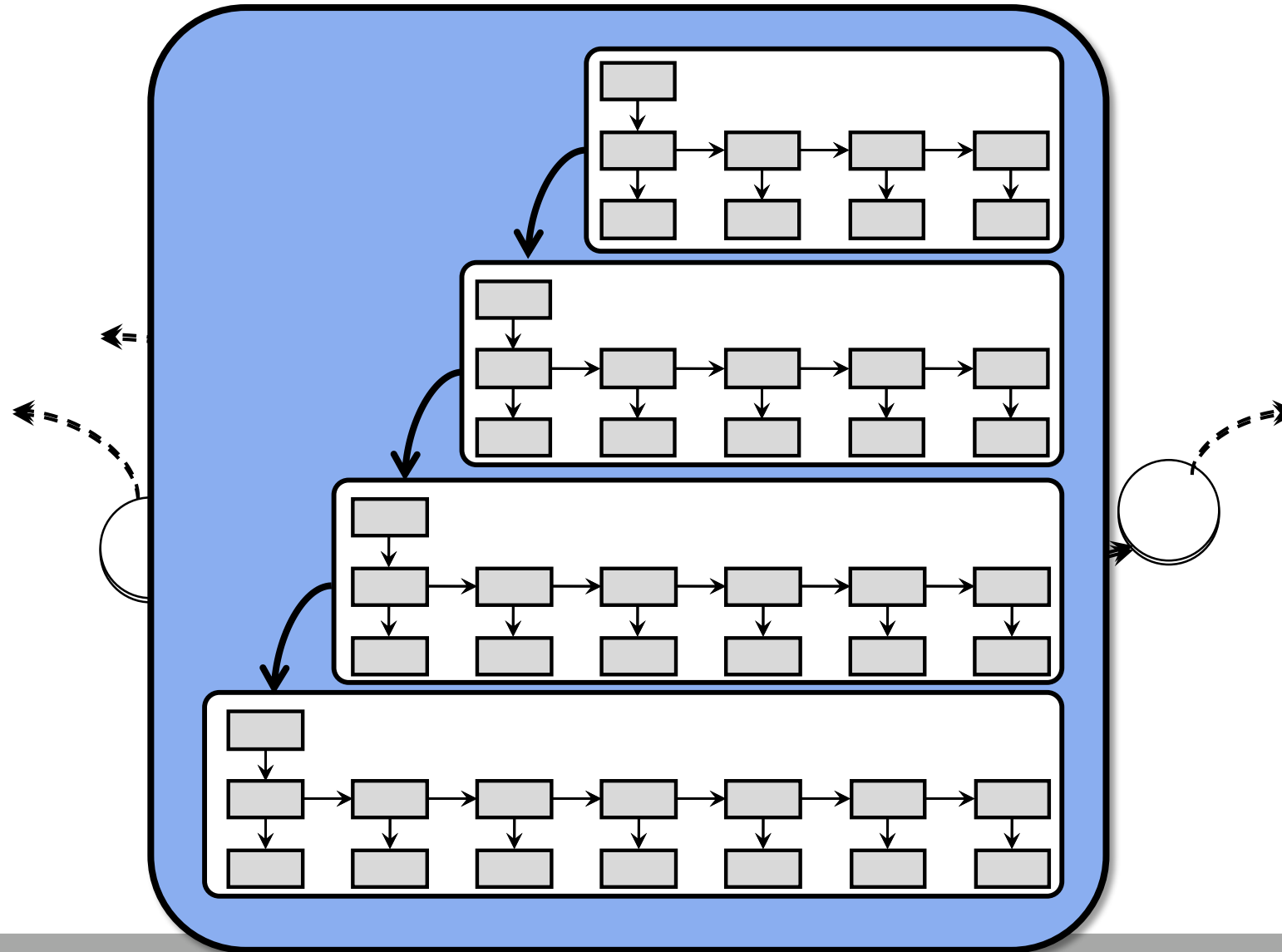
- Semantics of missing vs unfinished

Shaping Approaches

Motivation: Checking graph-based systems



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Shaping

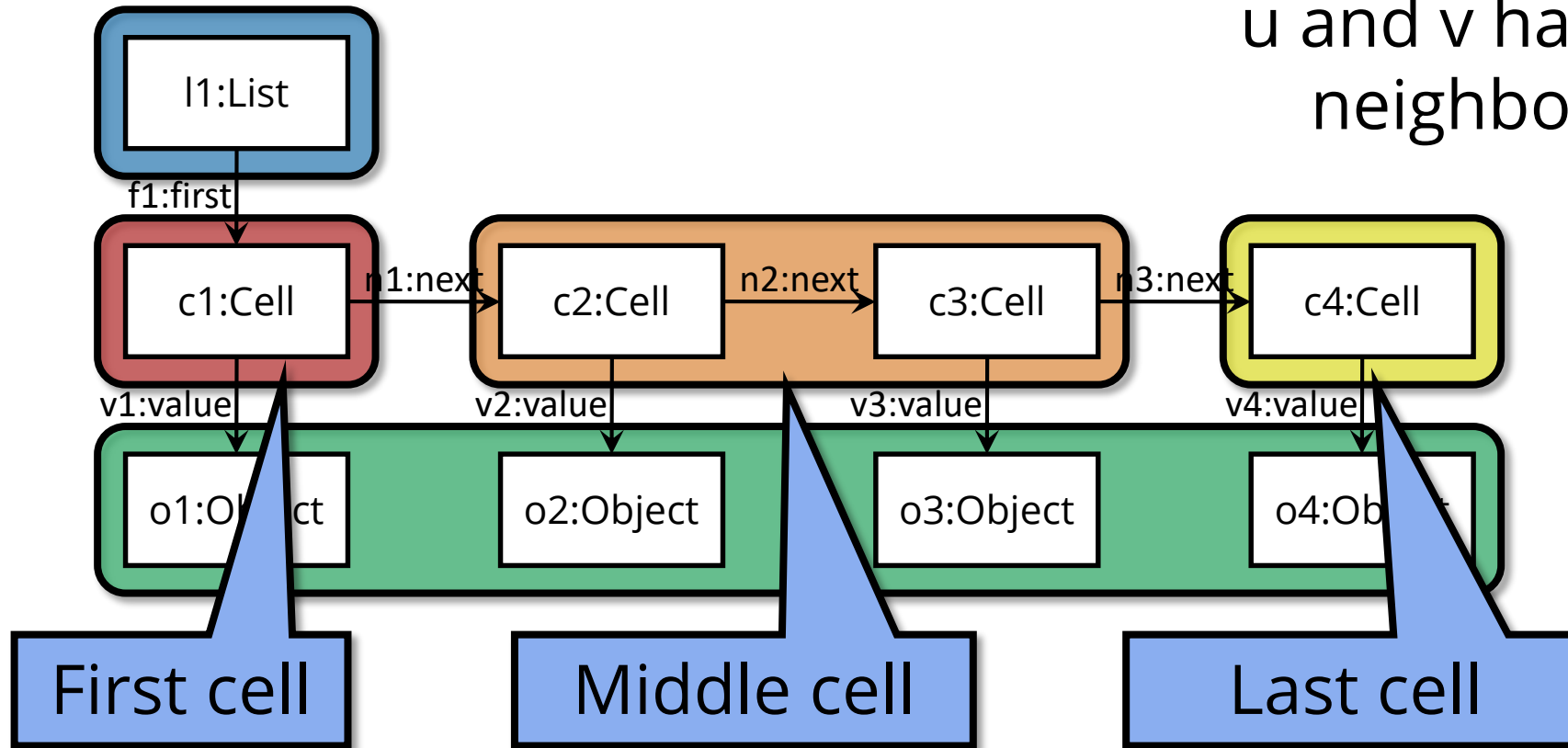
- **Goal:** Collect similar graphs together
- Similar graphs behave similarly

Neighborhood Equivalence:

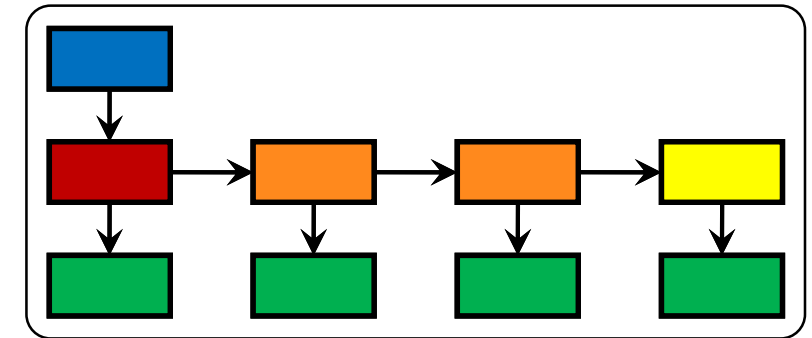
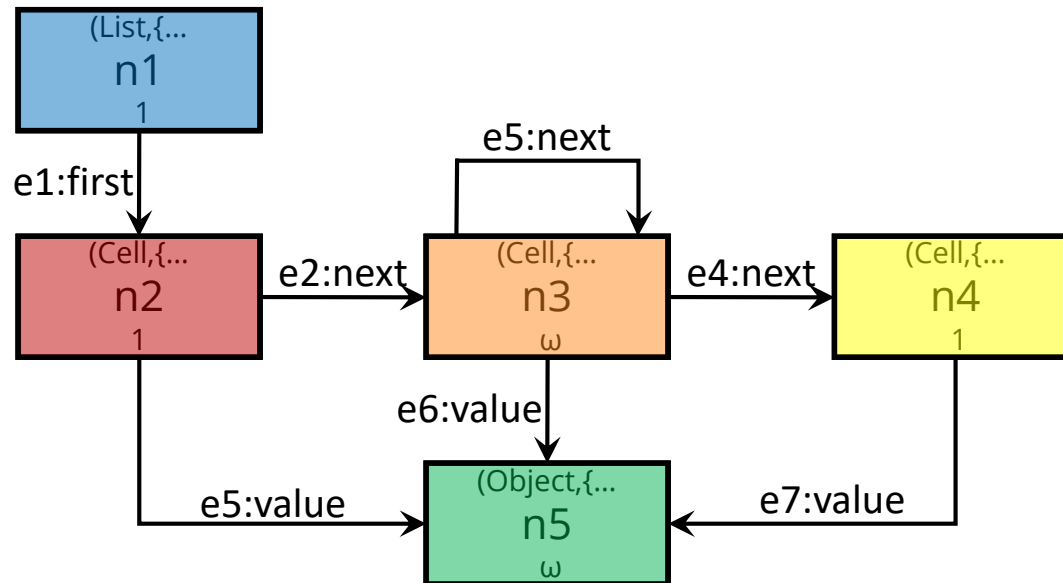
$u \sim v$

\leftrightarrow

u and v has similar neighborhood



Finite number of equivalence classes



Size = 4, 5, 6, ...
Same shape

Shaping summary

- Similar graphs collected together
- Uniform analysis of on the representation of similar graphs
- One of the few method to analyze infinite GT systems

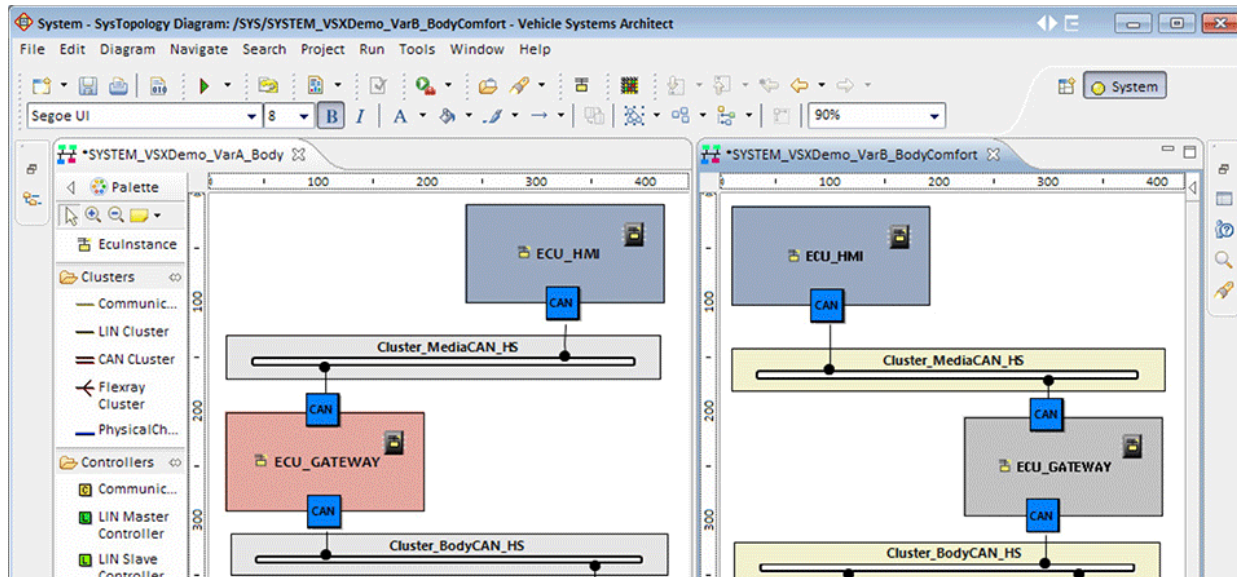
- Model \sqsubseteq Shape \sqsubseteq Metamodel

Model Generation

Motivation: Why to Generate Graph Models?

Tool Qualification

- Design of avionics / automotive systems
- Can you trust the tools?
- Safety standards (DO-178C) require systematic testing with guaranteed coverage



Source: <https://www.mentor.com/embedded-software/automotive/autosar>

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Validating Intelligent CPS Components

- AI Safety: How to check components driven by AI?
 - Treat AI component as black box
 - Generate test contexts
 - E.g. ICSE'18 paper from L. Briand's groups



<https://medium.com/self-driving-cars/beginners-guide-to-self-driving-vehicles-9e9003e790b8>

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Graph Database Benchmarks

- How to check that algorithms for graph DBs will behave well for real data?
- Real data has IP restrictions and never shown
- Real data is well-formed – random data is not



Source: <https://neo4j.com/blog/other-graph-database-technologies/>

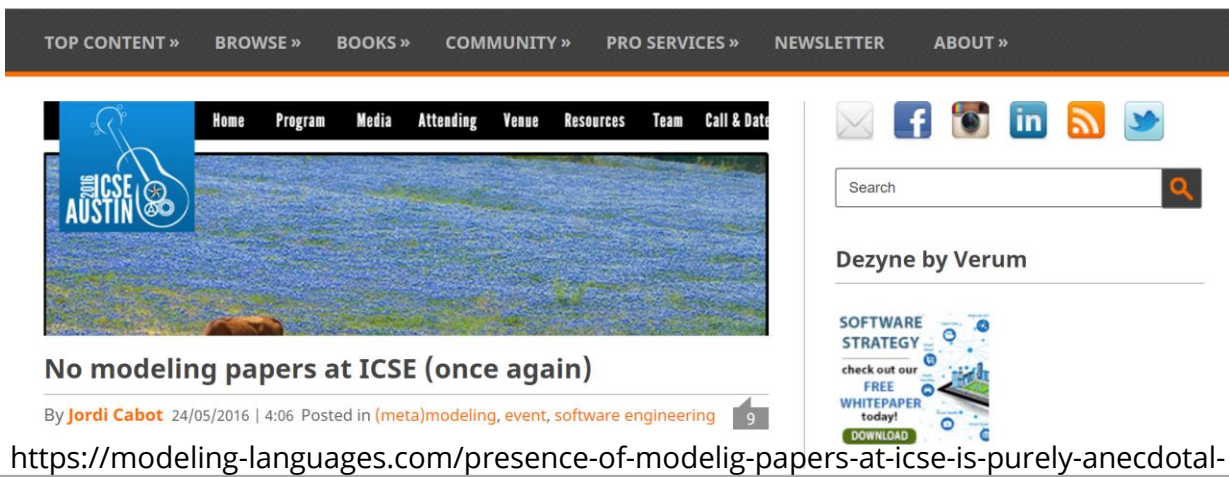
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Empirical Evaluation of Modeling Papers

- Real models are either confidential or too small
- Is your case study relevant & scalable?
- Existing generators are ad hoc and domain-specific

<https://modeling-languages.com/presence-of-modelig-papers-at-icse-is-purely-anecdotal-once-again/>

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Graph Model
Generator

Graph Database Benchmarks

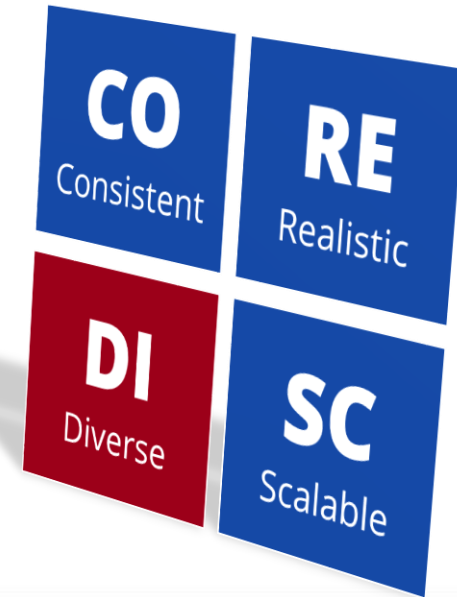
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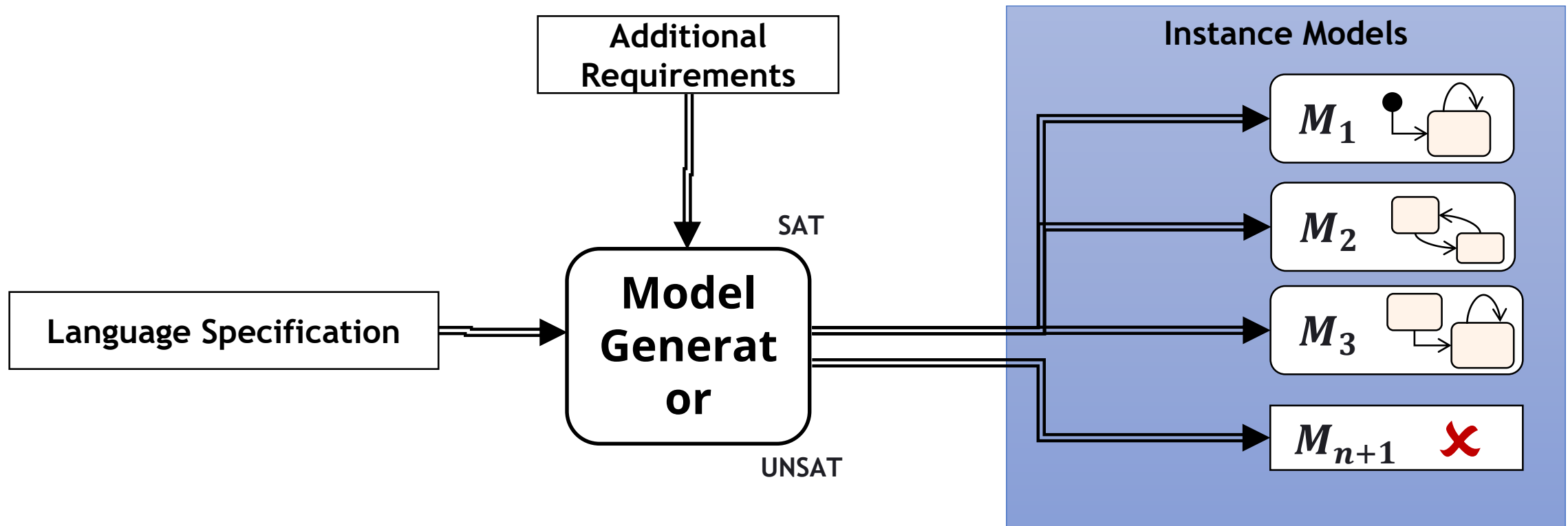
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Requirements & Objectives

the CoREDISc model

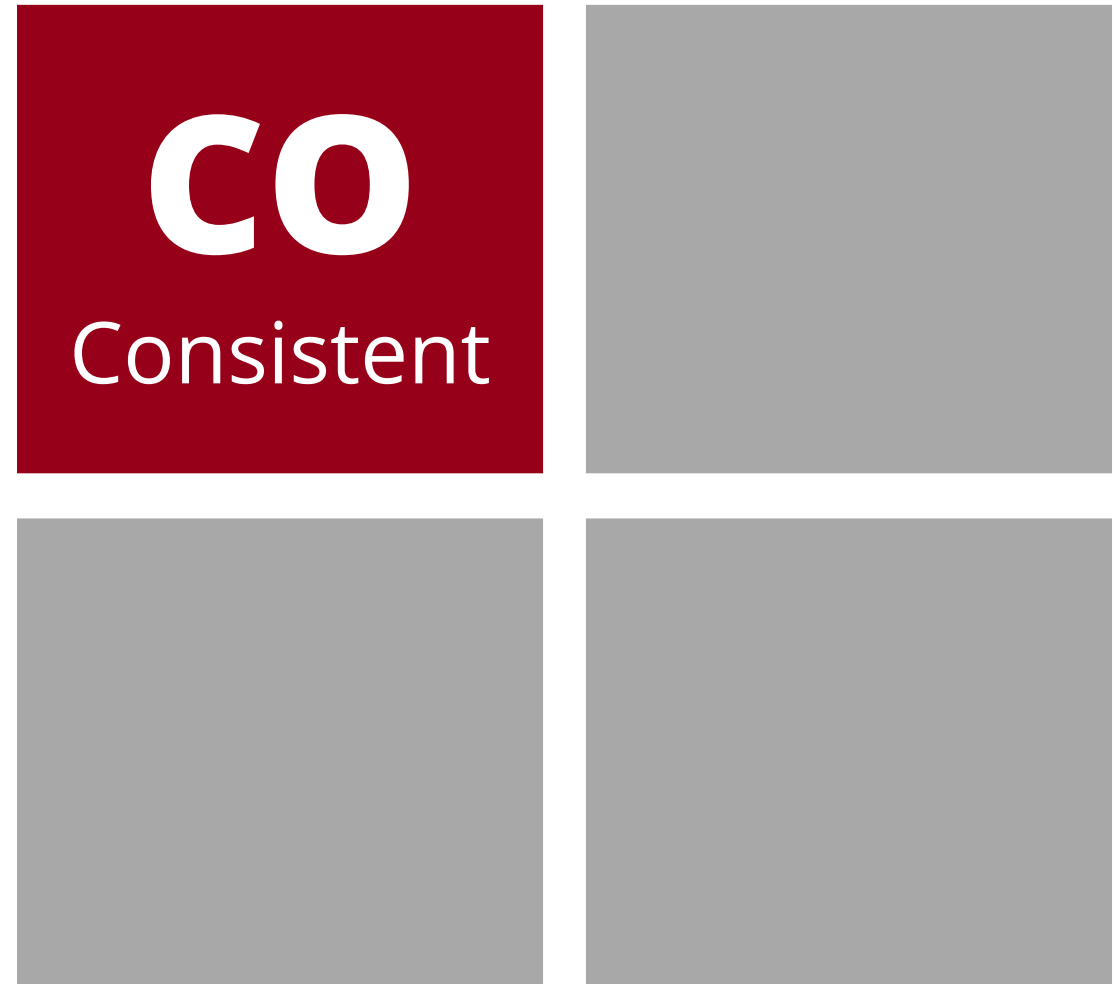


Setup of an ideal model generator



Properties of Model Generators: Consistent

- All (well-formedness) constraints are satisfied
- All (and only) consistent models are derived



Properties of Model Generators: Realistic

- Cannot be distinguished from a real model (By removing text+values and evaluating graph metrics)
- Set of generated models is close to real ones



Properties of Model Generators: Diverse

- Models are not symmetric
- The distance between any pairs of models is large

E.g. all equivalence classes are covered

CO
Consistent

RE
Realistic

DI
Diverse



Diversity as a requirement for testing

- Test case diversity
 - Test selection: similar test cases find similar errors
 - Test coverage: similar test cases cover the same code
- Methodologies
 - Equivalence partitioning, boundary-value analysis, etc.
 - Rely on *similarity, difference, distance*
 - Straightforward for simple structures, eg. Numbers
- What about models?

How to measure model **diversity**?

Diversity as a requirement for testing

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How to measure model **diversity**?

Properties of Model Generators: Scalable

- In size: ability to generate huge graphs
- In quantity: generation time of next model does not grow

CO

Consistent

RE

Realistic

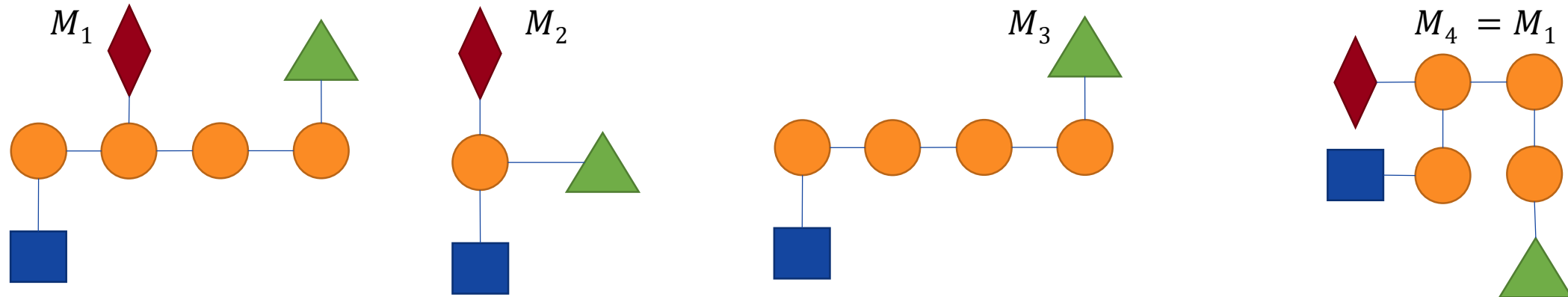
DI

Diverse

SC

Scalable

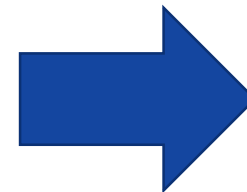
Model similarity and diversity



Which of these graphs...

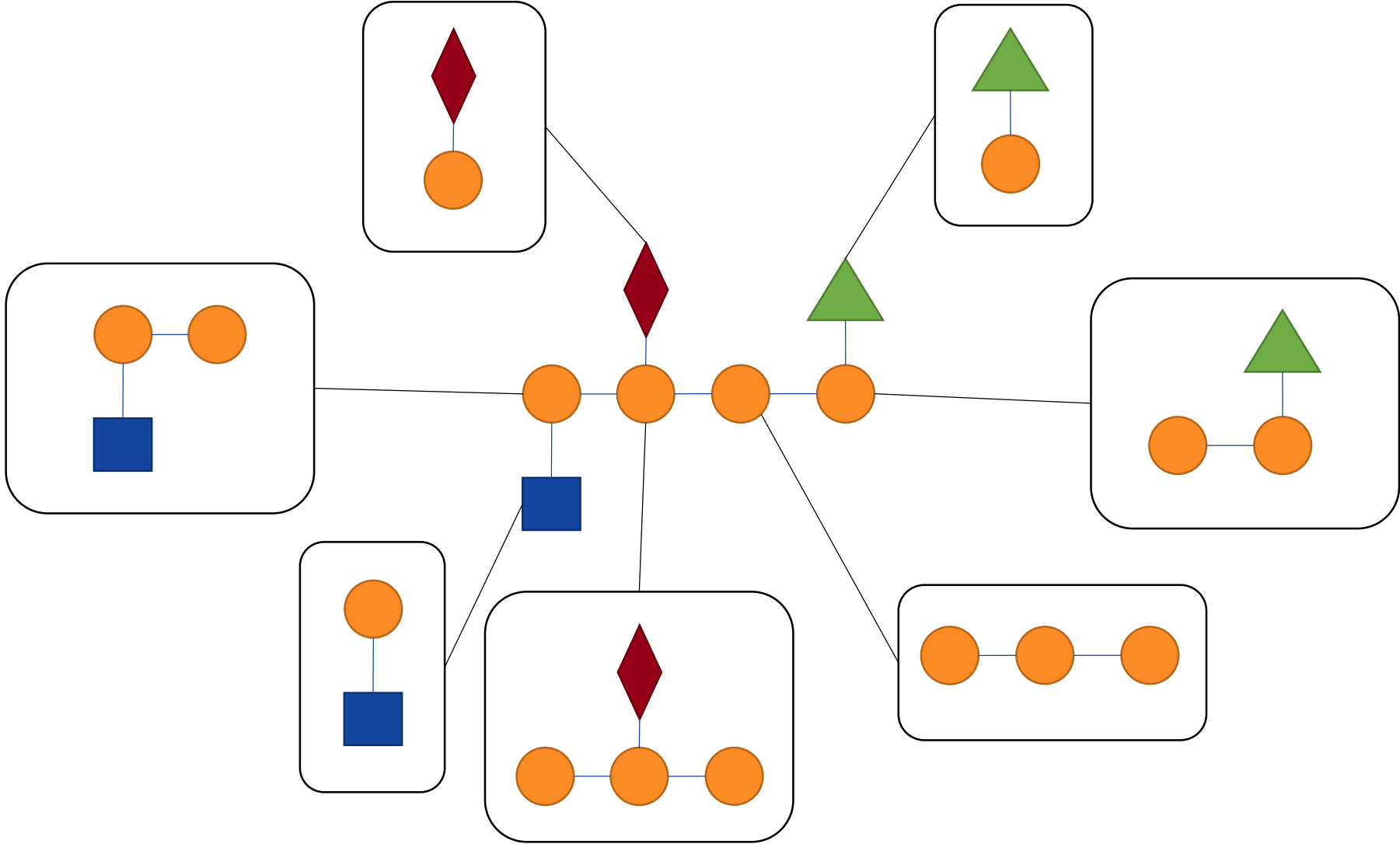
- ...are similar?
- ...are equivalent?
- ...should be selected as test cases?

How to automate the process?

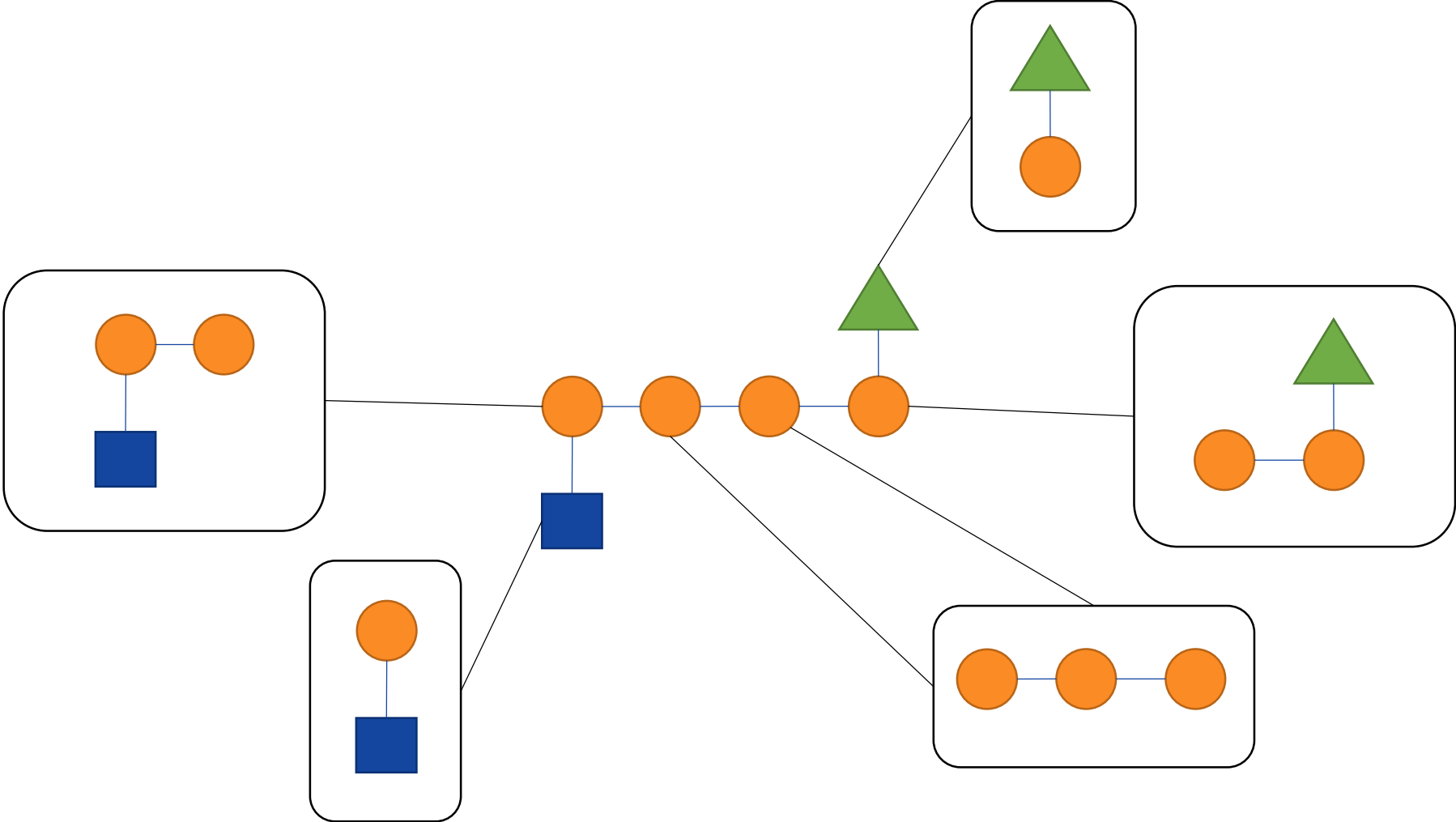


Solution:
neighbourhood
shapes

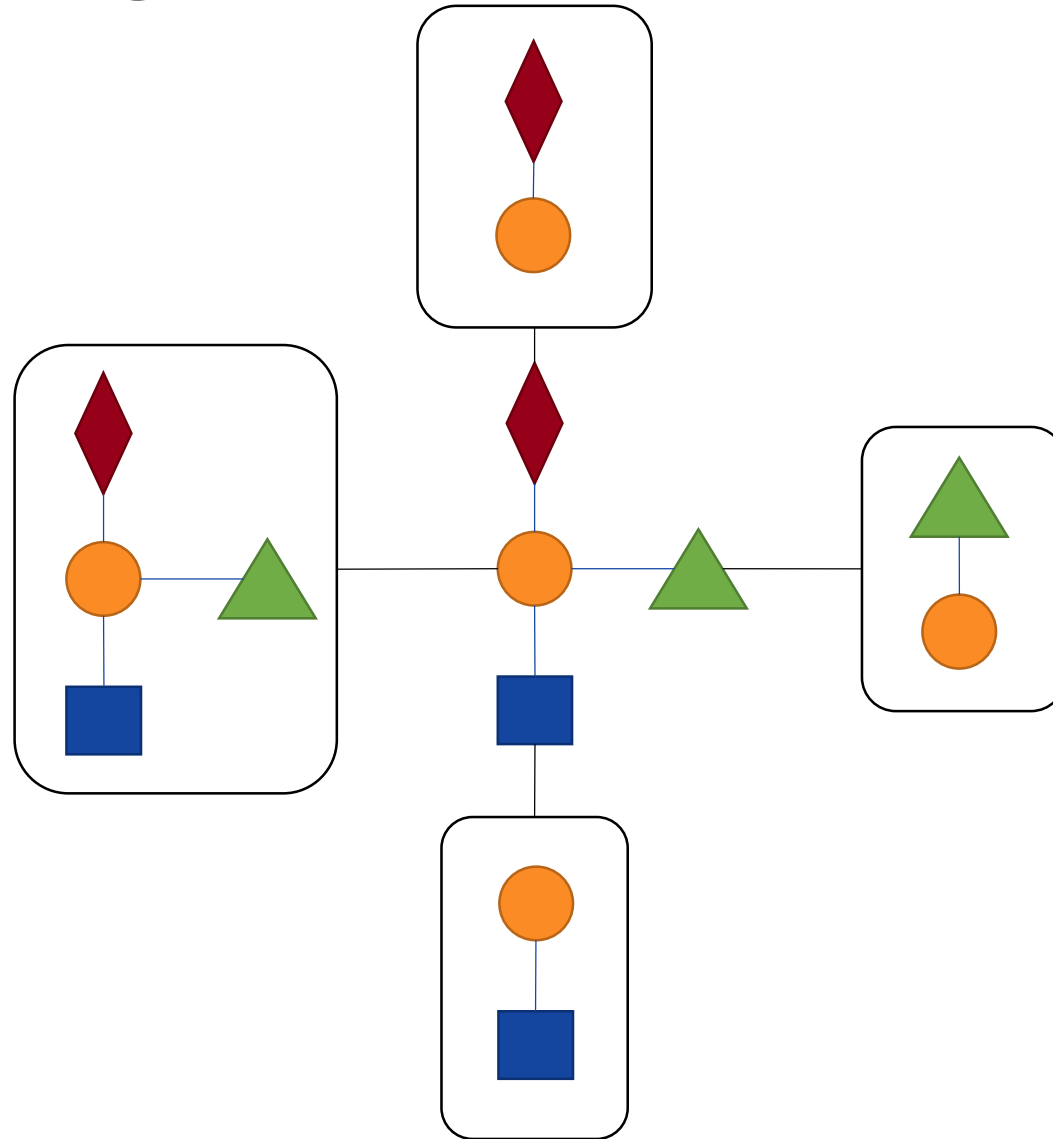
Shapes in M_1



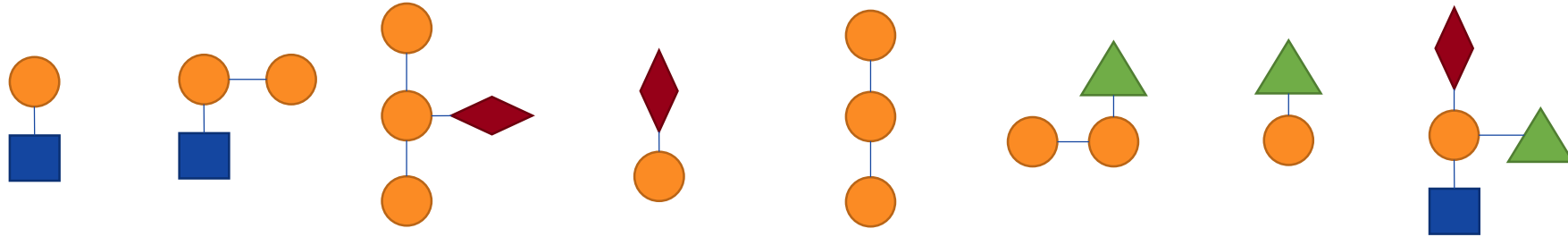
Shapes in M_2



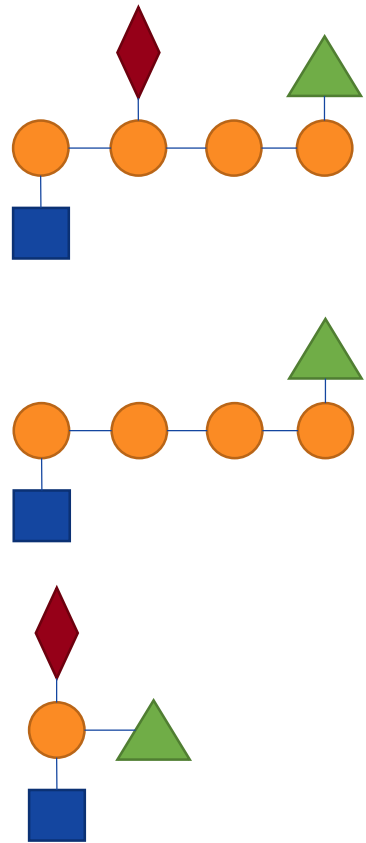
Shapes in M_3



Similarity basis: Shape vectors



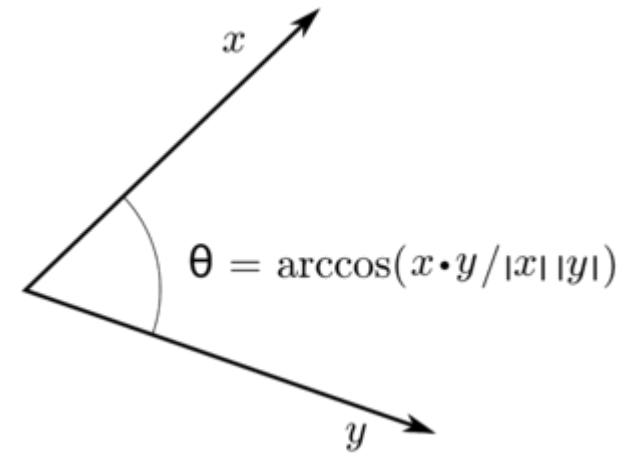
vector



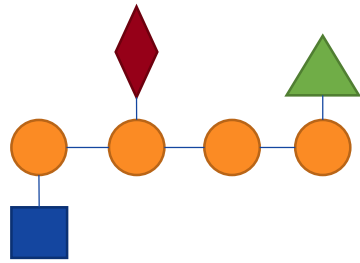
1	1	1	1	1	1	1	0	11111110
1	1	0	0	2	1	1	0	11002110
1	0	0	1	0	0	1	1	10010011

Cosine similarity

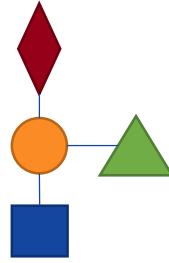
- Well known similarity measure between vectors
- The cosine of the enclosed angle
 - Nonnegative vectors $\rightarrow \theta < 90^\circ$
 - Smaller the angle larger the *cosine similarity*
- Computed from euclidean product
- Advantages:
 - Not affected by model size (as opposed to vector difference)
 - Sensitive to neighbourhood distribution



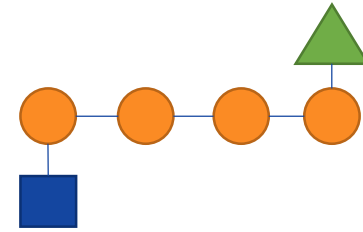
Cosine similarity of models



$$v(M_1) = (1, 1, 1, 1, 1, 1, 1, 0)$$



$$v(M_2) = (1, 0, 0, 1, 0, 0, 1, 1)$$



$$v(M_3) = (1, 1, 0, 0, 2, 1, 1, 0)$$

- Applying cosine similarity to shape vectors

- M_1 vs M_2 : 0.567 – *different*
- M_1 vs M_3 : 0.802 – *similar*
- M_2 vs M_3 : 0.353 – *very different*

→ First two models are similar

If M_1 is *real*, M_2 is *realistic*, M_3 is not.

Model diversity basis: neighbourhood sets

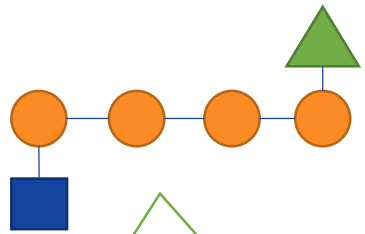
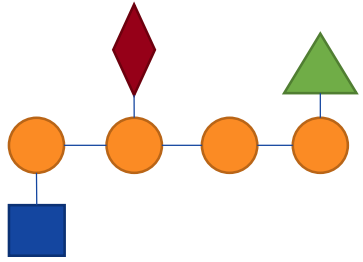
- Idea: Similar neighbourhoods cover similar parts of code

→ Goal: differentiate between models by neighbourhoods

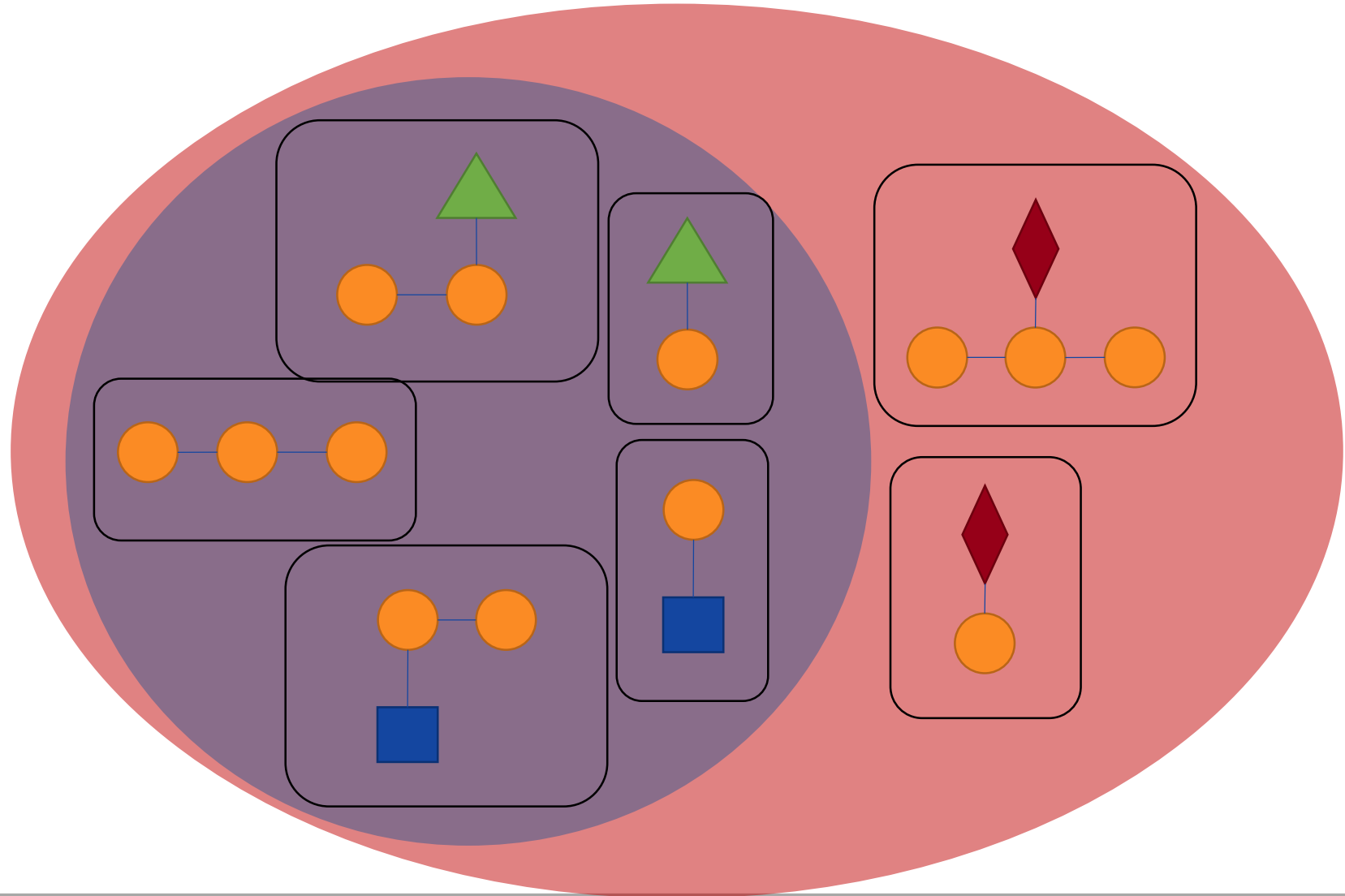
Advantage: not affected by shape distribution, model size

- *External diversity*: How big is the difference between two models?
 - Selection of diverse test cases
 - Symmetric difference of model neighbourhood sets
- *Internal diversity*: How effective is a model?
 - Test coverage vs input size
 - #neighbourhoods/#objects

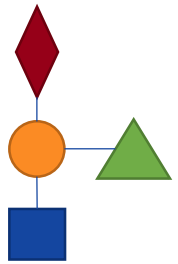
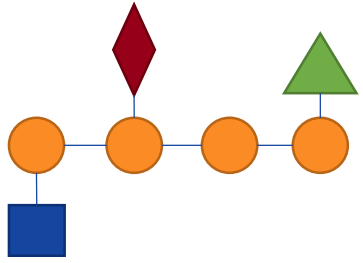
Shape difference: M_1 vs M_2



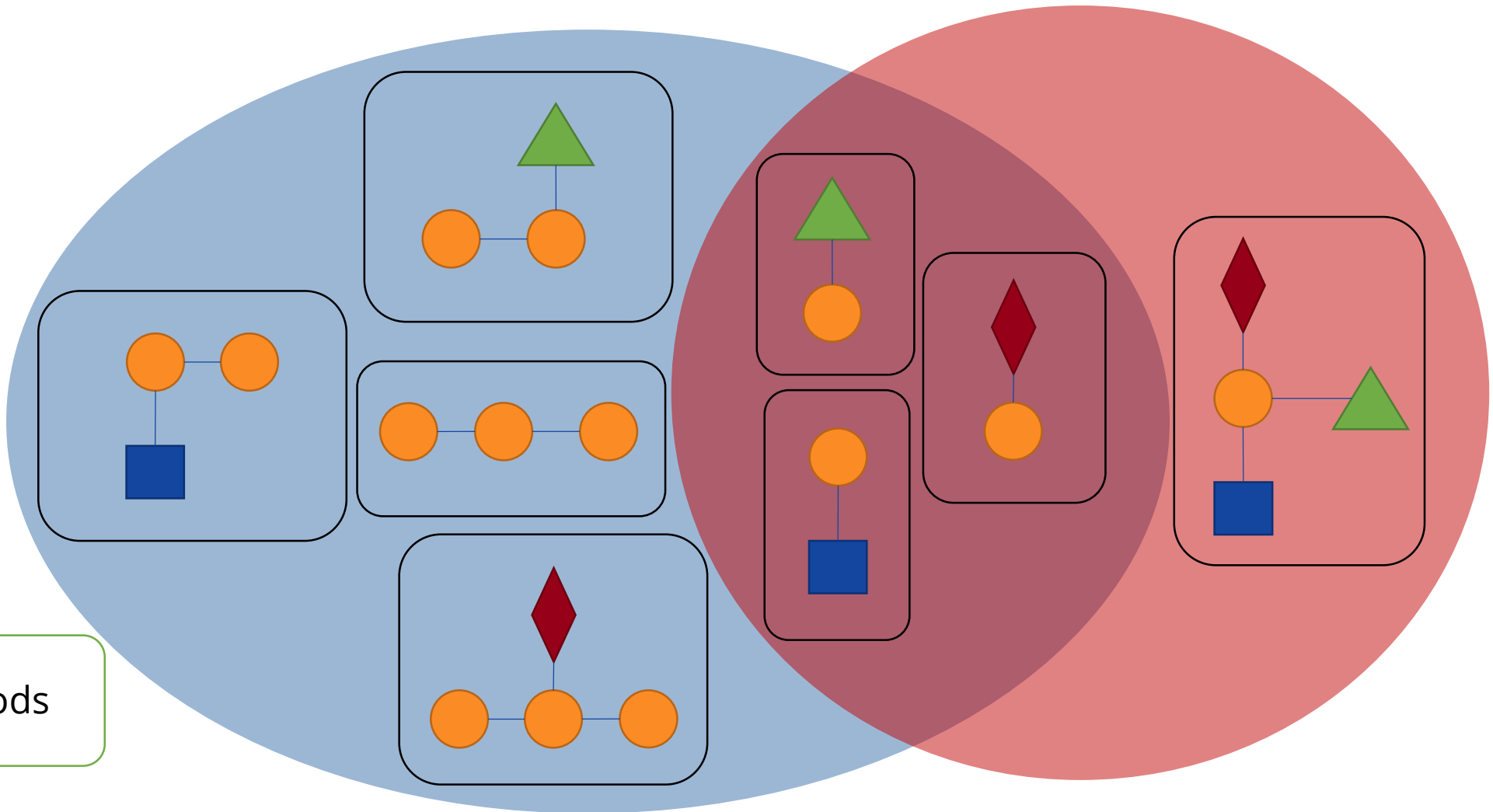
Similar:
5 neighbourhoods
in common



Shape difference: M_1 vs M_3



Different:
3 neighbourhoods
in common



Internal and external model diversity

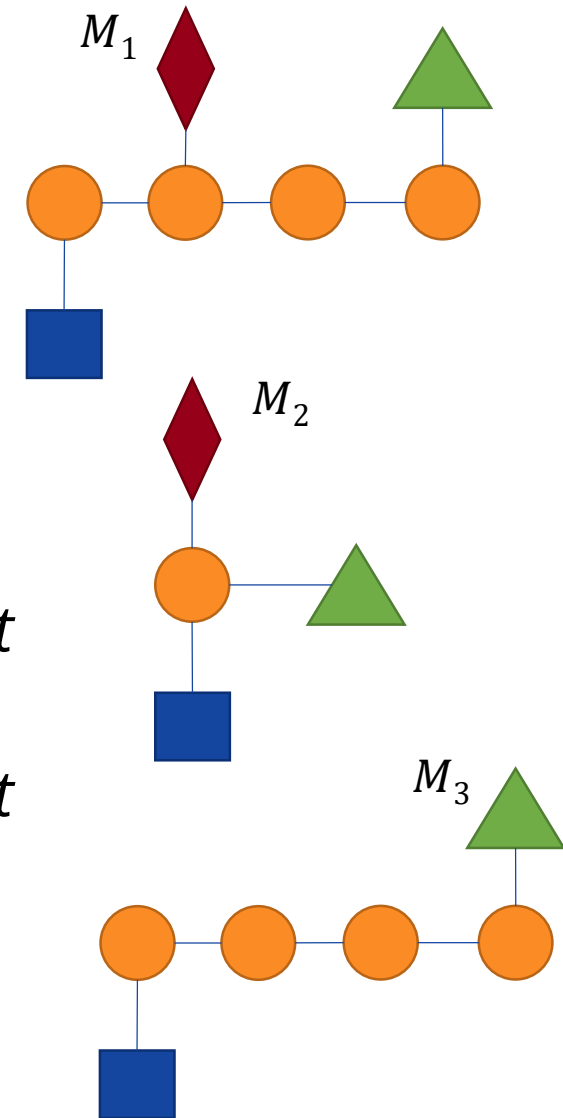
- Internal diversity:

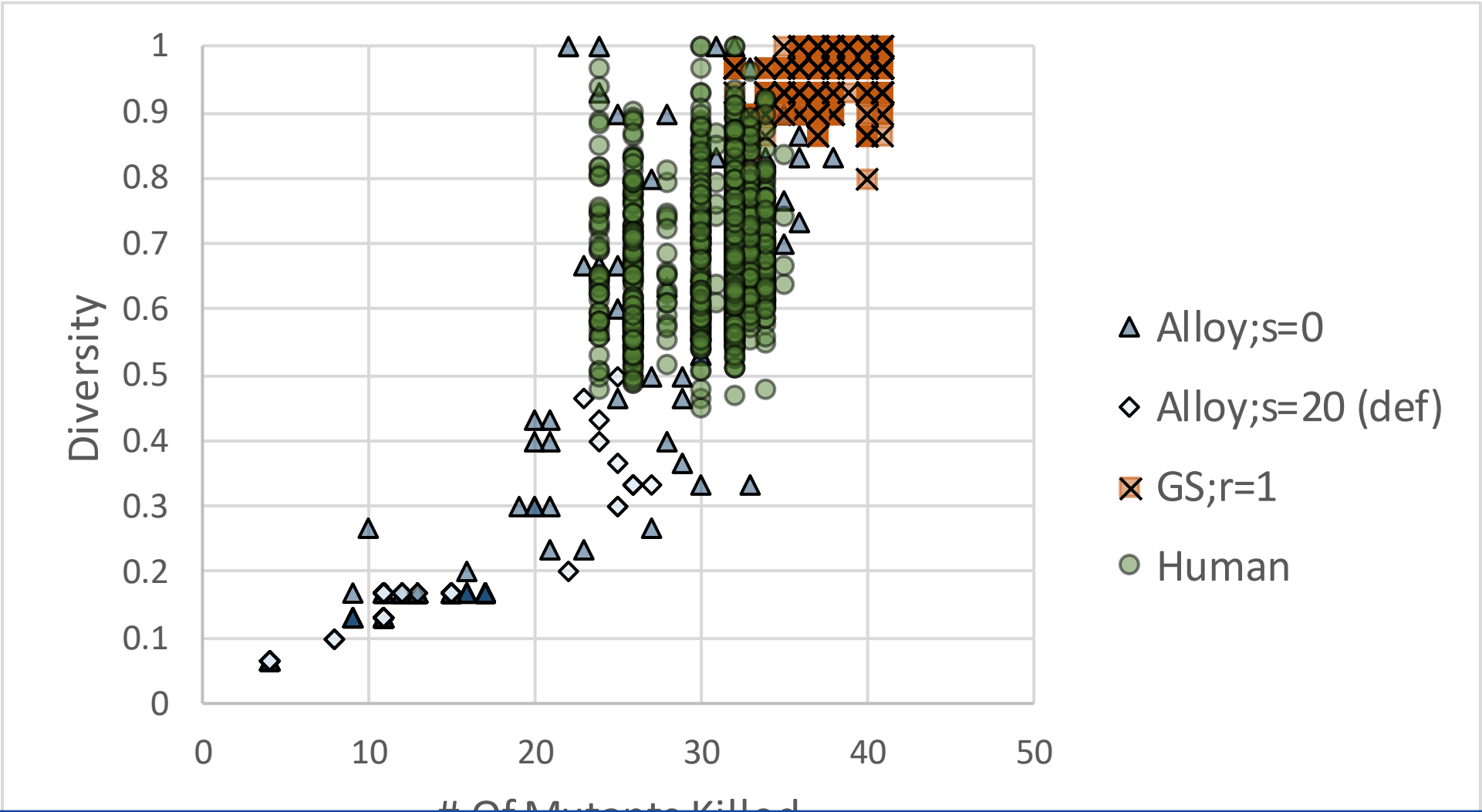
- M_1 : $7/7=1$
- M_2 : $4/4=1$
- M_3 : $5/6=0.8333$

- External diversity:

- M_1 vs M_2 : 5 neighbourhoods only in one model – *different*
- M_1 vs M_3 : 2 neighbourhoods only in one model – *similar*
- M_2 vs M_3 : 5 neighbourhoods only in one model – *different*

→ M_1 and M_2 should be the selected test cases





Alloy (def) < Alloy (s=0) < Human < GS

Correlation between **Diversity** and **Mutation Score** in Alloy+GS+Human

Properties of Model Generators: Scalable

- In size: ability to generate huge graphs
- In quantity: generation time of next model does not grow

CO

Consistent

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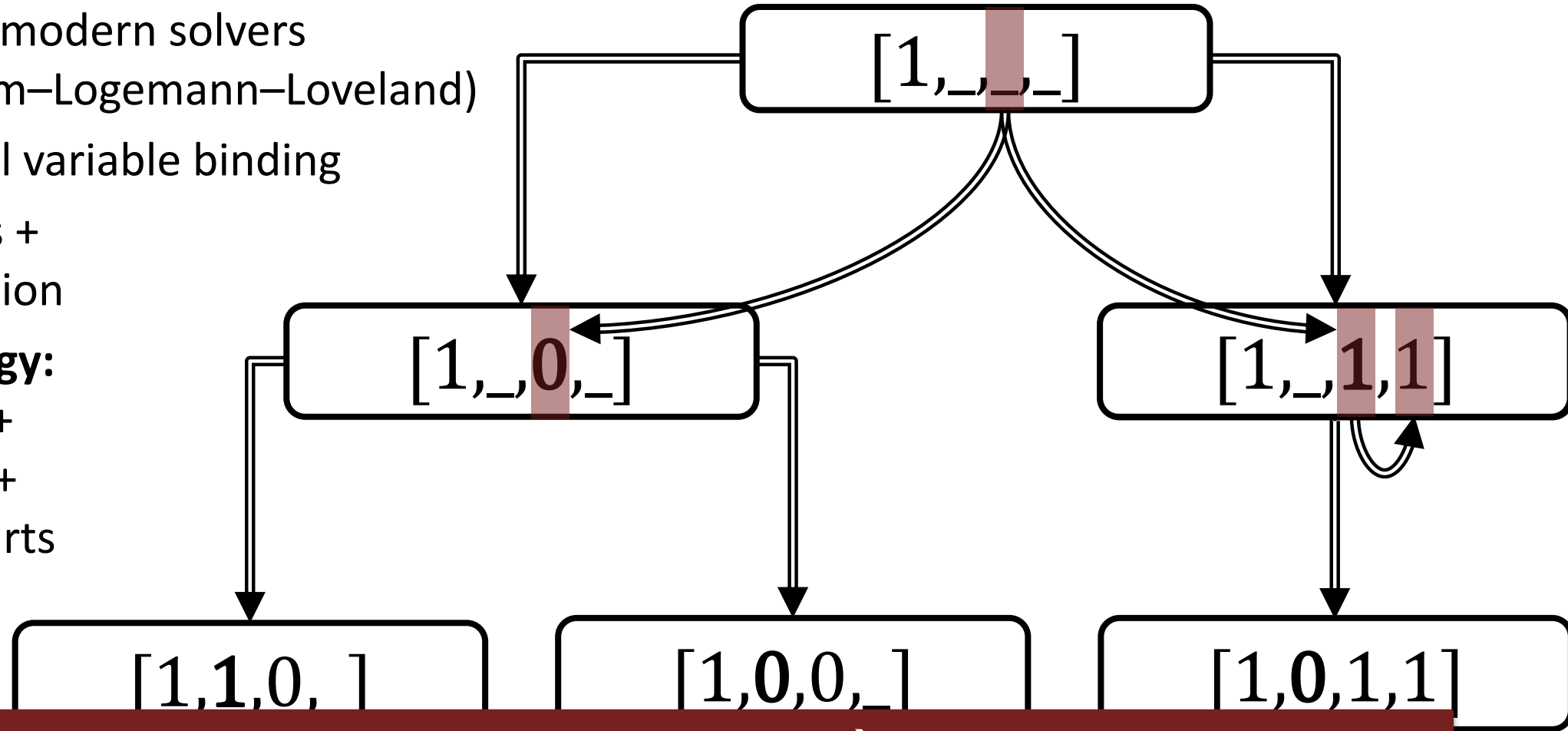
Scalable

Partial Modeling for Model Generation

3-Valued Models

SAT Solver Overview: DPLL Algorithm

- **DPLL:** Well-known SAT-algorithm, $(A \vee B \vee C) (\neg C \vee B \vee D) (\neg A \vee B \vee C) (\neg A \vee \neg B \vee \neg C)$
basis of most modern solvers
(Davis–Putnam–Logemann–Loveland)
- Refines partial variable binding
- Decision rules +
Unit propagation
- **Search Strategy:**
Backtracking +
Backjumping +
Random restarts

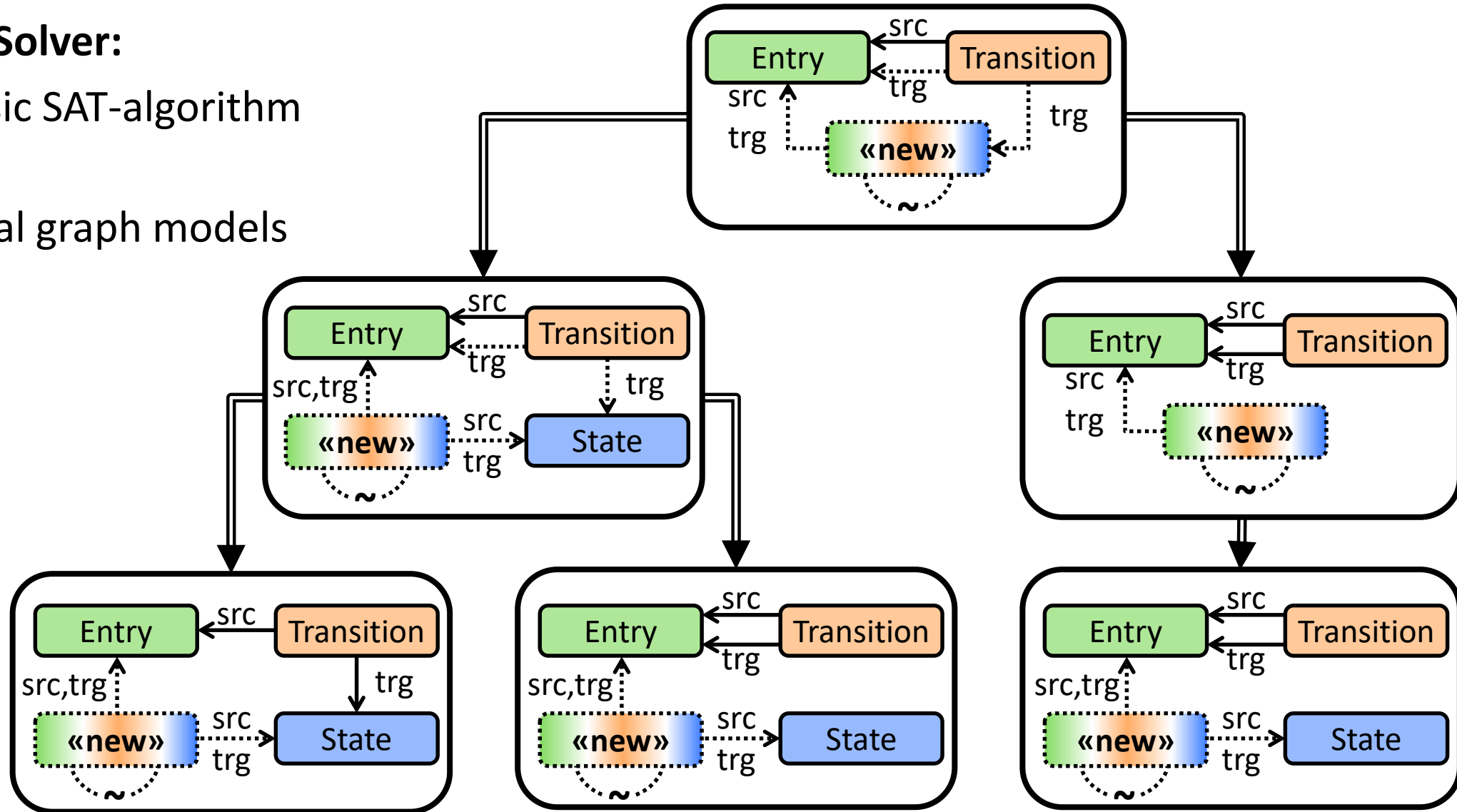


Our approach: Boolean variables \rightarrow Graphs

Graph Solver Overview: 3-Valued Partial Models as States

Graph Solver:

- 1) Based on classic SAT-algorithm
- 2) Refinement of 3-valued partial graph models

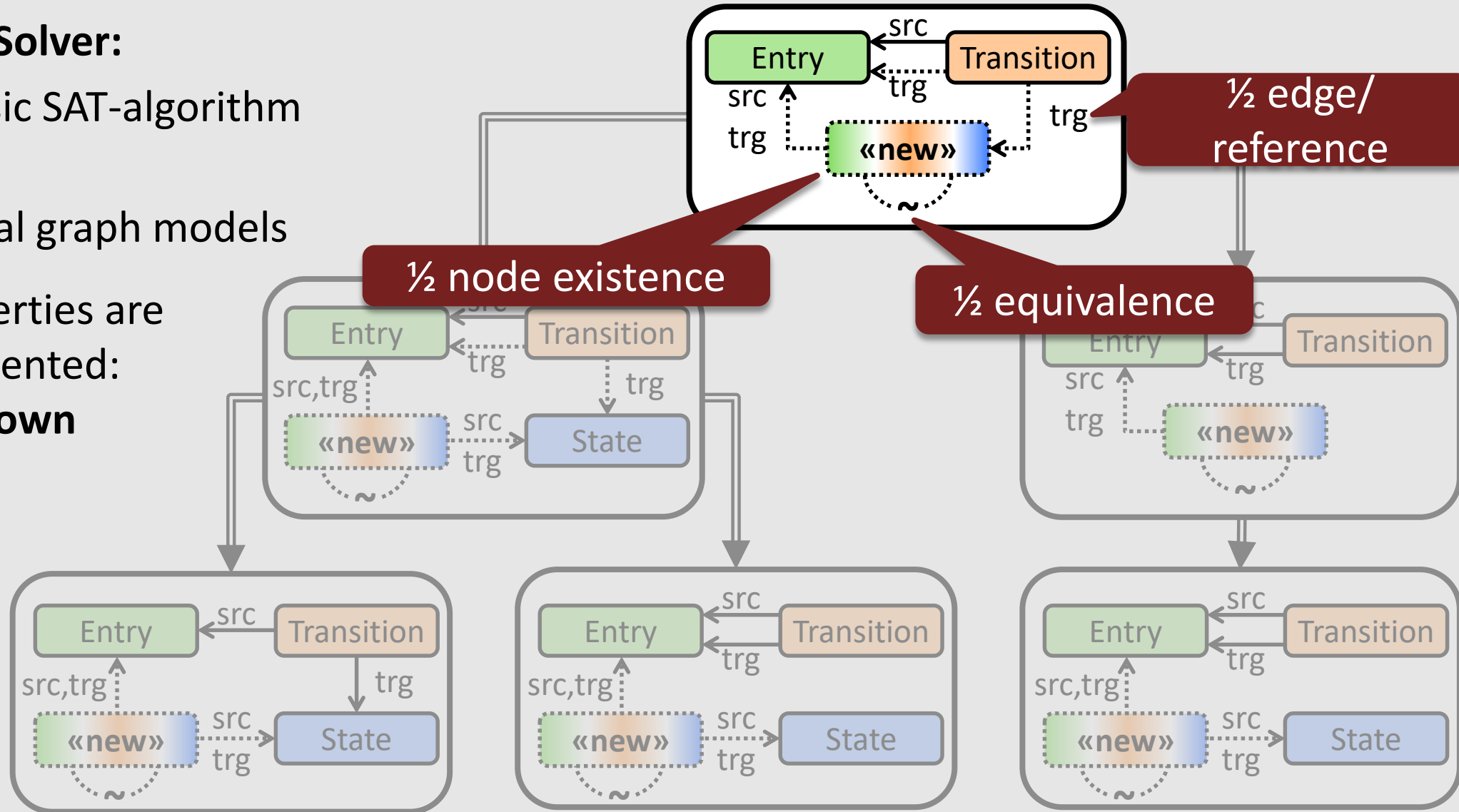


Graph Solver Overview: 3-Valued Partial Models as States

Graph Solver:

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- 2) Refinement of 3-valued partial graph models

- Uncertain properties are explicitly represented:
1 | 0 | $\frac{1}{2}$: **Unknown**

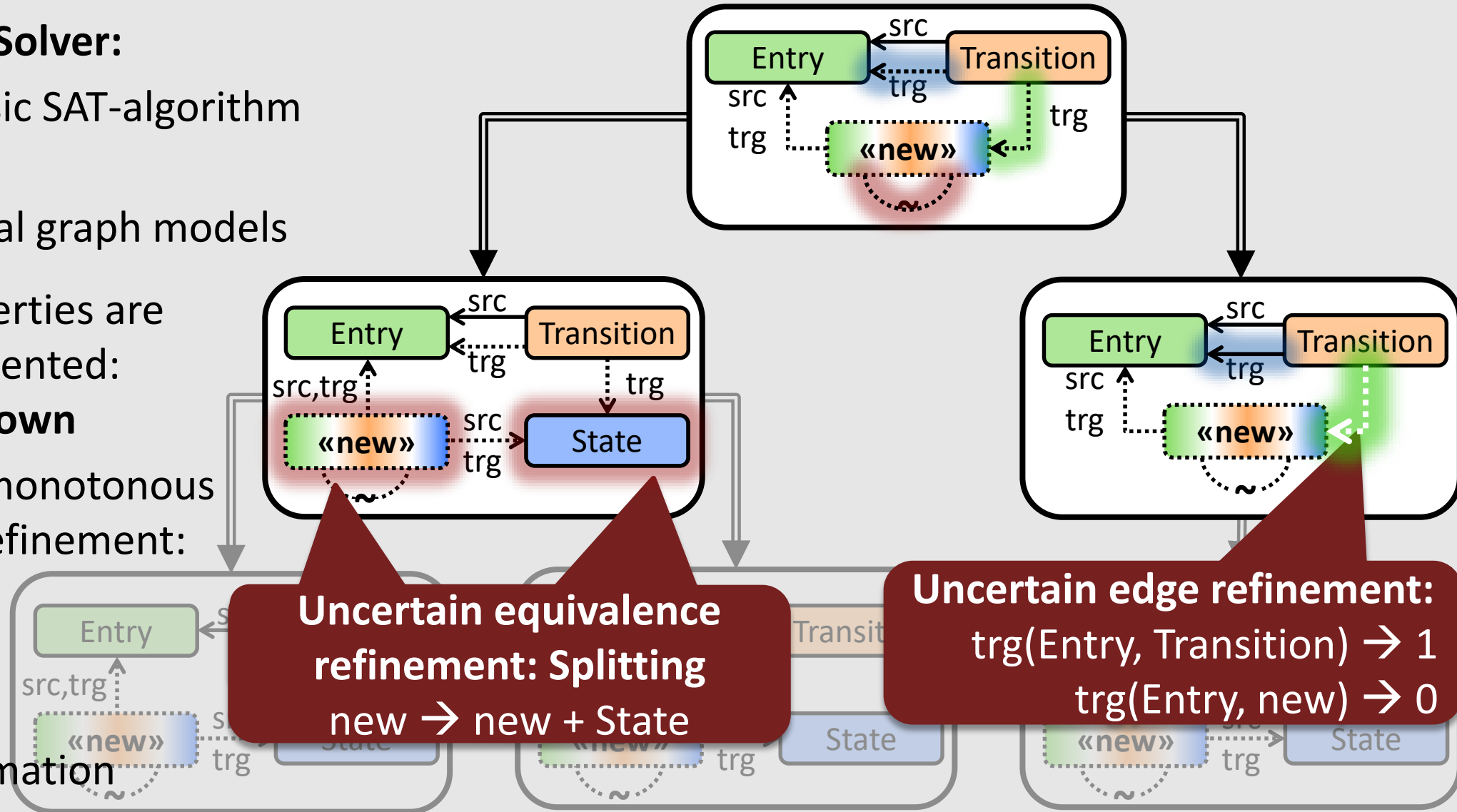


Graph Solver Overview: Partial Model Refinement

Graph Solver:

- 1) Based on classic SAT-algorithm
- 2) Refinement of 3-valued partial graph models

- Uncertain properties are explicitly represented:
 $1 \mid 0 \mid \frac{1}{2}$: **Unknown**
- Generation as monotonous partial model refinement:
 $\frac{1}{2} \rightarrow 1 \mid 0$
- Decision + Unit prop. \rightarrow Graph Transformation



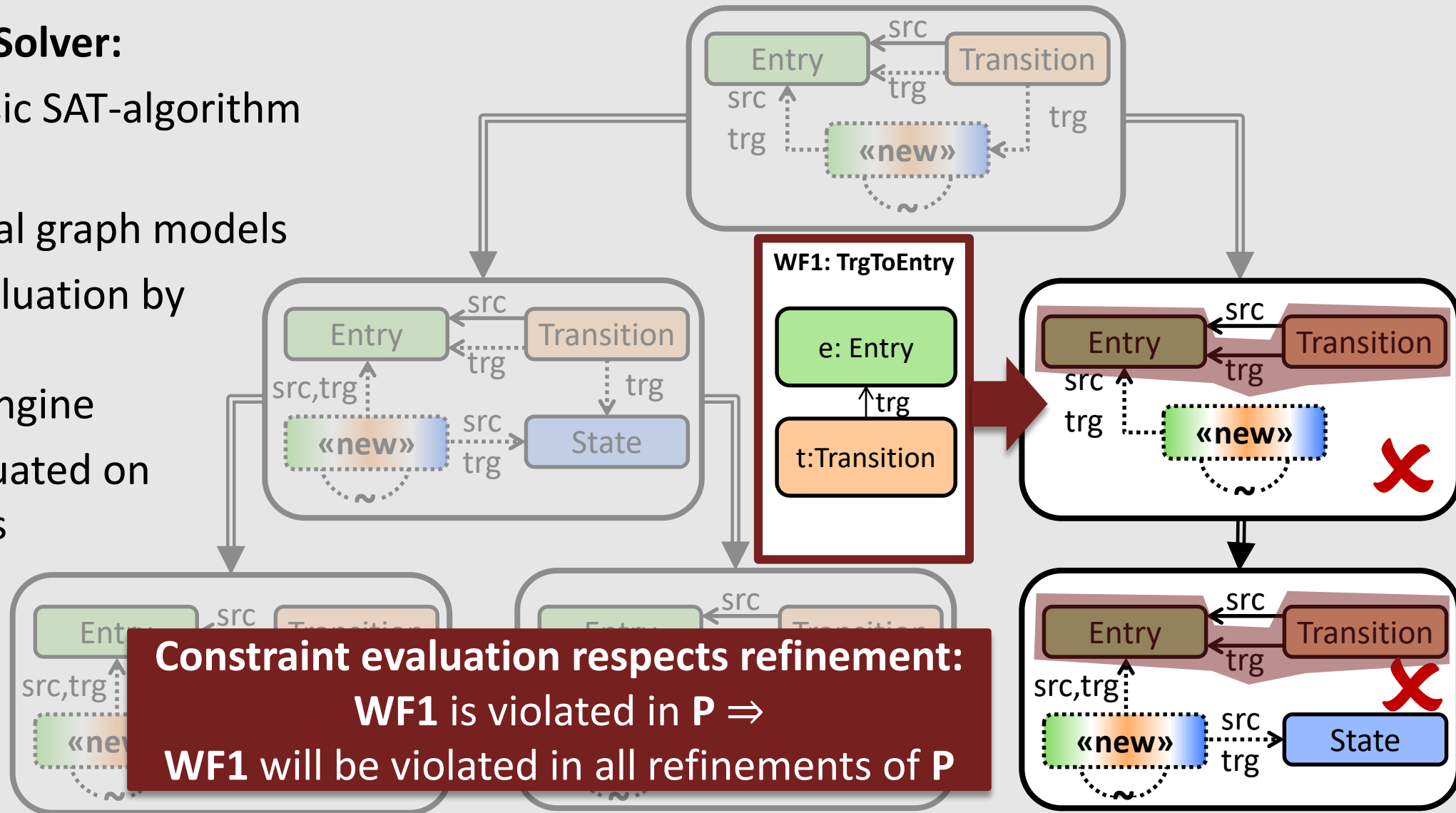
Uncertain equivalence refinement: Splitting
 $\text{new} \rightarrow \text{new} + \text{State}$

Uncertain edge refinement:
 $\text{trg}(\text{Entry}, \text{Transition}) \rightarrow 1$
 $\text{trg}(\text{Entry}, \text{new}) \rightarrow 0$

Graph Solver: Approximated Constraint Evaluation

Graph Solver:

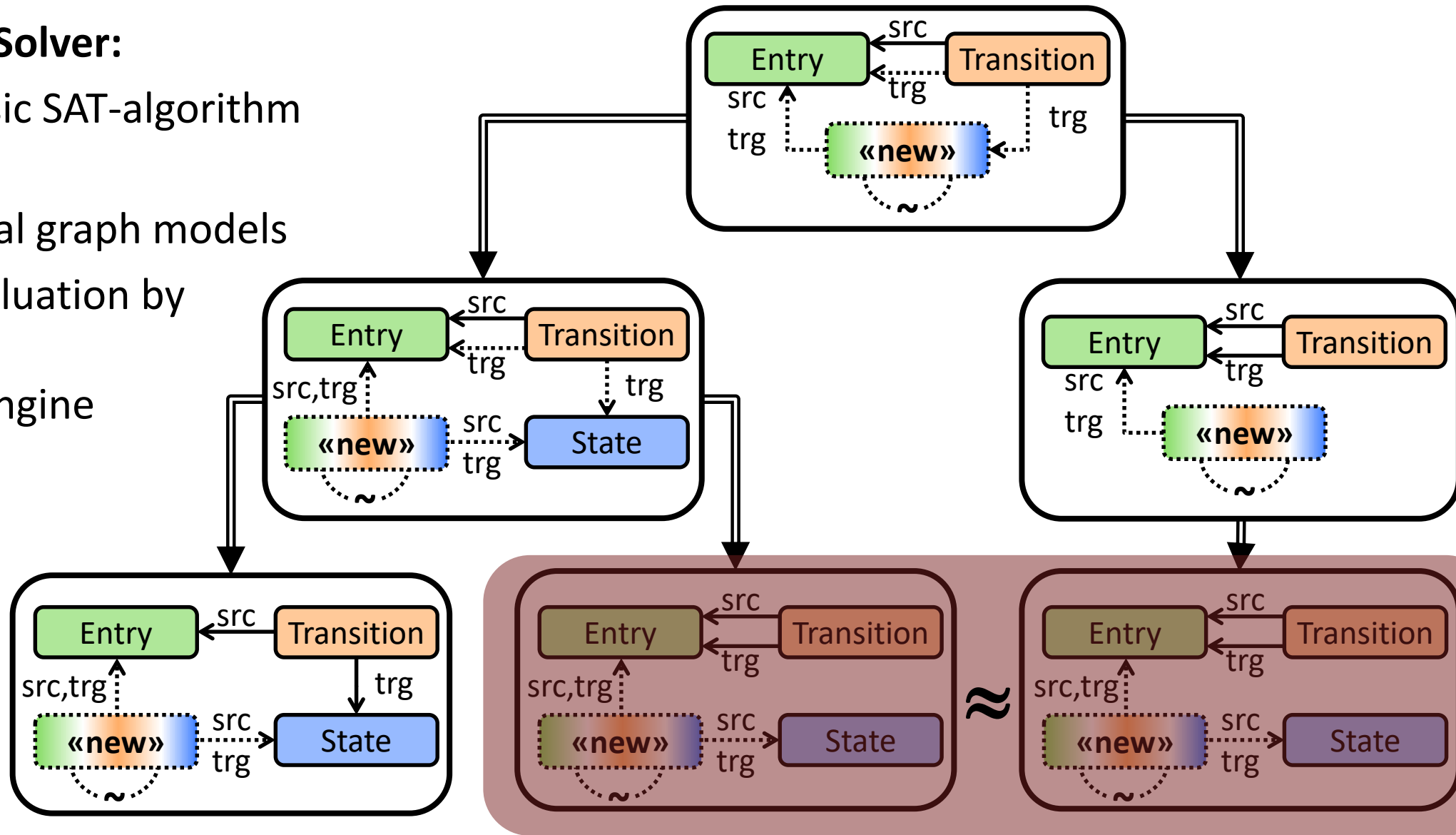
- 1) Based on classic SAT-algorithm
 - 2) Refinement of 3-valued partial graph models
 - 3) Constraint evaluation by incremental graph query engine
- Constraint evaluated on partial solutions
 - Monotonous reasoning
 - Incremental constraint reevaluation



Graph Solver Overview: Equivalence Partitioning

Graph Solver:

- 1) Based on classic SAT-algorithm
 - 2) Refinement of 3-valued partial graph models
 - 3) Constraint evaluation by incremental graph query engine
 - 4) Equivalence detection by graph isomorphism
- State encoding

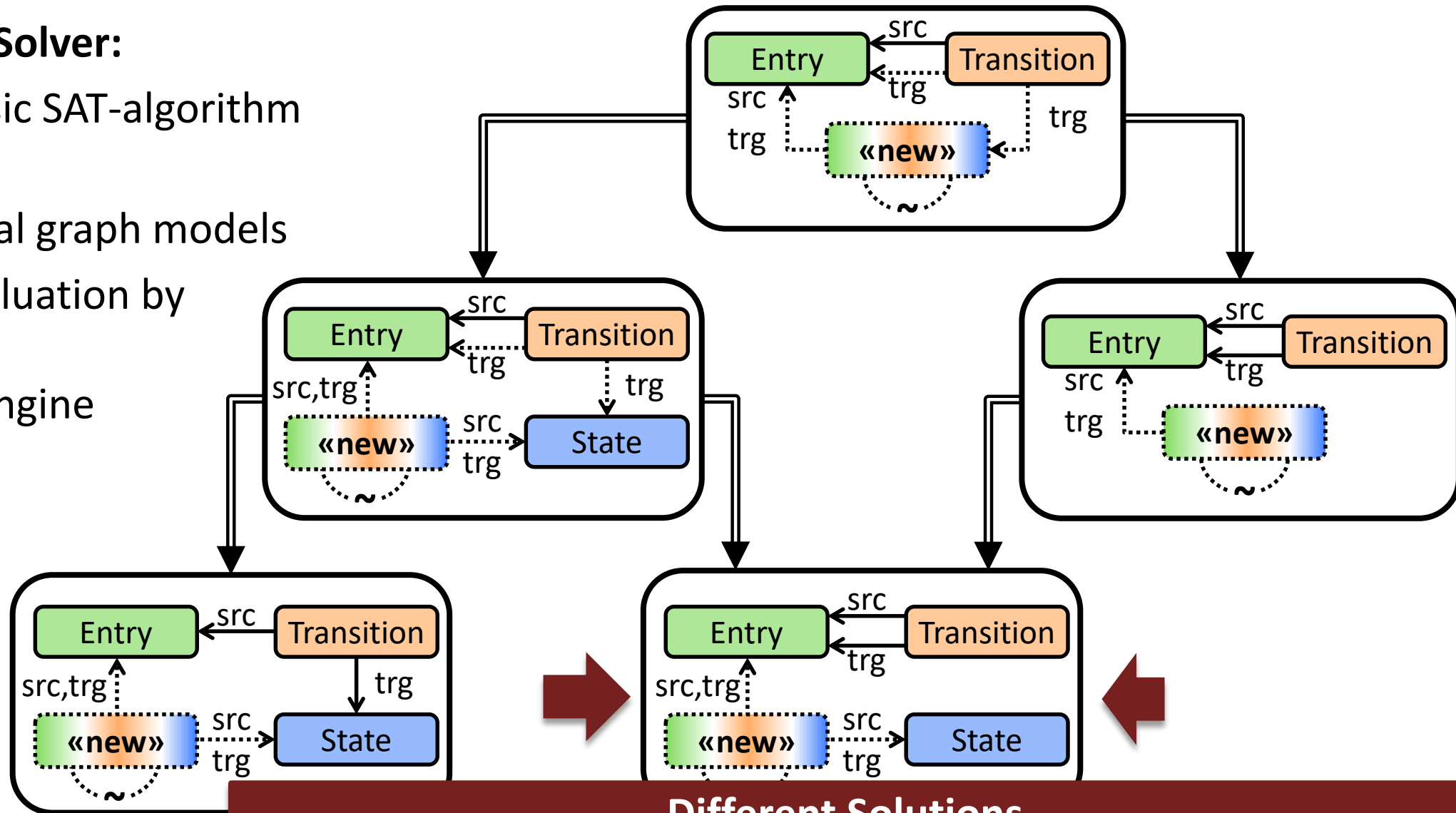


Graph Solver Overview: Equivalence Partitioning

Graph Solver:

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- 4) Equivalence detection by graph isomorphism

- State encoding
- Partial order reduction

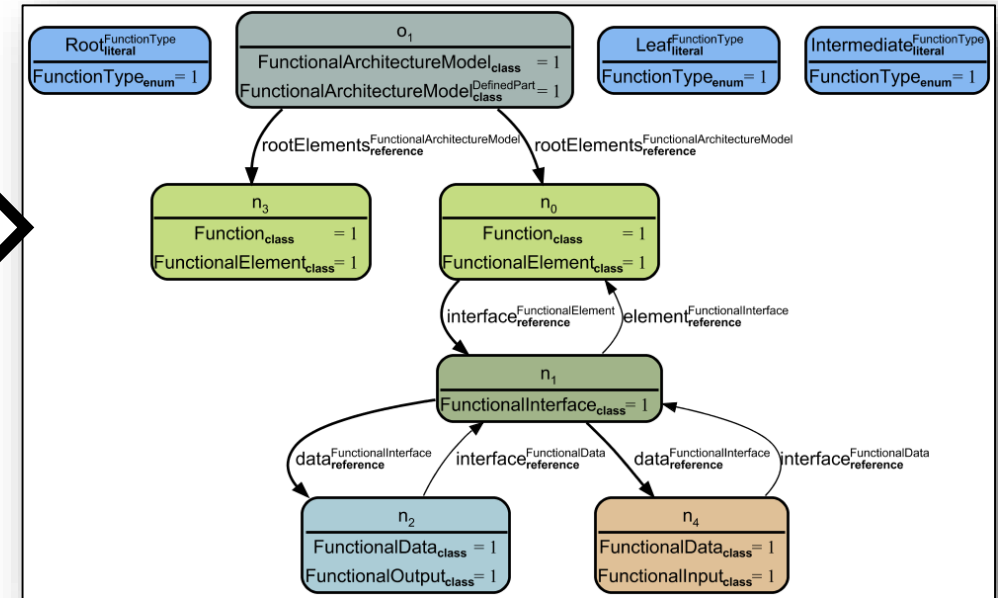
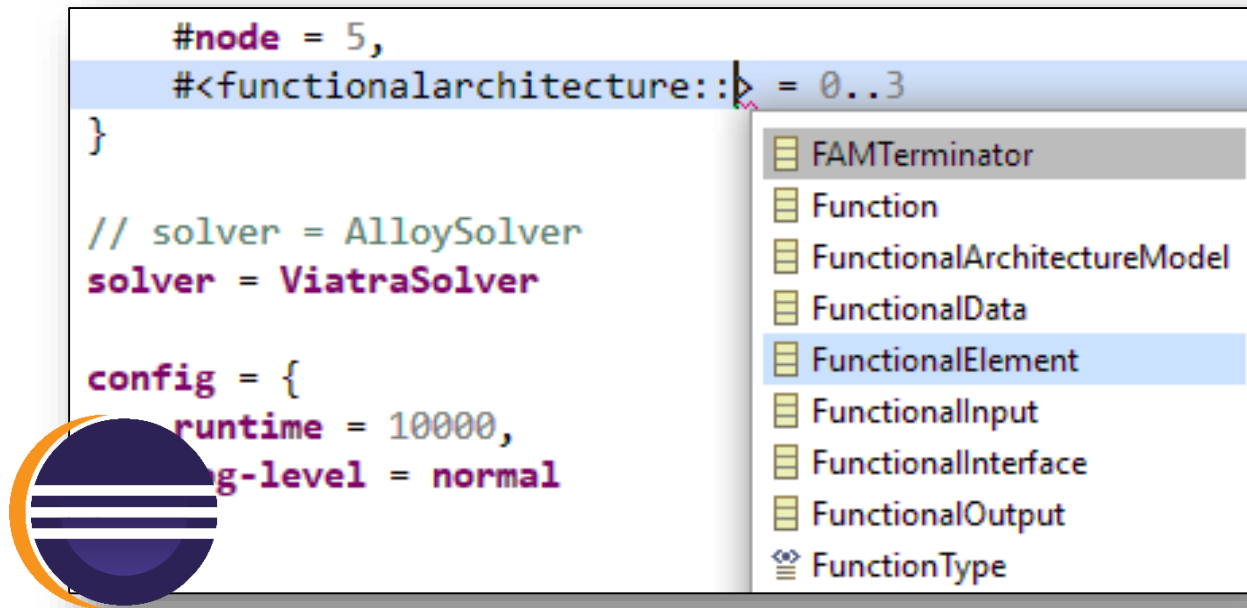



Different Solutions

VIATRA Solver: An Open Source Implementation

- Standard EMF as input and output | Configuration language | Visualization

```
#node = 5,  
#<functionalarchitecture::> = 0..3  
}  
  
// solver = AlloySolver  
solver = ViatraSolver  
  
config = {  
  runtime = 10000,  
  log-level = normal  
}
```



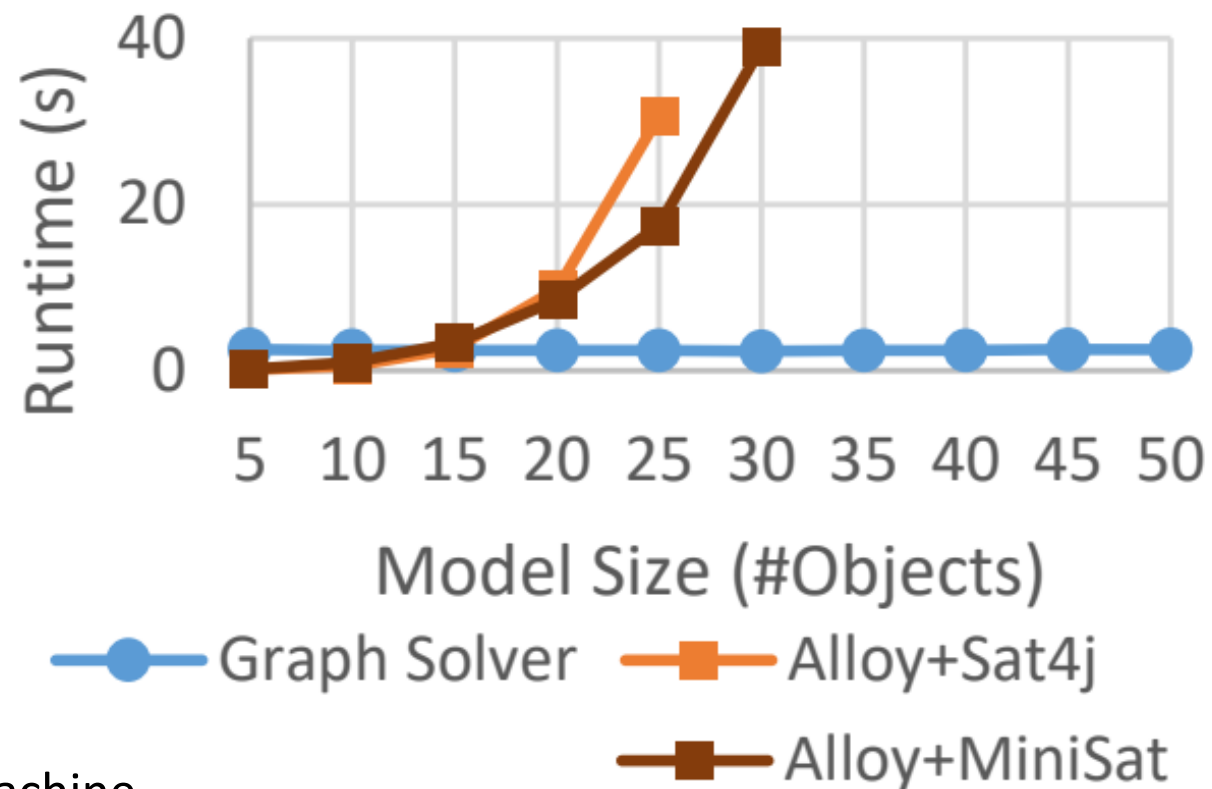
- Incremental Query Engine:  VIATRA
 - Constraint language: VIATRA Query
 - Internally uses: Incremental constraint reevaluation, DPLL as VIATRA DSE
- Open source: github.com/viatra/VIATRA-Generator

Scalability Measurements

Maximal model size

	Largest model (#Objects)		
	Graph Solver	Sat4J	MiniSat
FAM+WF	6250	58	61
FAM-WF	7000	87	92
Yak+WF	1000	–	–
Yak-WF	7250	86	90
FS	4750	87	89
Ecore	2000	38	41

Example comparison (FAM)



FAM: Industrial, Avionics

Yakindu: Industrial, Statemachine

FS: File System example of Alloy

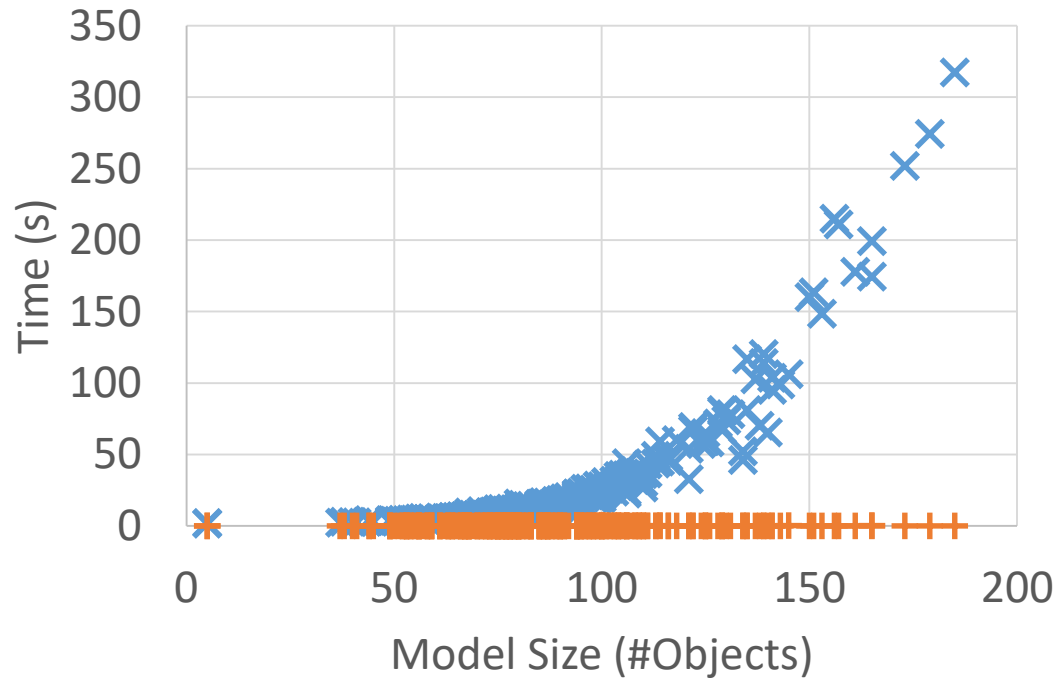
Ecore: Metamodelling language

5 min timeout

Our solver generates ~two orders of magnitude larger models

Additional Findings

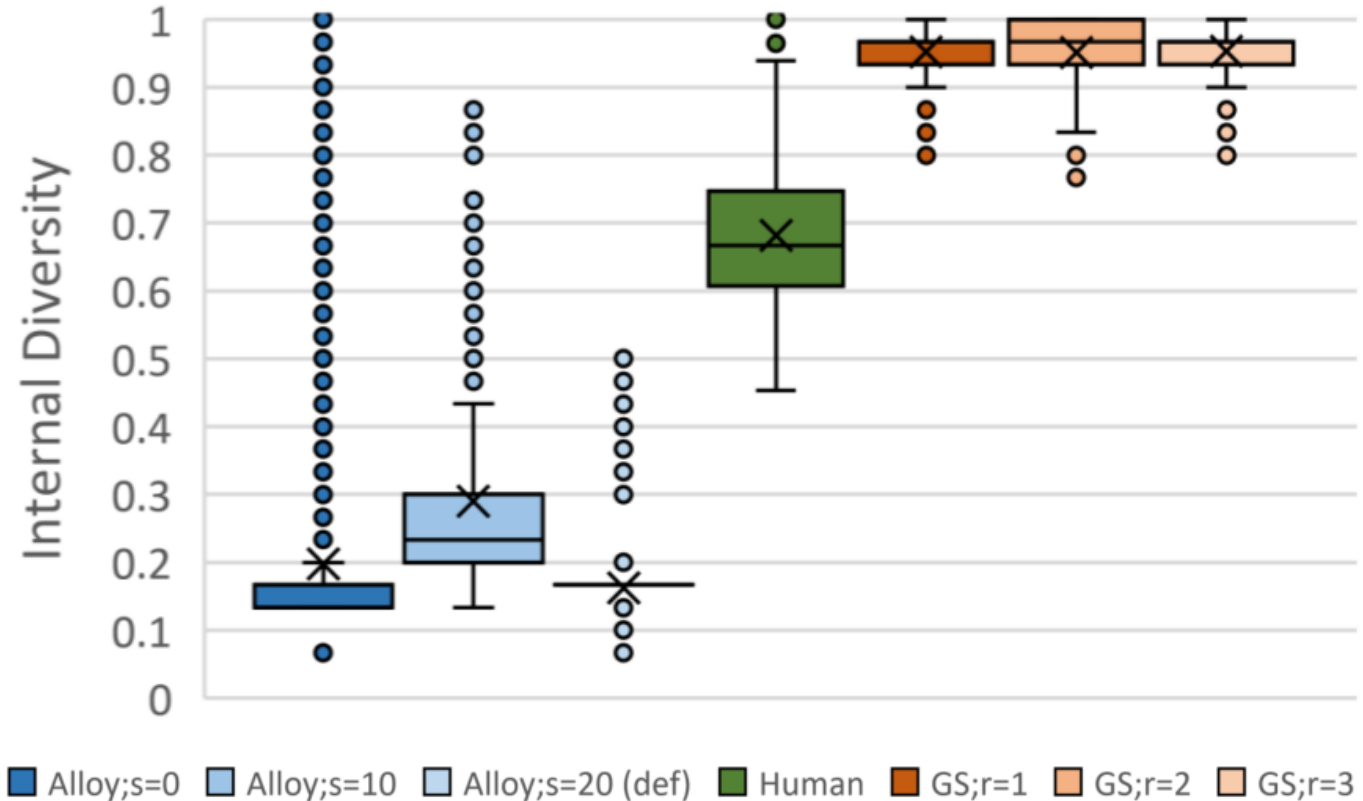
Constraint evaluation on complete graphs: Query Engine vs Alloy



× Validation by Alloy

+ Validation by Graph Query Engine

Diversity of graph models: Alloy vs Human vs Graph Solver

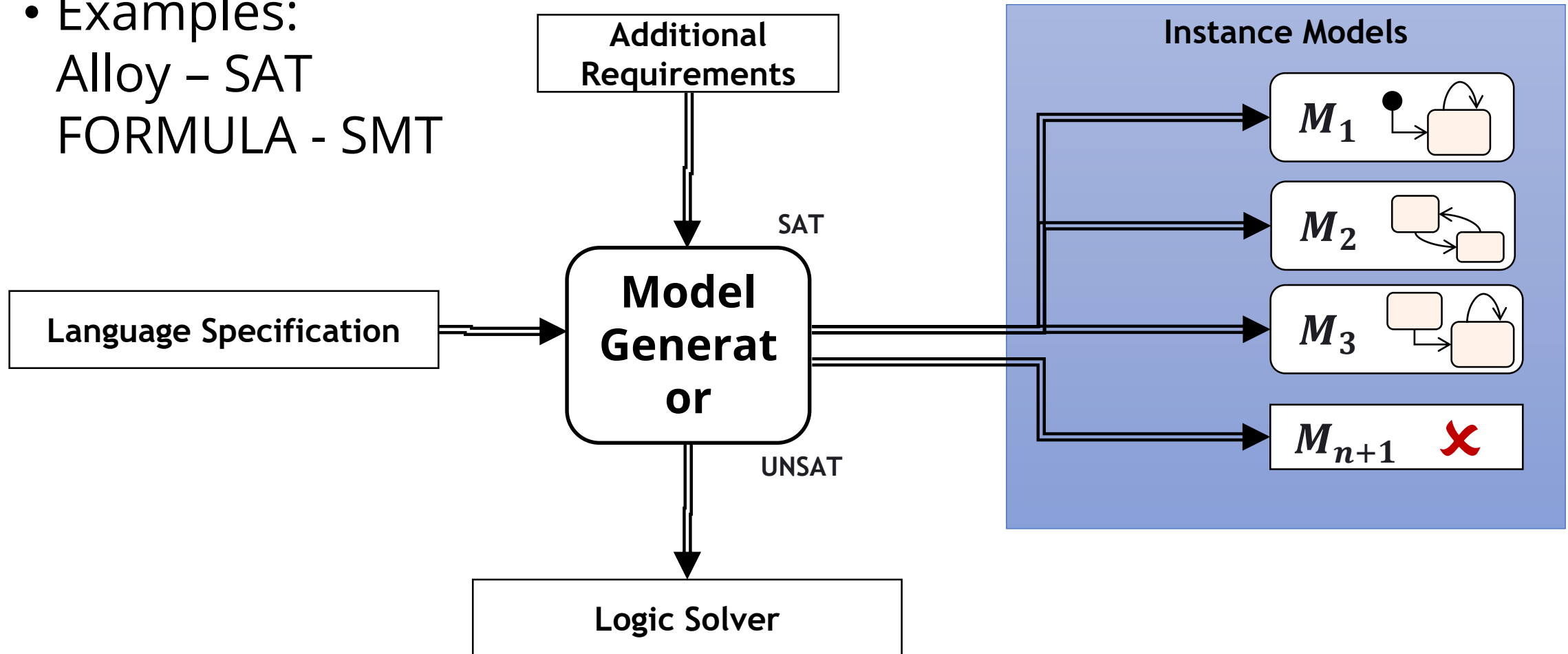


■ Alloy; s=0 ■ Alloy; s=10 ■ Alloy; s=20 (def) ■ Human ■ GS; r=1 ■ GS; r=2 ■ GS; r=3

Related Approaches

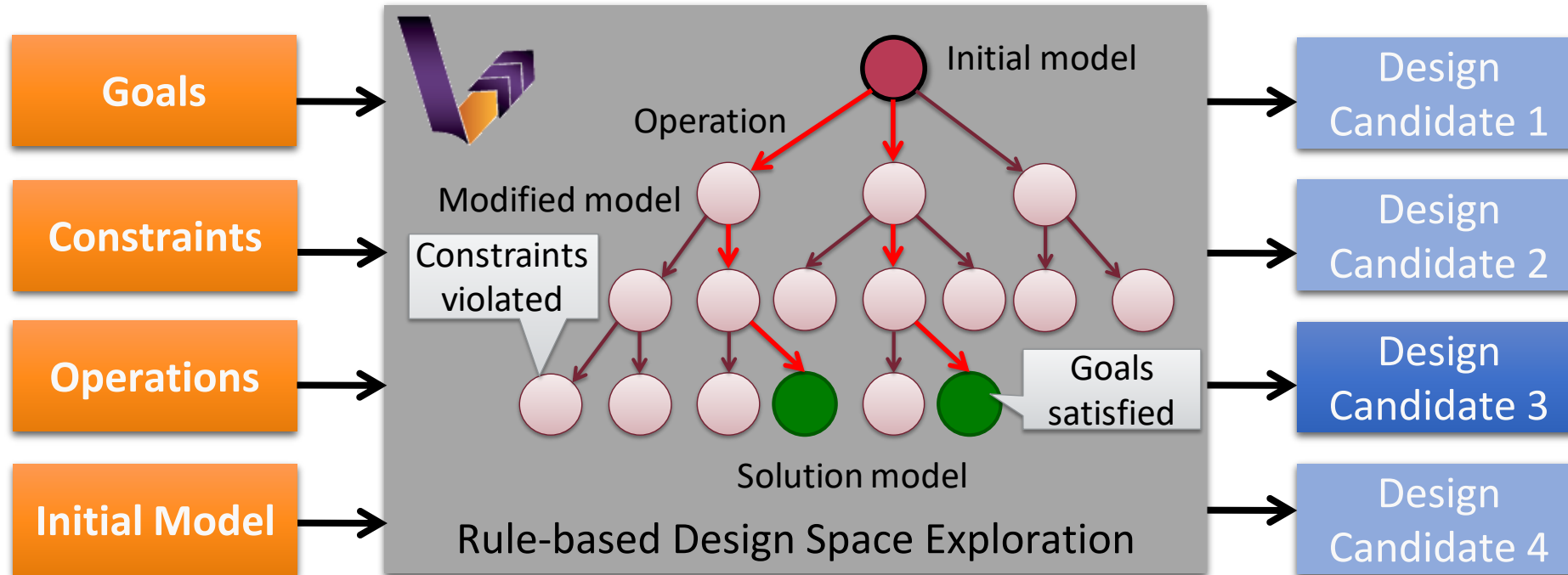
Solver-based model generators

- Examples:
Alloy – SAT
FORMULA - SMT



Rule-based Design Space exploration

ASE 11
ASE 14



Heuristics

- Approximate distance from a solution
- Guided or multi-objective optimization
- Backtracking / backjumping

Summary & Learning outcomes

Learning summary

- Model abstraction technique
- Model generation challenges
- Model generation \Leftrightarrow abstraction refinement