

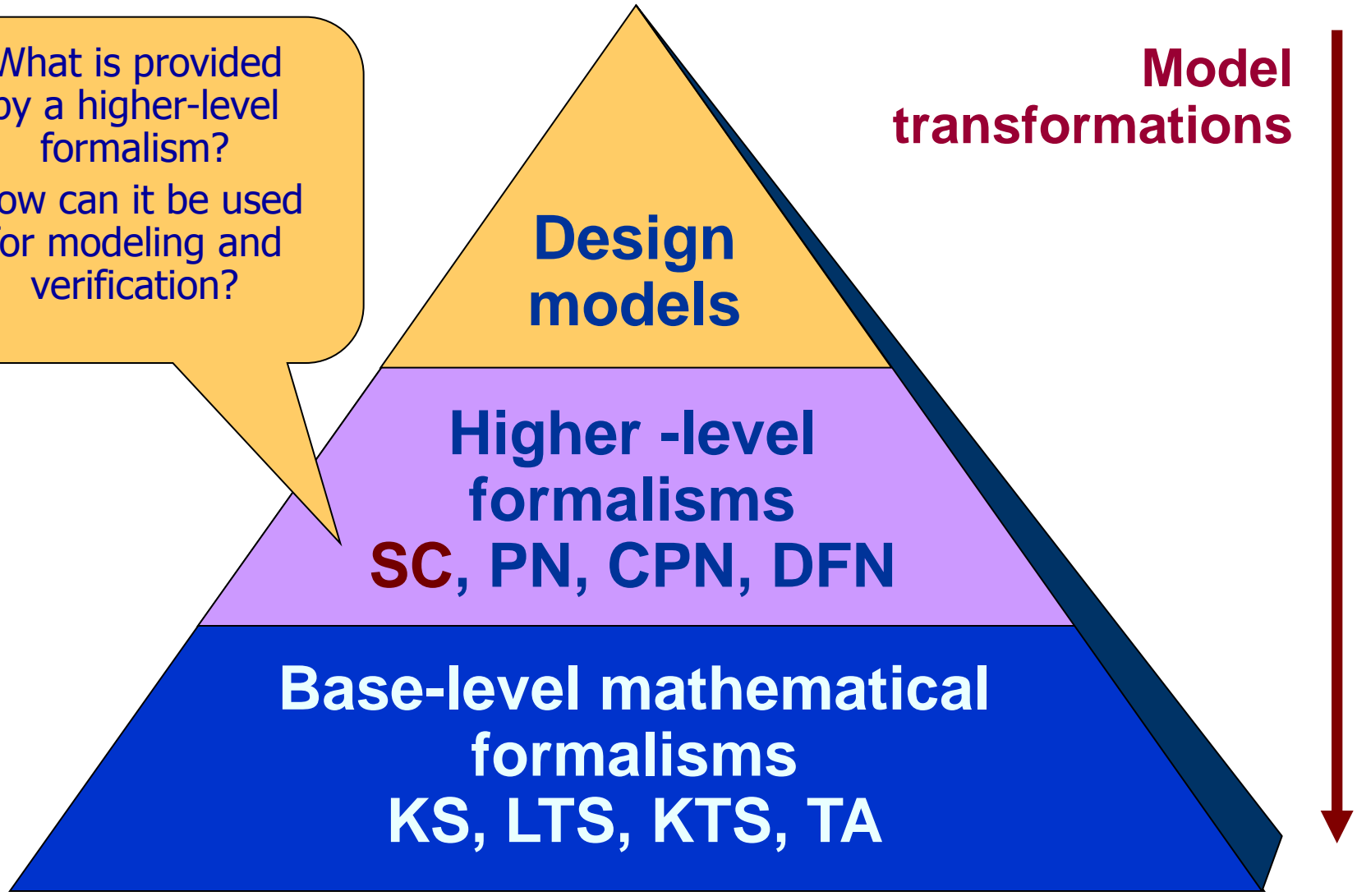
Higher-level formalisms: Statecharts

dr. István Majzik

BME Department of Measurement and
Information Systems

Formal models for verification

What is provided by a higher-level formalism?
How can it be used for modeling and verification?



Outline

- Basic elements
- Syntax of statecharts
 - UML 2 statechart diagram (state machine)
- Semantics of statecharts
 - UML 2 State Machine semantics
 - (Other semantics possible: e.g. Harel semantics)
- Using statecharts

What is the goal of statecharts?

- **Modeling state-based, event-driven behavior**
 - Description of the behavior of a state machine (~automaton)
 - **Reactive behavior:**
Describes change of state triggered by external events
 - E.g. incoming messages, signals, calls, ...
 - **Actions:** operations assigned to transitions
 - E.g. assignment, outgoing message, ...
- **Common usage:**
 - **Embedded systems:** processing incoming events (e.g. controlling a robot, processing signals, ...)
 - **Protocols:** processing messages

Terminology

- **State, active state**
 - Certain conditions hold (e.g. operation can be executed)
 - State variables have certain values
- **State transition**
 - Change of state
 - **Trigger event** can make it happen
 - Transitions without trigger: “spontaneous” execution
 - **Guard condition** can be assigned to transitions
 - Transition can occur only if guard condition is true
 - **Actions** can be executed when transitions occur
 - Operation or behavior assigned to a transition
- **Event**
 - Asynchronous occurrence, can have parameters
 - Individual entity, the instance of an event class

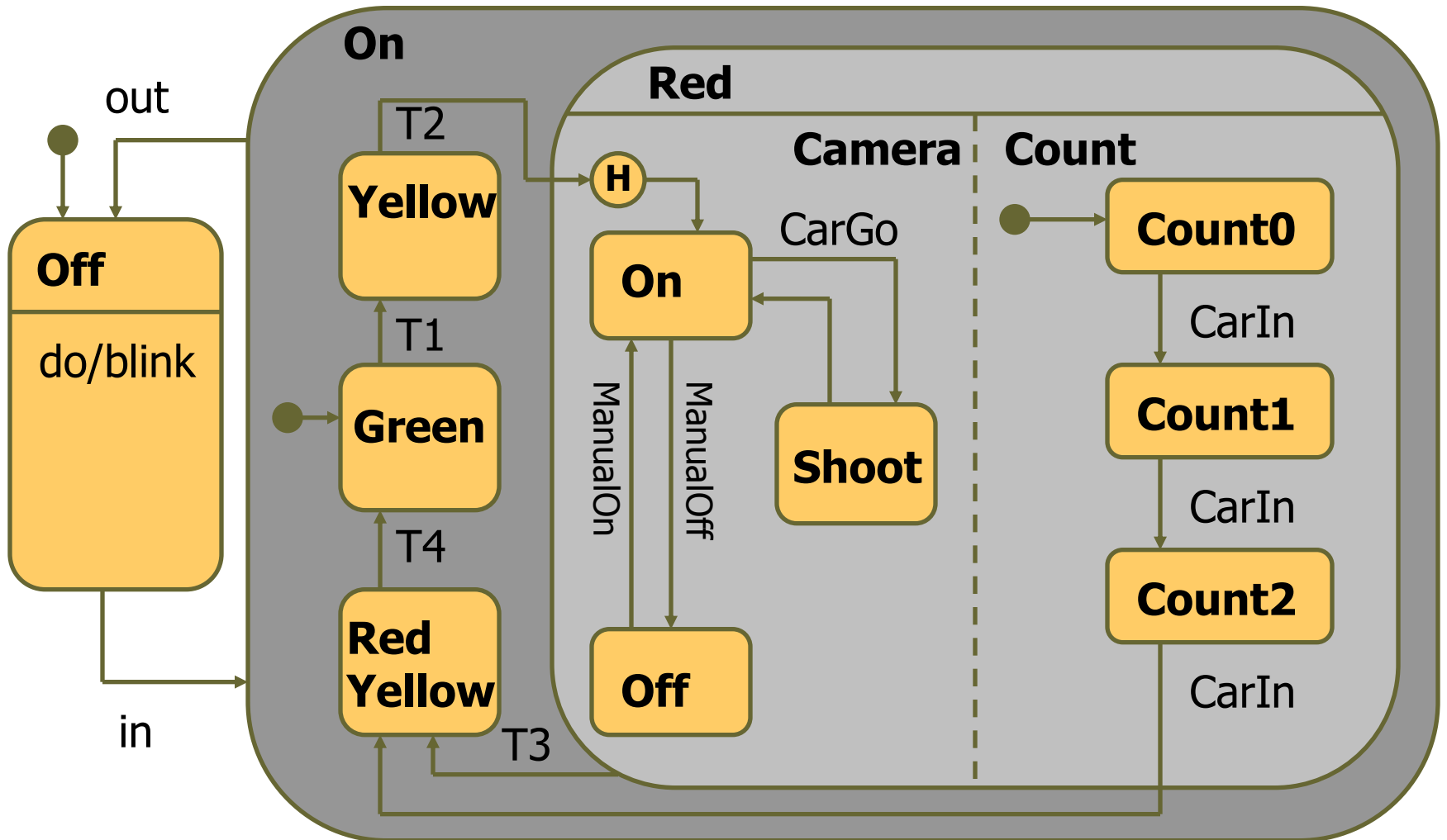
Additional features for convenient modeling

- **Refinement of states: State hierarchy**
 - Superstate: for the common properties of substates
- **Description of concurrent behavior**
 - No ordering is enforced
(processing simultaneously or in an arbitrary order)
 - Multi-threaded/distributed/parallel execution
- **Complex transitions**
 - Fork, join, conditional branch
- **Memory: Return to a previous state configuration**
 - Return from the processing of an interrupting event
 - In a single level of hierarchy or even deeper

State machines and statecharts

- **State machine:**
 - Flat, simple states and transitions
 - Similar to automata (e.g., in UPPAAL)
- **Statechart: extension of state machines**
 - **State hierarchy:** state refinement
 - **Concurrent regions:** to describe concurrent behavior
 - **Complex transitions:** fork, join, branch
 - **Memory:** “Storing” the last active state configuration
 - Some syntactic sugar
 - Rarely used (unintuitive) extensions
 - Delayed event, synchronization state, ...

Example: A statechart



Syntax of statecharts (conforming to UML)

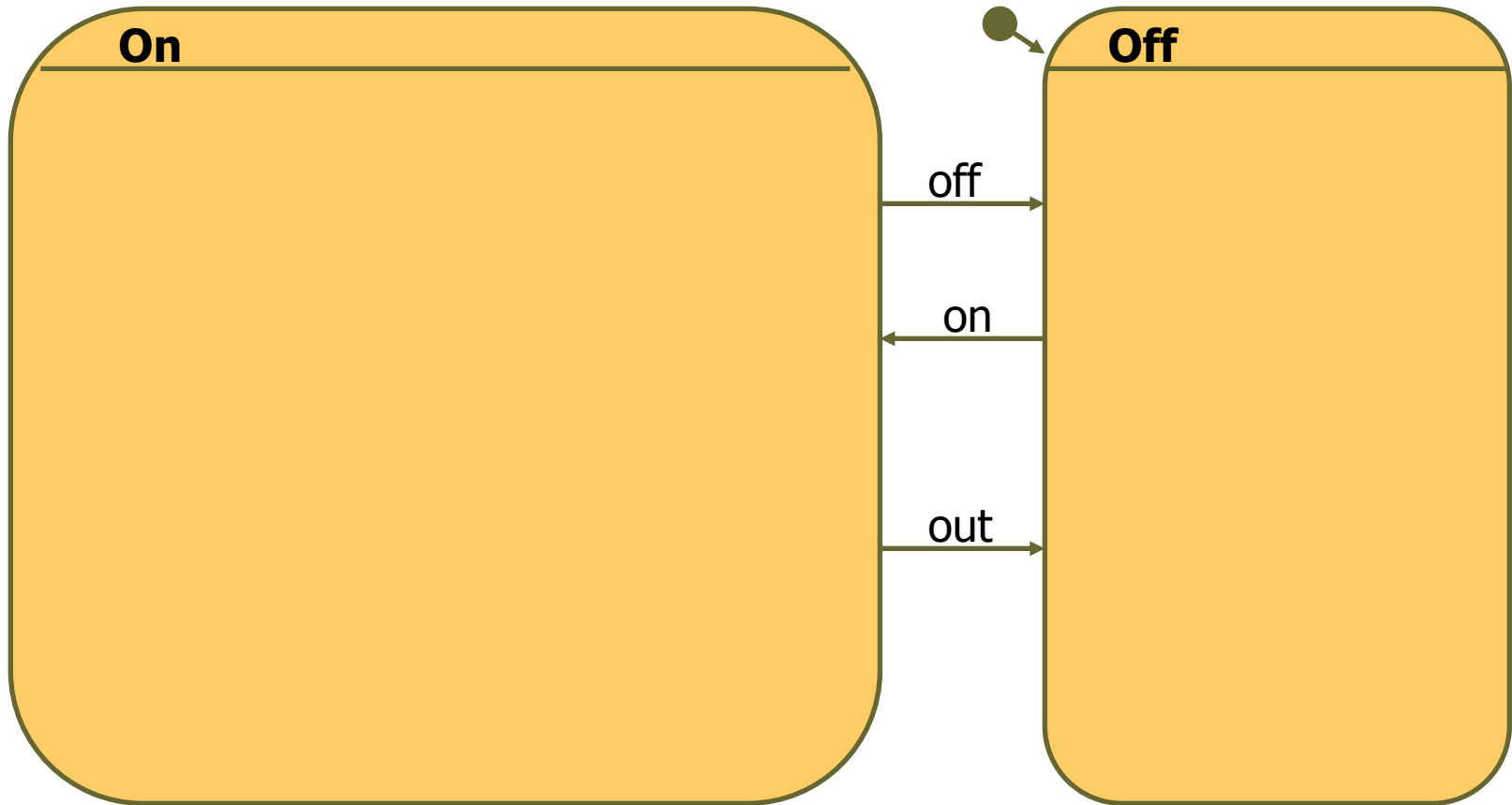
States: Actions and state refinement

- State: Basic modeling element
- Actions assigned to states:
 - Entry action (**entry** / ...)
 - Exit action (**exit** / ...)
 - Internal actions (**do** / ..., **<event>** / ...)
- State refinement
 - **Simple state**: no refinement
 - **OR-refinement**: substates of a superstate
 - Exactly one substate is active when the superstate is active
 - **AND-refinement**: **concurrent regions**
 - One substate in every region is active when superstate is active

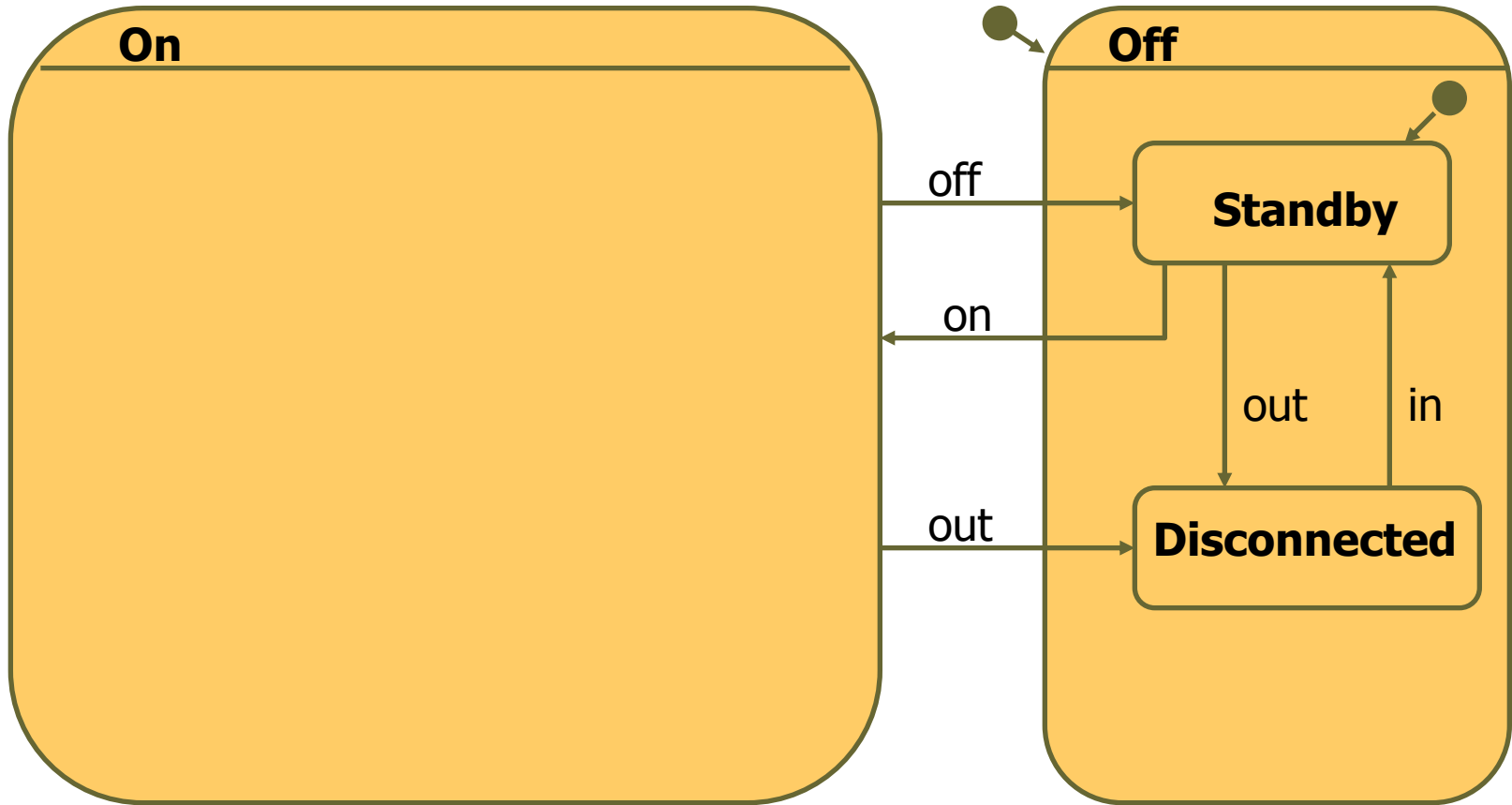
print_job

entry / init()
exit / reset()
do / poll()
job / print()

Example: State refinement

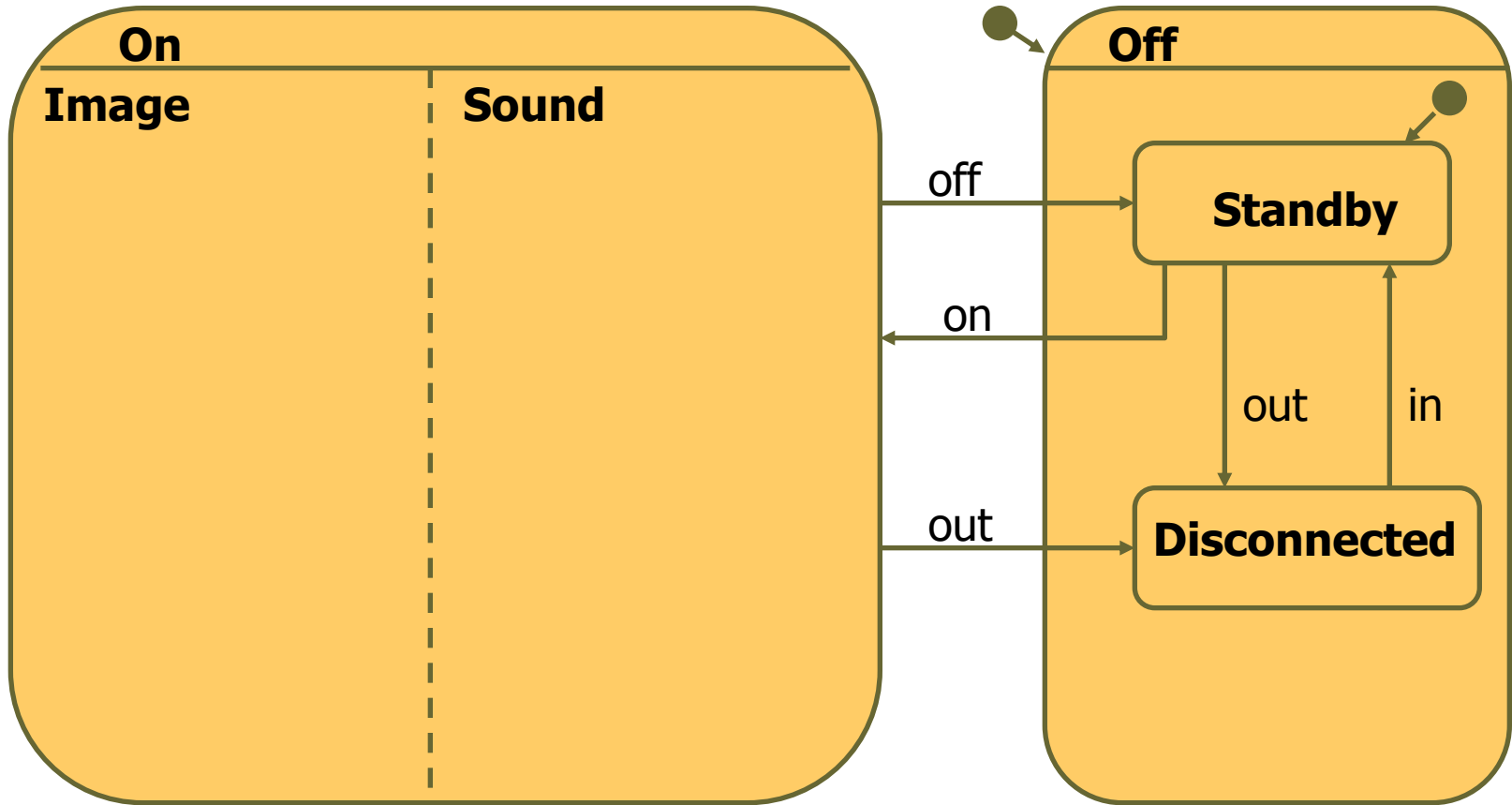


Example: State refinement



OR-refinement

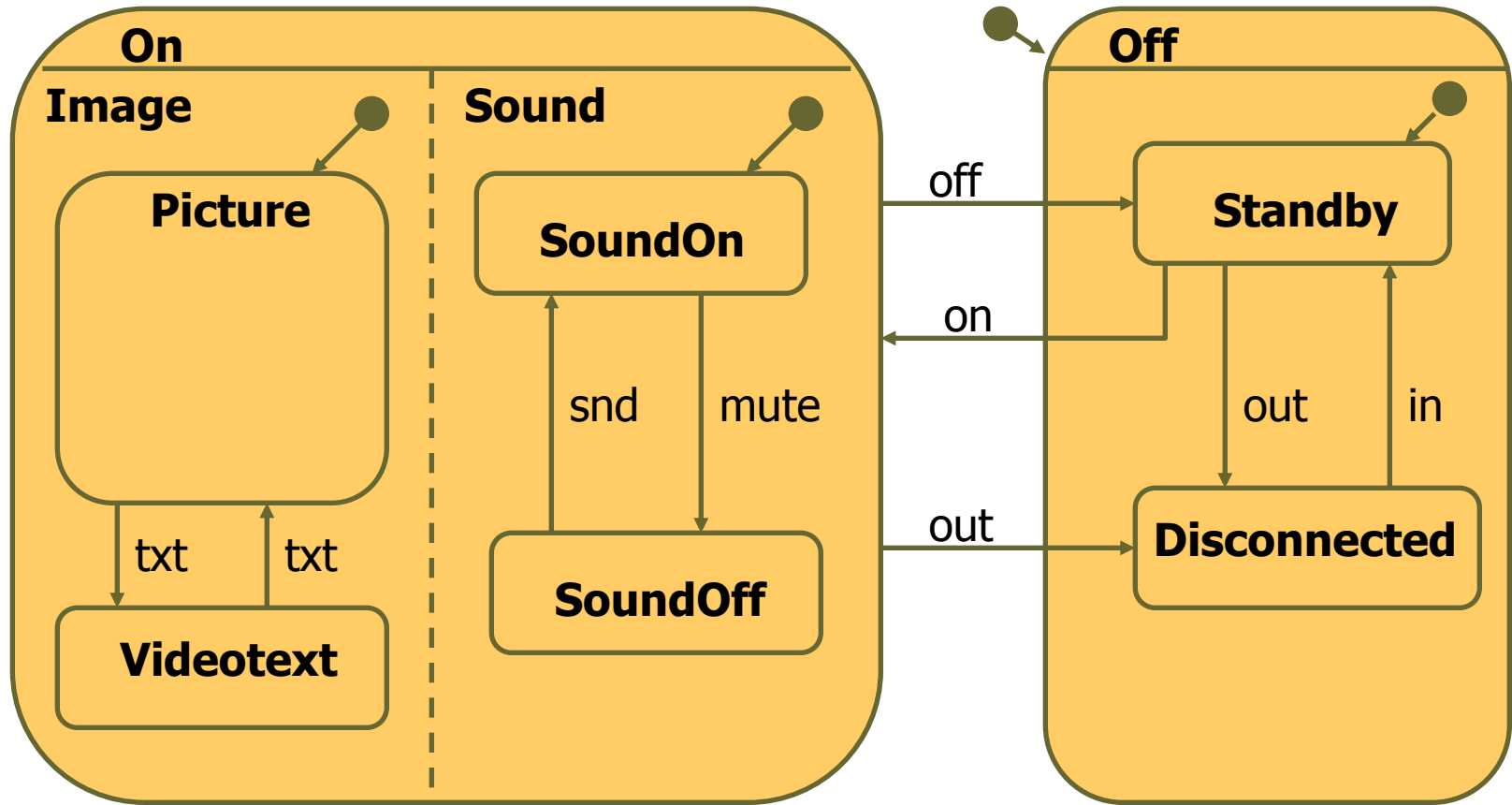
Example: State refinement



AND-refinement

OR-refinement

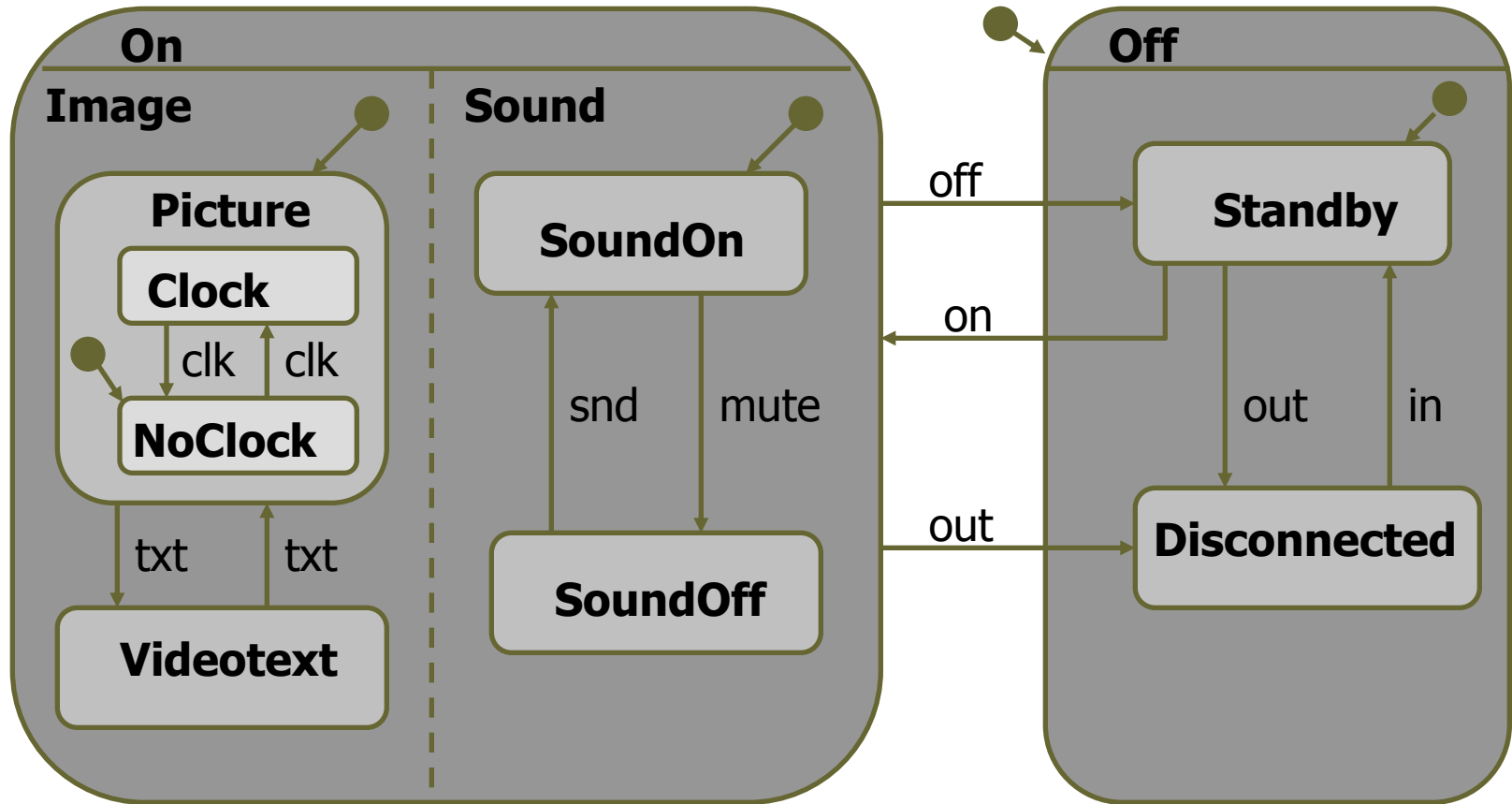
Example: State refinement



AND+OR-refinement

OR-refinement

Example: State refinement

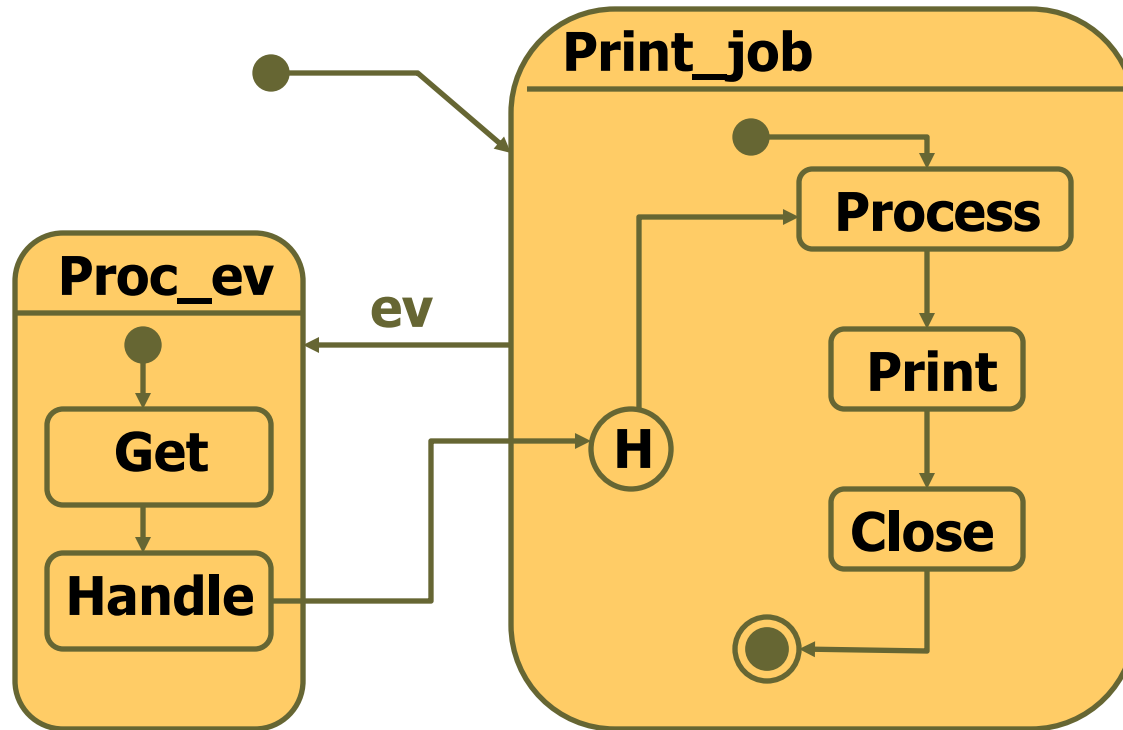


Pseudostates

- **Initial state:** activated when superstate is activated
 - Should be one in every OR-refinement
 - Should be one in every region of an AND-refinement
- **Final state:** behavior terminates
- **History states:**
 - “Stores” last active state configuration
 - **Simple** history state: only on given hierarchy level
 - **Deep** history state: remembers lower levels as well
 - In a region of an AND-refinement: Only **for the region**
 - What is the meaning of a transition **entering** the history state?
 - When executed, the stored state configuration is restored
 - What is the meaning of a transition **leaving** the history state?
 - Gives the **default state** in case the region has not been activated before



Example: History state



(State) transitions

- Specification of the change of state configuration
- Syntax:

trigger [guard] / **action**

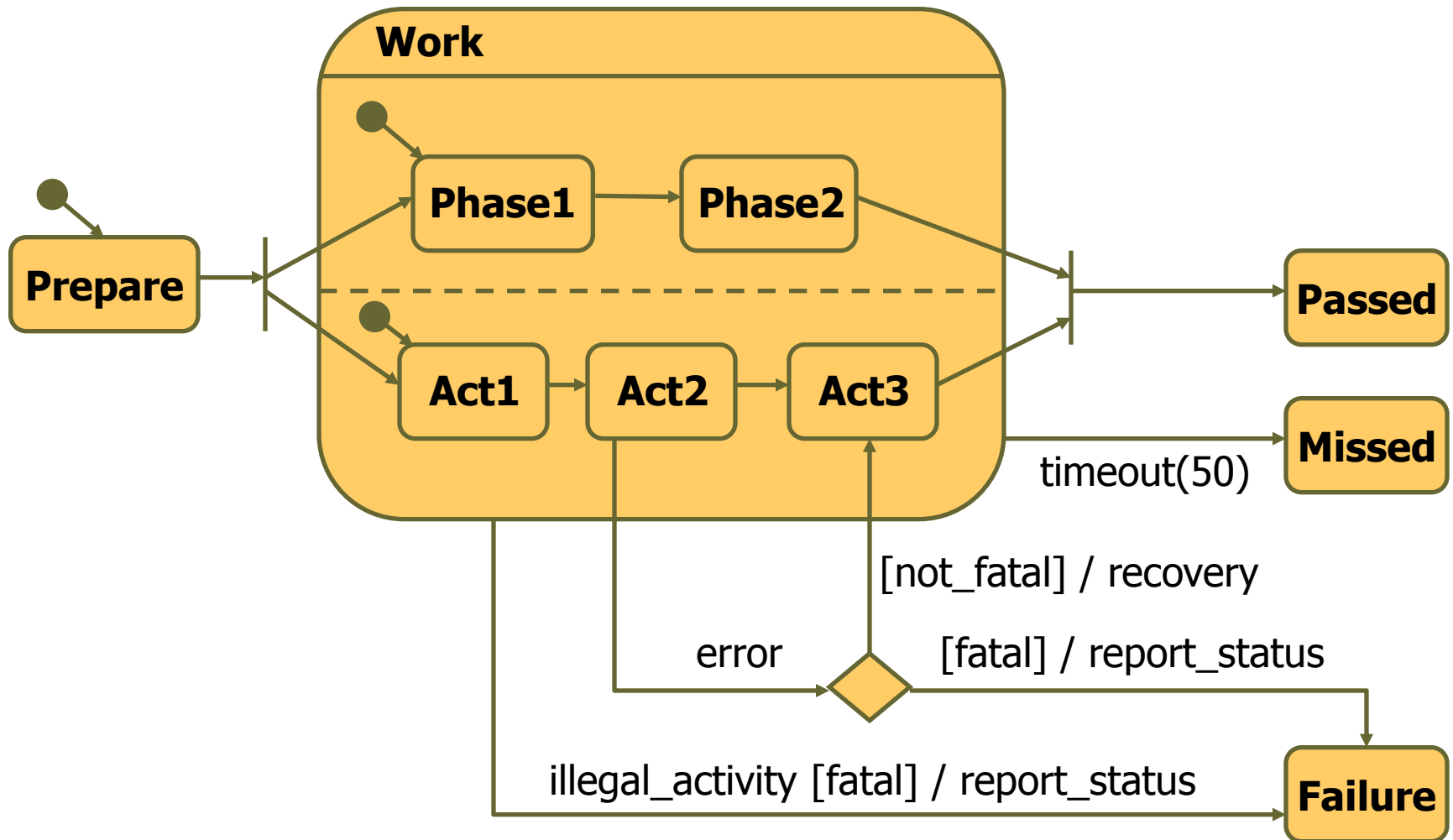


- **trigger**: triggering event
- **guard**: guard condition of the state
 - Predicate over state variables and parameters of the event
 - May also refer to states: `is_in(state)`
- **action**: operation
 - Action semantics: atomic operation

Special transitions

- Complex transitions
 - **Fork**: to enter multiple states, each in a concurrent region
 - **Join**: leave states in concurrent regions simultaneously
 - **Branching (condition)**: combined notation for multiple transitions differing in guard conditions and actions (segments)
- Transitions crossing hierarchy levels
 - Permitted (although not elegant)
- Time-out as a trigger
 - Occurs when the source state has been active for the specified time

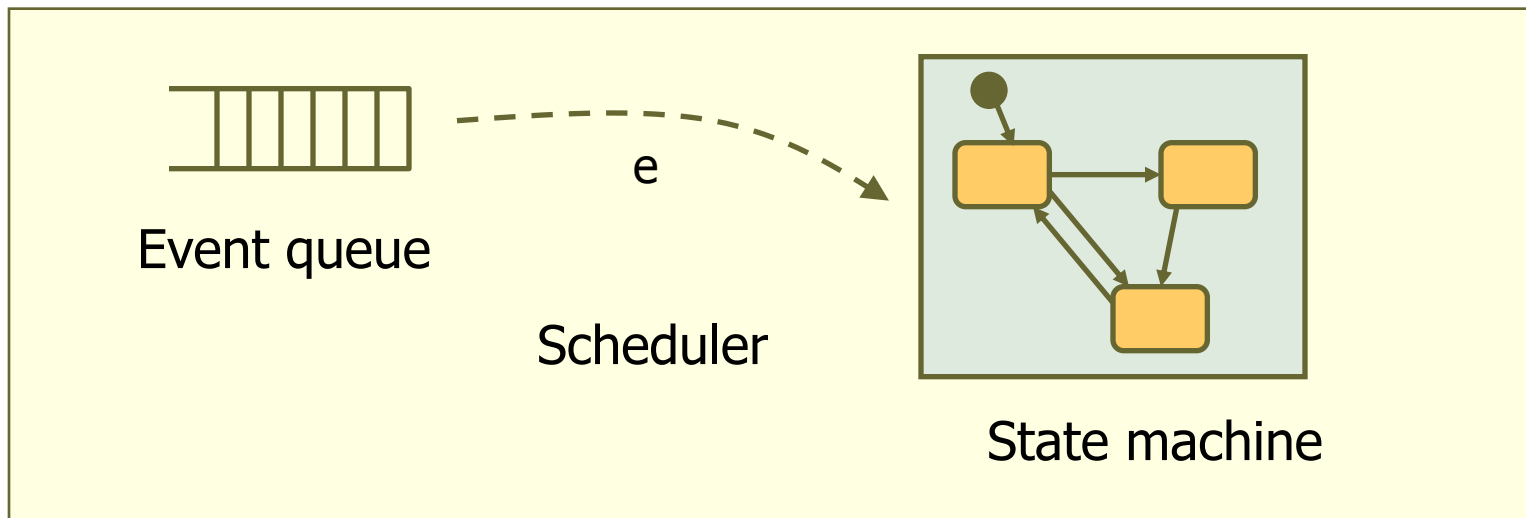
Example: State transitions



Formal semantics of statecharts (conforming to UML)

Semantics: How does it work?

- Basic elements:
 - State machine: Its behavior described by the statechart
 - Event queue + Scheduler: „runtime environment“ (external elements)



What is specified by the semantics?

Behavior of the state machine when processing an event → a step of the state machine

- Transitions “fire”
 - A single event may trigger multiple concurrent transitions (in active regions)
- Change of state configuration
 - There may be multiple active states
 - One active substate in every region of an active superstate
 - One active substate in an active OR-refined superstate
 - Superstate of an active state is also active
 - Applied recursively

Basic properties of the semantics

- Events are processed one by one
 - The scheduler passes the new event only if the previous event has been completely processed
 - Stable state configuration: no enabled spontaneous transitions
- Complete processing of events (run to completion)
 - Maximal set of transitions fire
 - Every enabled transition will fire unless prevented by a conflict
 - After firing all of these, the next event is passed
- The main point of the semantics is the event processing
 - Based on this, the statechart can be implemented by software (source code generation)

Steps of event processing 1/4

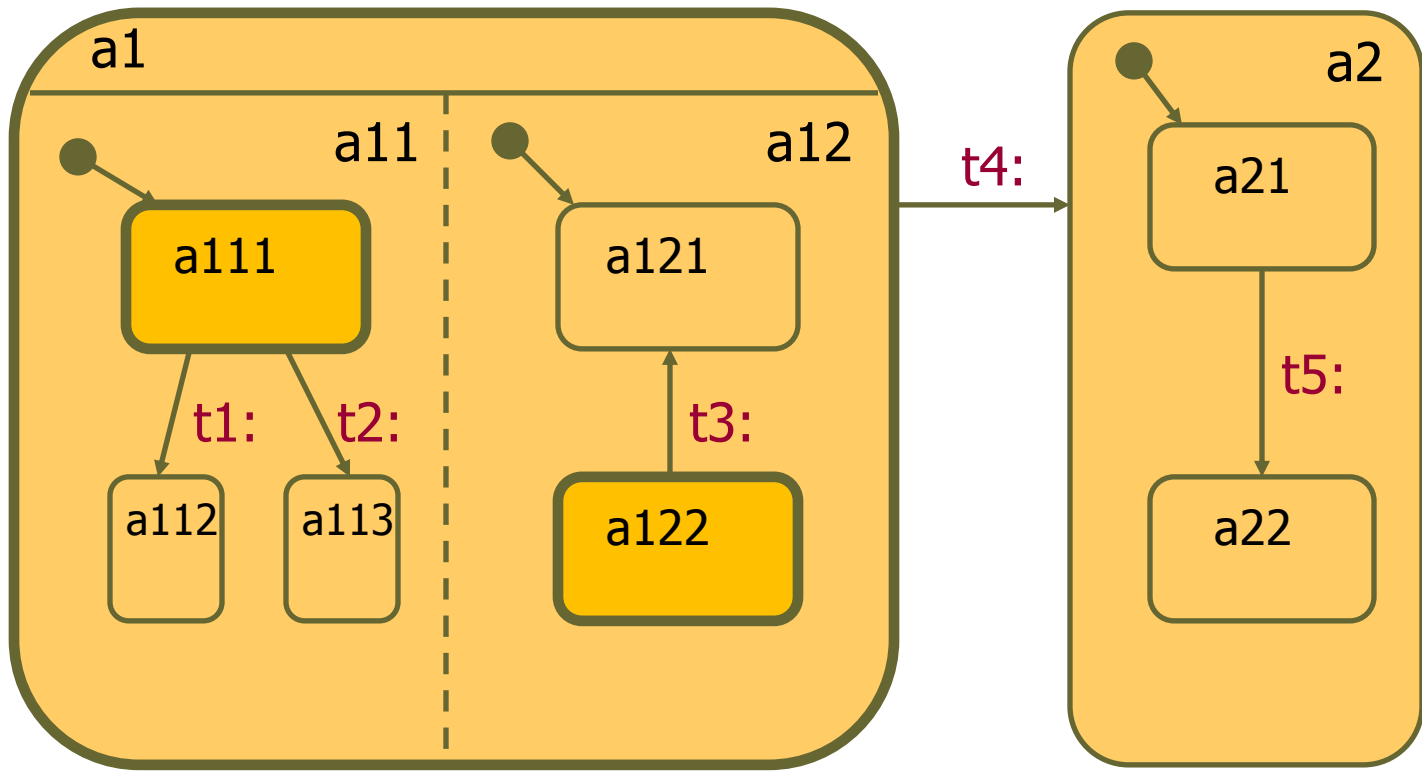
- External condition: The scheduler passes an event to the stable state machine
- Enabled transitions:
 - Source state is active
 - Selected event triggers transition
 - Guard condition is true

Based on the number of enabled transitions:

- If only one: Fire!
- If none: Is the event delayed?
 - Yes: store it, wait for a new event
 - No: event may be discarded (without any actions)
- If multiple transitions: Need to **select** transitions to fire
 - Based on: **conflicts**

Example: Conflict

In this example, transitions $t1, \dots, t5$ are triggered by the same event e . Active states are denoted by thicker borders.



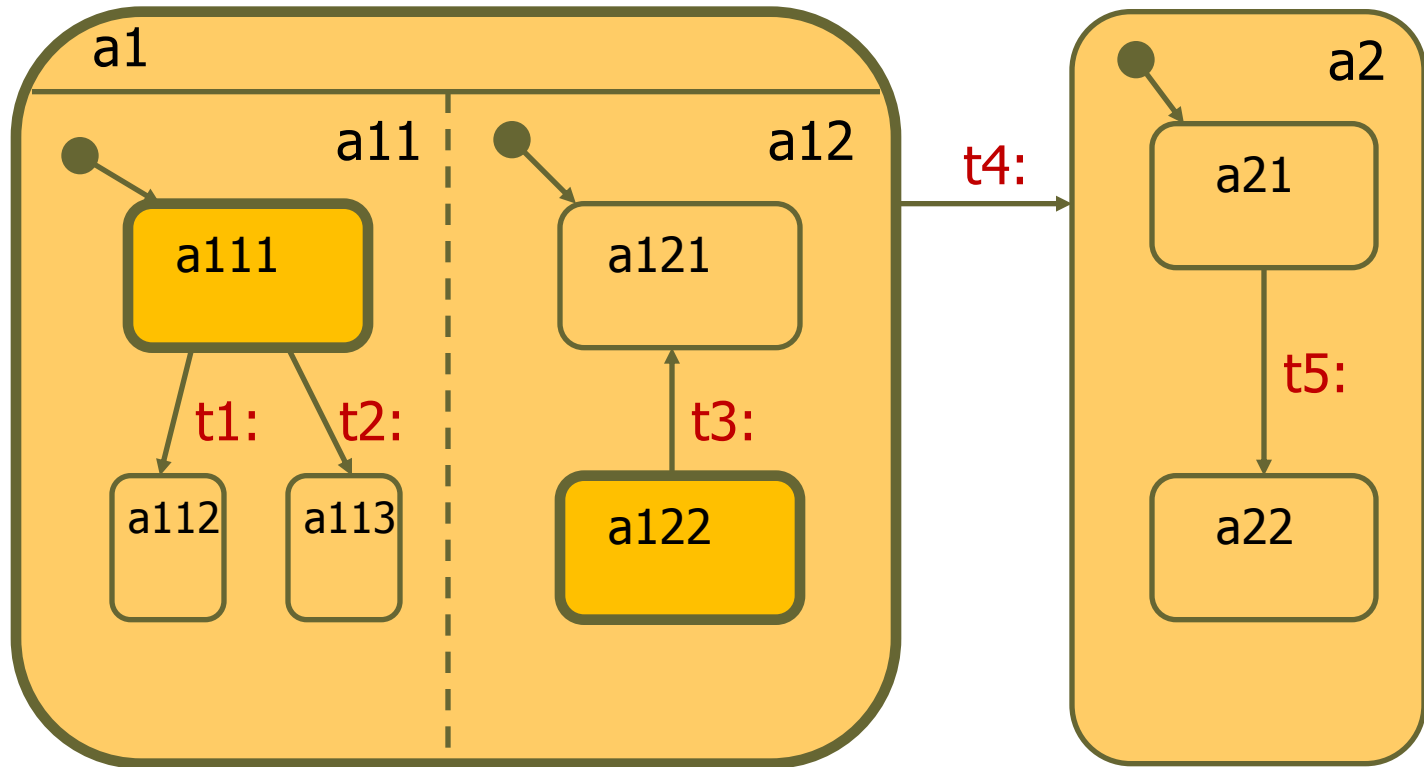
- Not enabled: $t5$ (source state inactive)
- Cannot fire together: $(t1, t2)$; $(t4, t1)$; $(t4, t2)$; $(t4, t3)$
- May fire together: $(t1, t3)$; $(t2, t3)$;

Steps of event processing 2/4

- **Fireable transitions are selected:**
 - Maximal number of transitions without conflict
 - Simultaneous firing of concurrent transitions
- **Conflict between transitions:**
 - They leave the same state, that is, the intersection of the sets of states inactivated is non-empty
- **Resolving conflicts:**
 - **Based on priority:** the priority of a transition is higher if its source state is lower in the refinement hierarchy
 - OO concept: refinement “overrides” behavior
 - **Nondeterministic choice** in case of the same priority

Example: Conflict resolution

Transitions t_1, \dots, t_5 are triggered by the same event e .
Which may fire together in the active state configuration?

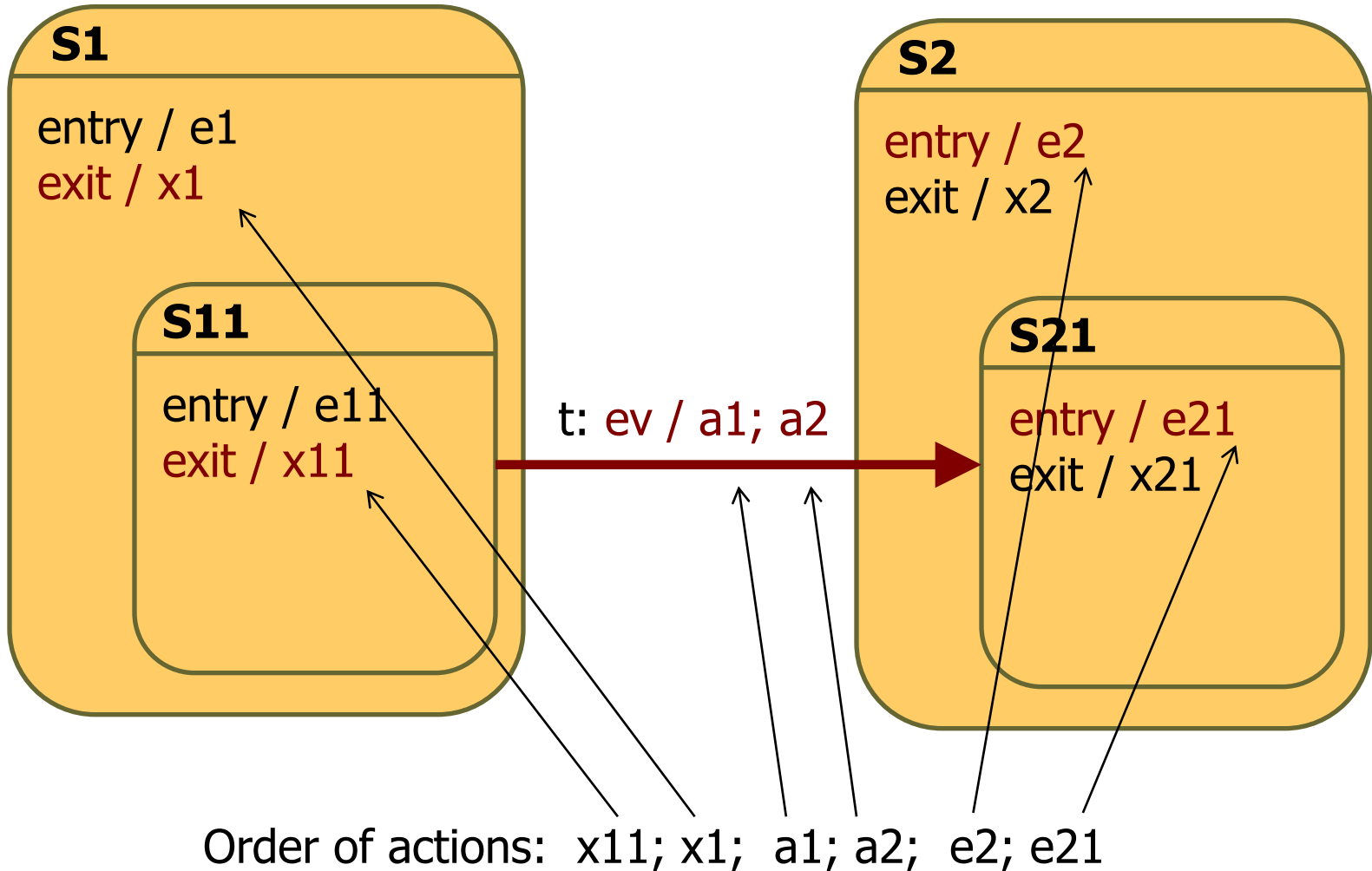


- Higher priority than t_4 : t_1 , t_2 and t_3
- Cannot fire together: (t_1, t_2) ; (t_4, t_1) ; (t_4, t_2) ; (t_4, t_3)
- Fireable: (t_1, t_3) or (t_2, t_3)

Steps of event processing 3/4

- Selected transitions **fire**:
 - In a **nondeterministic order** (no conflict among them)
 - Therefore the order of actions is also nondeterministic
- Firing of a single transition:
 1. Source states are **exited**
 - On lower hierarchy levels first
 - **Exit** actions are executed in this order
 2. Action(s) of the transition are **executed**
 3. Target states are **entered** → new configuration
 - On higher hierarchy levels first
 - **Entry** actions are executed in this order

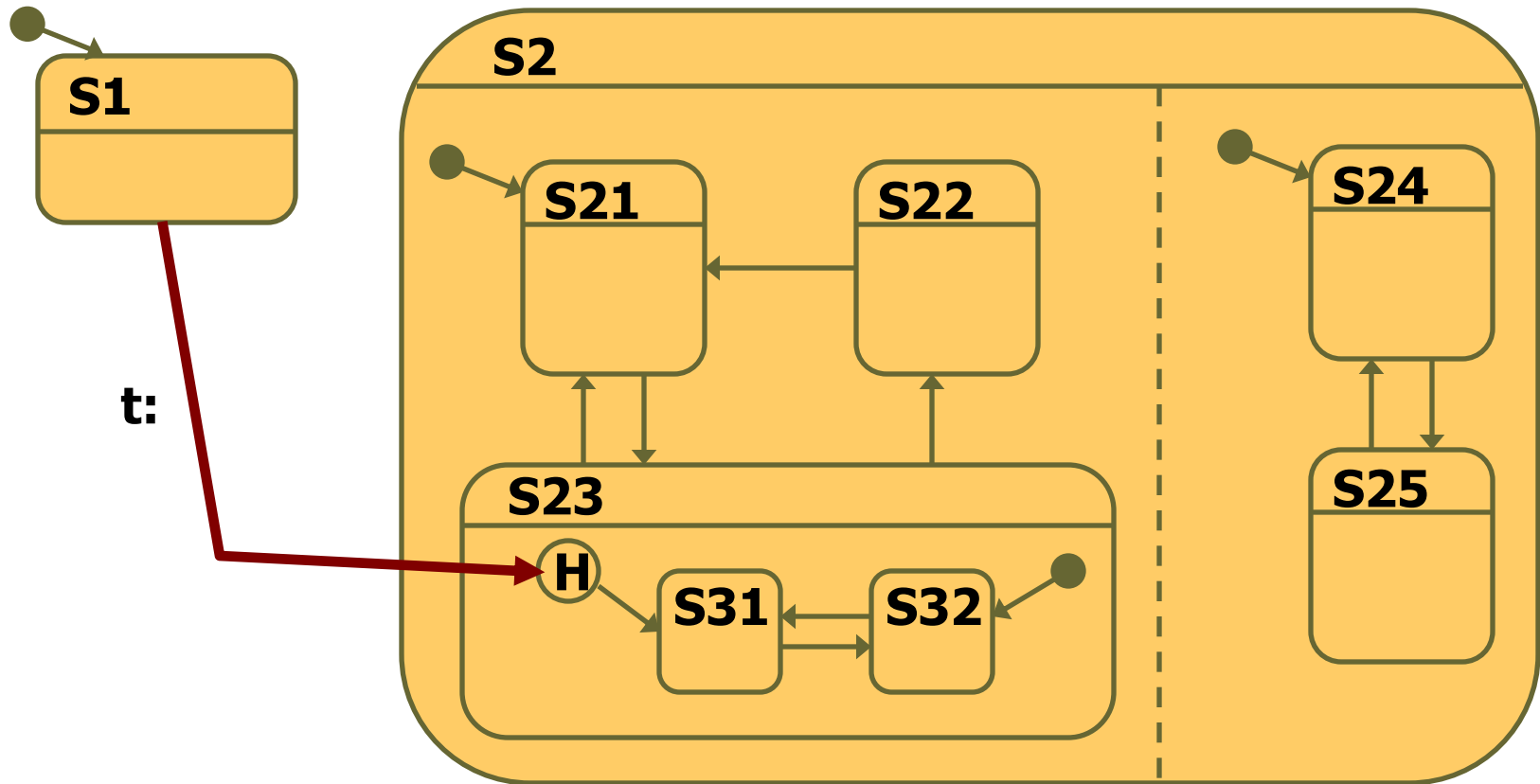
Example: Ordering of actions



Steps of event processing 4/4

- **Entering** new configuration in case of different target states:
 - If target state is **simple** (not refined) :
 - Will be part of the new configuration
 - Its superstates (in which it is a substate) also activated
 - Activated superstates will activate a substate in each of their concurrent regions (determined by initial state)
 - If target state has **OR-refinement**:
 - Its initial substate is activated
 - If target state has **AND-refinement**:
 - Its initial substates are activated in every region
 - If **history** state:
 - The most recent state configuration is reactivated
 - If this is the first activation: default state is activated
 - If state is **not stable**: proceed immediately to the next

Example: Entering a concurrent state

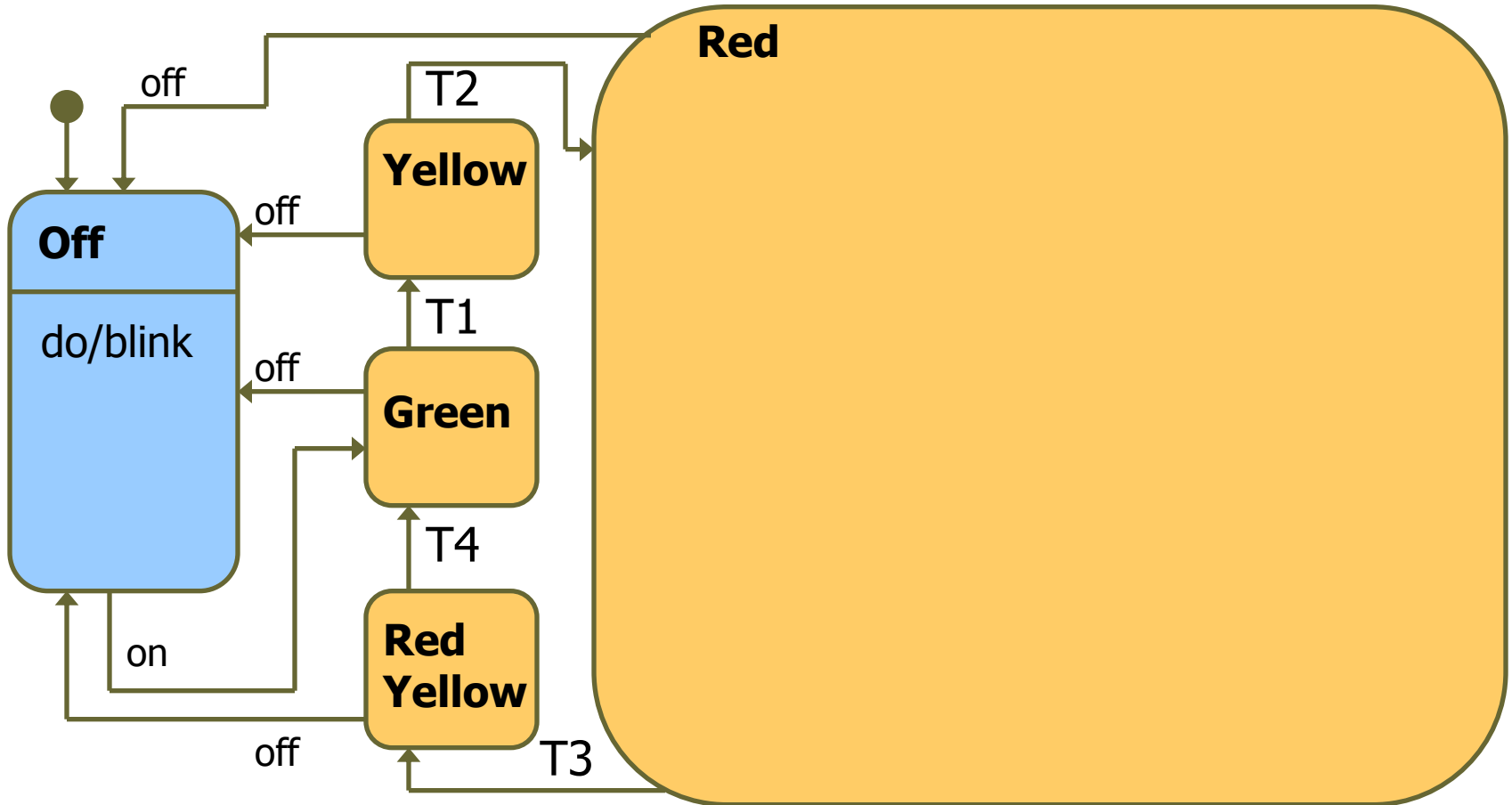


What will be the new state configuration after firing transition **t**?

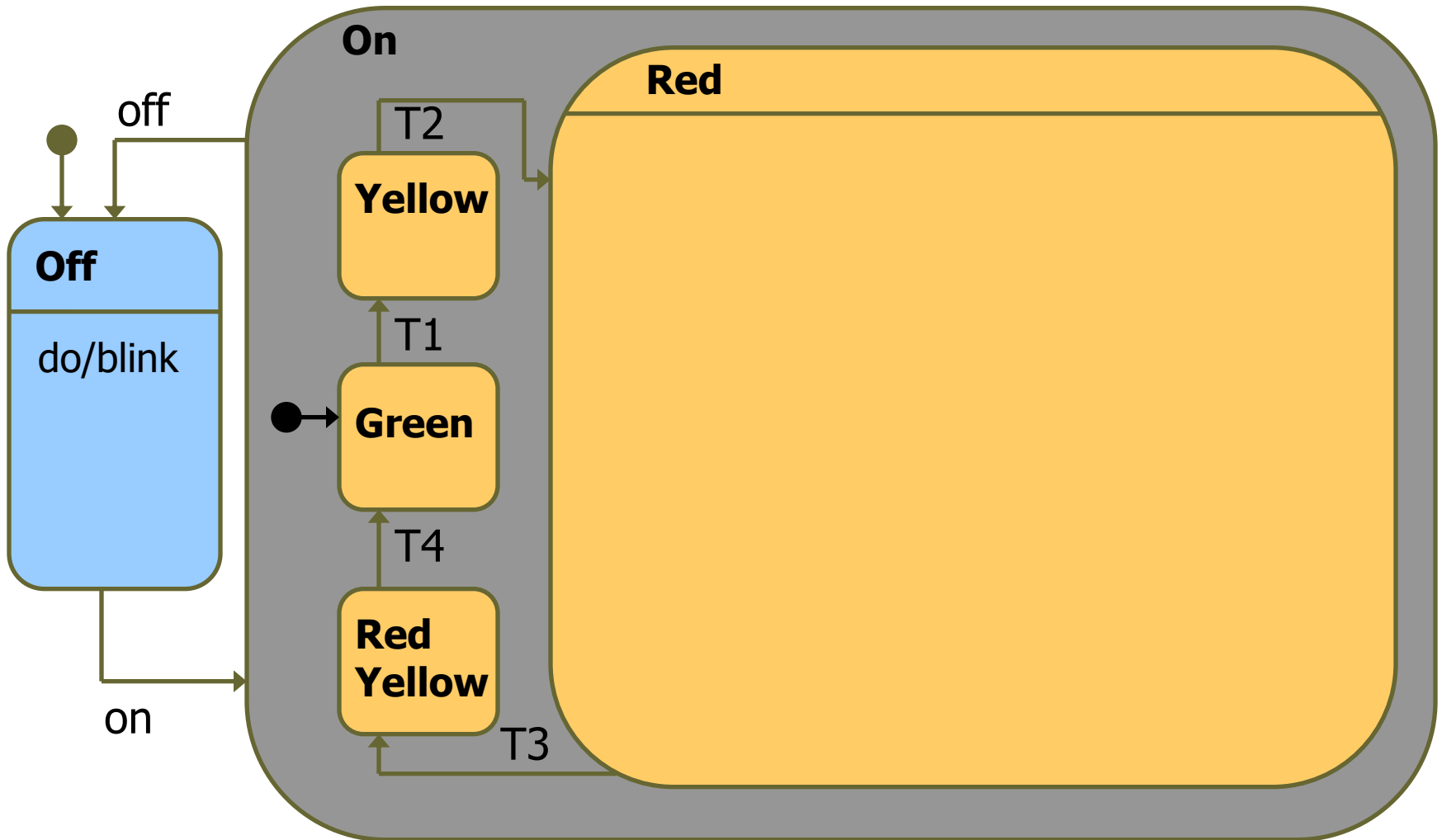
Modeling example

- Traffic light controller in the intersection of a main road with a side road
 - Off: blinking yellow
 - When turned on: green for the main road
 - Green, yellow, red cycle: triggered by timer events
 - If at least 3 cars waiting on the main road: switch to green regardless of timers
 - Automatically take photos of vehicles crossing the main road during the red light
 - Manually switch on/off for this feature

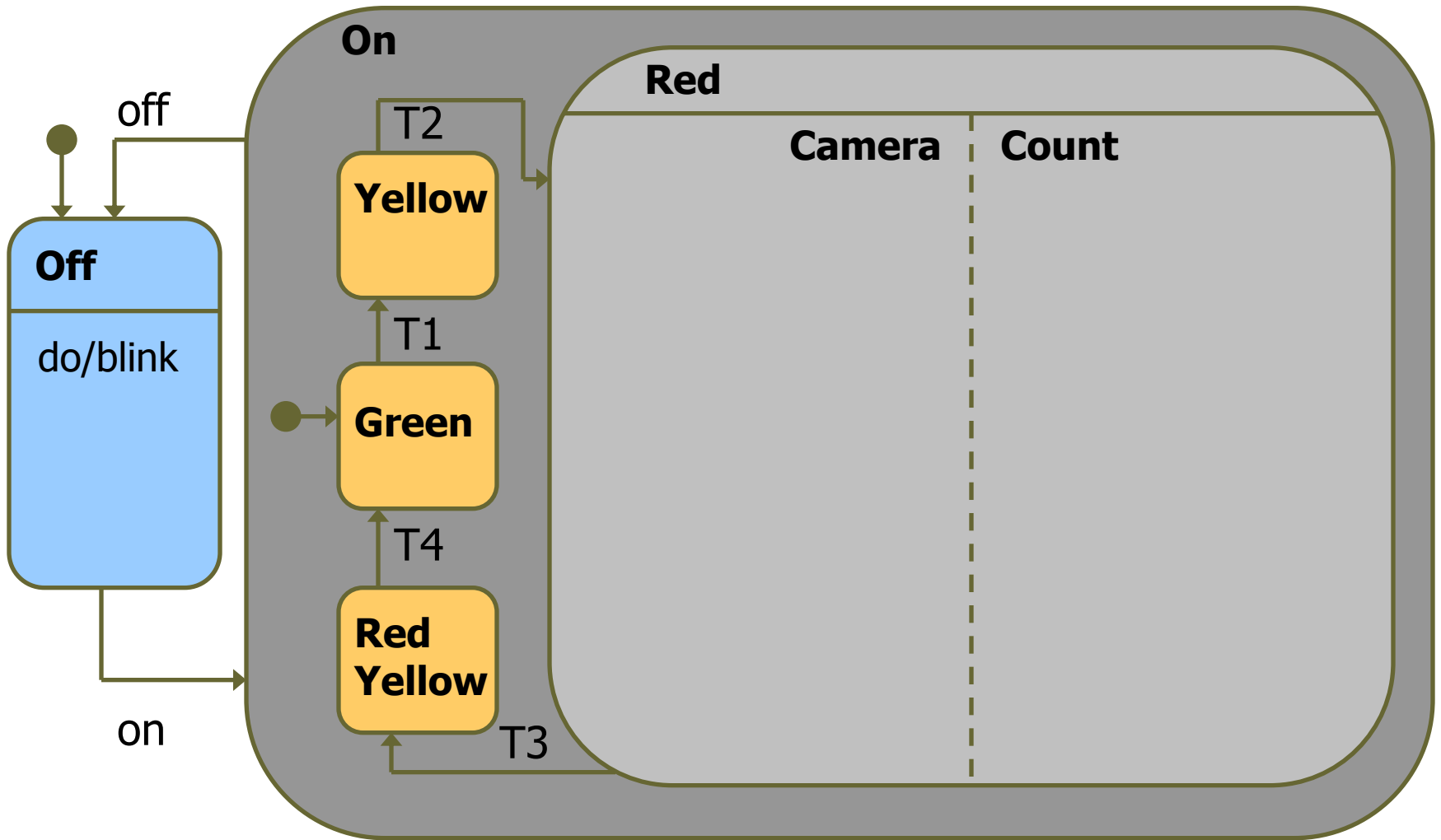
1. Main cycle (for the main road)



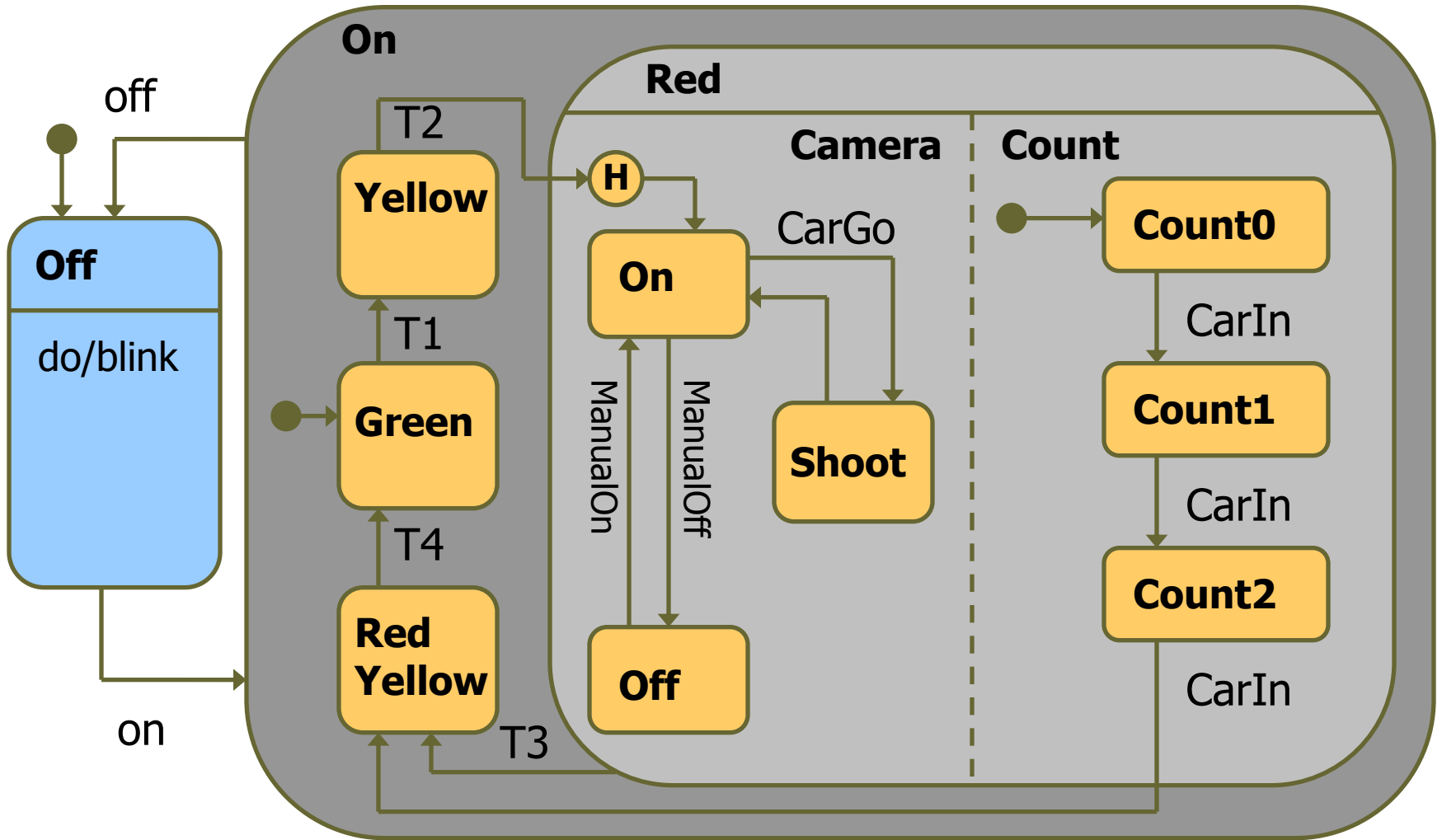
2. With state hierarchy



3. Concurrent regions



4. Complete controller



Role of statecharts in UML 2

- Description of state-based, event-driven behavior
 - To model the behavior of an active object
- Formalizing actions: UML 2 Action Semantics
 - Method call
 - Read/write attributes
 - ... (many possible operations)
 - Ideas similar to Colored Petri nets
- Formalizing actions: There are other alternatives (e.g., Alf)

What can we do with statecharts?

- Generating source code
 - Multiple templates
- Model checking
 - Temporal logics can be “customized” for statecharts
 - May be verified by transforming to low-level model
- Generating tests
 - Can be realized with a model checker
- Generating monitor code for runtime verification
 - Statechart as a reference (specifies valid behavior to be compared to the implementation)

Basics of statecharts (summary)

- Extensions
- Statechart syntax
 - State hierarchy, concurrent regions, history states
 - Complex transitions
- Statechart semantics
 - Enabled transitions
 - Selection of fireable transitions
 - Firing transitions
 - Forming a new state configuration
- Statechart tools
 - UML 2 toolsets
 - Yakindu Statechart Tools (statecharts.org)
 - Quantum Programming (state-machine.com)